

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE

GAN

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

(Adapted from Eleanor Quint and Ian Goodfellow)

sscott@cse.unl.edu



Introduction

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction
Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AE

Variational AE

· anatona ·

t-SNE

- Autoencoding is training a network to replicate its input to its output
- Applications:
 - Unlabeled pre-training for semi-supervised learning
 - Learning embeddings to support information retrieval
 - Generation of new instances similar to those in the training set
 - Data compression



Outline

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction Basic Idea

Stacked AE

Transposed

Convolutions Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE GAN

- Basic idea
- Stacking
- Types of autoencoders
 - Denoising
 - Sparse
 - Contractive
 - Variational
 - Generative adversarial networks



CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

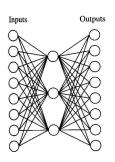
Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE



Input	Hidden					Output
-		7	Values	3		
10000000	\rightarrow	.89	.04	.08	\rightarrow	10000000
01000000	\rightarrow	.15	.99	.99	\rightarrow	01000000
00100000	\rightarrow	.01	.97	.27	\rightarrow	00100000
00010000	\rightarrow	.99	.97	.71	\rightarrow	00010000
00001000	\rightarrow	.03	.05	.02	\rightarrow	00001000
00000100	\rightarrow	.01	.11	.88	\rightarrow	00000100
00000010	\rightarrow	.80	.01	.98	\rightarrow	00000010
00000001	\rightarrow	.60	.94	.01	\rightarrow	00000001

- Sigmoid activation functions, 5000 training epochs, square loss, no regularization
- What's special about the hidden layer outputs?



496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

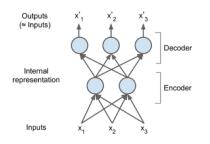
Sparse AE

Contractive AF

Variational AE

t-SNF GAN

 An autoencoder is a network trained to learn the **identity function:** output = input



- Subnetwork called **encoder** $f(\cdot)$ maps input to an embedded representation
- Subnetwork called **decoder** $g(\cdot)$ maps back to input space
- Can be thought of as lossy compression of input
- Need to identify the important attributes of inputs to reproduce faithfully





496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE

- General types of autoencoders based on size of hidden layer
 - **Undercomplete** autoencoders have hidden layer size smaller than input layer size
 - ⇒ Dimension of embedded space lower than that of input space
 - ⇒ Cannot simply memorize training instances
 - Overcomplete autoencoders have much larger hidden layer sizes
 - ⇒ Regularize to avoid overfitting, e.g., enforce a sparsity constraint



Example: Principal Component Analysis

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

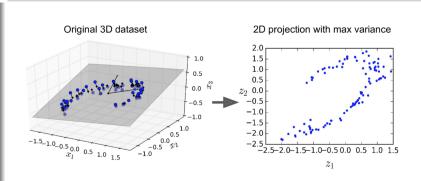
Sparse AE

Contractive AF

Variational AE

t-SNF

GAN



 A 3-2-3 autoencoder with linear units and square loss performs principal component analysis: Find linear transformation of data to maximize variance



CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

Contractive

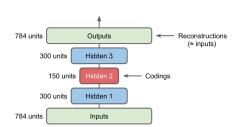
Variational AE

variational AE

t-SNF

GAN

AF



 A stacked autoencoder has multiple hidden layers

• Can share parameters to reduce their number by exploiting symmetry: $W_4 = W_1^{\top}$ and $W_3 = W_2^{\top}$

```
weights1 = tf.Variable(weights1_init, dtype=tf.float32, name="weights1")
weights2 = tf.Variable(weights2_init, dtype=tf.float32, name="weights2")
weights3 = tf.transpose(weights2, name="weights3")  # shared weights
weights4 = tf.transpose(weights1, name="weights4")  # shared weights
```



Incremental Training

496/896 Lecture 5: Autoencoders Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

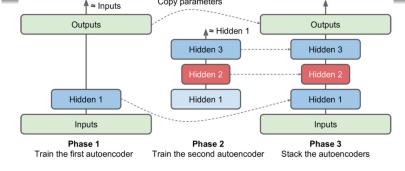
Sparse AE

Contractive AF

Variational AE

t-SNF

GAN



Copy parameters

- Can simplify training by starting with single hidden laver H_1
- Then, train a second AE to mimic the output of H₁
- Insert this into first network
- Can build by using H₁'s output as training set for Phase 2





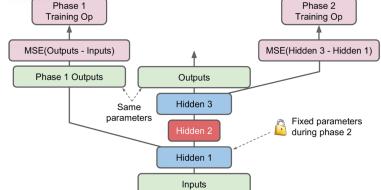
Incremental Training (Single TF Graph)

Phase 1 Phase 2 CSCE Training Op Training Op 496/896 Lecture 5: Autoencoders MSE(Outputs - Inputs) MSE(Hidden 3 - Hidden 1) Stephen Scott Phase 1 Outputs Outputs Introduction Basic Idea Hidden 3 Same Stacked AE parameters Fixed parameters Transposed during phase 2 Convolutions Denoising AE Hidden 1 Sparse AE

Previous approach requires multiple TensorFlow graphs

4 D > 4 A > 4 B > 4 B > B 9 9 0

 Can instead train both phases in a single graph: First left side, then right



Contractive AF Variational AE

t-SNE GAN



Stacked Autoencoders Visualization

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

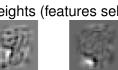
Sparse AE

Contractive AF

Variational AE

t-SNE

GAN









Input MNIST Digit

Network Output





Weights (features selected) for five nodes from H_1 :



Semi-Supervised Learning

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

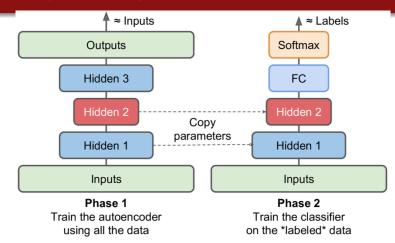
Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE



- Can pre-train network with unlabeled data
- ⇒ learn useful features and then train "logic" of dense layer with labeled data





Transfer Learning from Trained Classifier

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

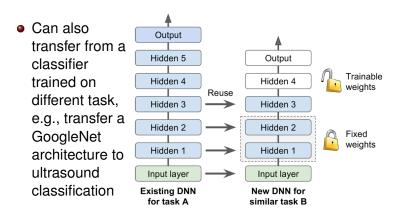
Sparse AE

Contractive AF

Variational AE

t-SNE

GAN



Often choose existing one from a model zoo



Transposed Convolutions

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNF

- What if some encoder layers are convolutional? How to upsample to original resolution?
- Can use, e.g., linear interpolation, bilinear interpolation, etc.
- Or, transposed convolution, e.g., tf.layers.conv2d_transpose



Transposed Convolutions (2)

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

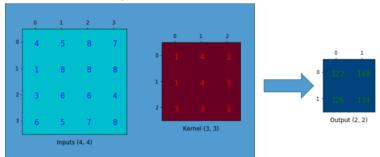
Sparse AE

Contractive AF

Variational AE

t-SNE **GAN**

Consider this example convolution





Transposed Convolutions (3)

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AF

Variational AE

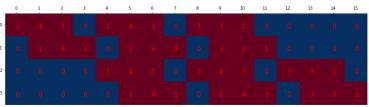
t-SNE

GAN









Convolution Matrix (4, 16)



Transposed Convolutions (4)

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

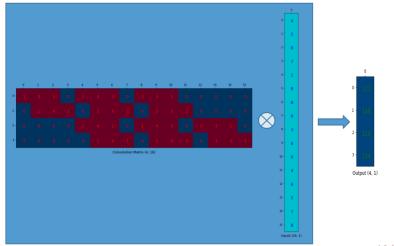
Contractive AF

Variational AE

t-SNE

GAN

This representation works with matrix multiplication on flattened input:





Transposed Convolutions (5)

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

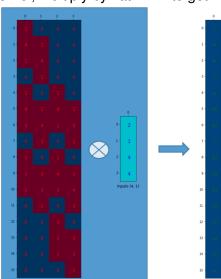
Contractive AF

Variational AE

t-SNE

GAN

Transpose kernel, multiply by flat 2×2 to get flat 4×4





Denoising Autoencoders Vincent et al. (2010)

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive

Variational AE

t-SNE GAN

- Can train an autoencoder to learn to denoise input by giving input **corrupted** instance \tilde{x} and targeting **uncorrupted** instance x
- Example noise models:
 - Gaussian noise: $\tilde{x} = x + z$, where $z \sim \mathcal{N}(\mathbf{0}, \sigma^2 I)$
 - Masking noise: zero out some fraction ν of components of x
 - Salt-and-pepper noise: choose some fraction ν of components of x and set each to its min or max value (equally likely)



Denoising Autoencoders

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

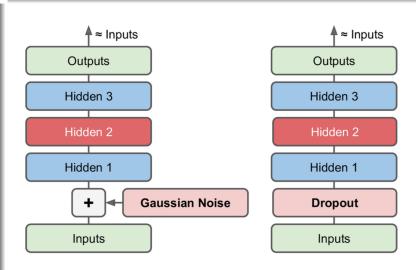
Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE





Denoising Autoencoders Example

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed

Convolutions Denoising AE

Sparse AE

Contractive ΑE

Variational AE

t-SNE







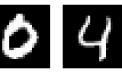




















Denoising Autoencoders

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE Transposed

Convolutions

Denoising AE

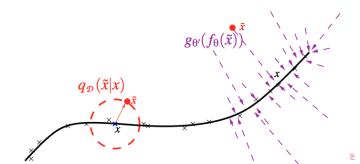
Sparse AE

Contractive

Variational AE

t-SNE

- How does it work?
- Even though, e.g., MNIST data are in a 784-dimensional space, they lie on a low-dimensional manifold that captures their most important features
- Corruption process moves instance x off of manifold
- Encoder f_{θ} and decoder $g_{\theta'}$ are trained to project \tilde{x} back onto manifold





Sparse Autoencoders

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed

Convolutions

Denoising AE

Sparse AE

Contractive

Variational AE

variational At

t-SNE

GAN

An overcomplete architecture

Regularize outputs of hidden layer to enforce sparsity:

$$\tilde{\mathcal{J}}(\mathbf{x}) = \mathcal{J}(\mathbf{x}, g(f(\mathbf{x}))) + \alpha \Omega(\mathbf{h})$$
,

where \mathcal{J} is loss function, f is encoder, g is decoder, h = f(x), and Ω penalizes non-sparsity of h

- E.g., can use $\Omega(\mathbf{h}) = \sum_i |h_i|$ and ReLU activation to force many zero outputs in hidden layer
- Can also measure average activation of h_i across mini-batch and compare it to user-specified target sparsity value p (e.g., 0.1) via square error or Kullback-Leibler divergence:

$$p\log\frac{p}{q} + (1-p)\log\frac{1-p}{1-q}$$
,

where q is average activation of h_i over mini-batch



Contractive Autoencoders

496/896 Lecture 5:

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

Contractive

Variational AE

variational At

t-SNE

GAN

Similar to sparse autoencoder, but use

$$\Omega(\mathbf{h}) = \sum_{j=1}^{m} \sum_{i=1}^{n} \left(\frac{\partial h_i}{\partial x_j} \right)^2$$

- I.e., penalize large partial derivatives of encoder outputs wrt input values
- This **contracts** the output space by mapping input points in a neighborhood near x to a smaller output neighborhood near f(x)
 - ⇒ Resists perturbations of input x
- If h has sigmoid activation, encoding near binary and a CE pushes embeddings to corners of a hypercube



496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea Stacked AE

Transposed

Convolutions

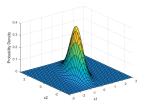
Denoising AE Sparse AE

Contractive

Variational AE

t-SNE

- VAE is an autoencoder that is also generative model
 - ⇒ Can generate new instances according to a probability distribution
 - E.g., hidden Markov models, Bayesian networks
 - Contrast with discriminative models, which predict classifications
- Encoder f outputs $[\mu, \sigma]^{\top}$
 - Pair (μ_i, σ_i) parameterizes Gaussian distribution for dimension $i = 1, \ldots, n$
 - Draw $z_i \sim \mathcal{N}(\mu_i, \sigma_i)$
 - Decode this latent variable z to get g(z)





Variational Autoencoders Latent Variables

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

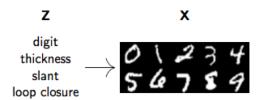
Contractive

Variational AE

t-SNE GAN

Independence of z dimensions makes it easy to generate instances wrt complex distributions via decoder g

- Latent variables can be thought of as values of attributes describing inputs
 - E.g., for MNIST, latent variables might represent "thickness", "slant", "loop closure"





Variational Autoencoders Architecture

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

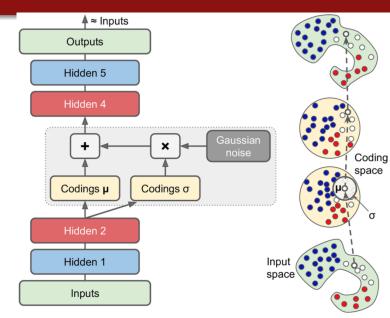
Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE





Variational Autoencoders Optimization

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction Basic Idea

Stacked AE

Transposed

Convolutions Denoising AE

Sparse AE

Variational AE

t-SNE GAN

Contractive

 Maximum likelihood (ML) approach for training generative models: find a model (θ) with maximum probability of generating the training set \mathcal{X}

- Achieve this by minimizing the sum of:
 - End-to-end AE loss (e.g., square, cross-entropy)
 - Regularizer measuring distance (K-L divergence) from latent distribution $q(z \mid x)$ and $\mathcal{N}(\mathbf{0}, I)$ (= standard multivariate Gaussian)
- $\mathcal{N}(\mathbf{0}, I)$ also considered the **prior distribution** over z (= distribution when no x is known)

```
eps = 1e-10
latent loss = 0.5 * tf.reduce sum(
        tf.square(hidden3_sigma) + tf.square(hidden3_mean)
        - 1 - tf.log(eps + tf.square(hidden3_sigma)))
```



Reparameterization Trick

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed

Convolutions

Denoising AE

Sparse AE

Contractive AE

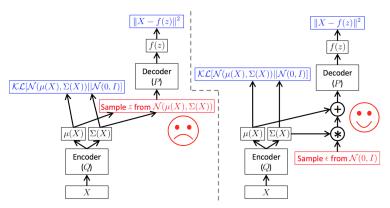
Variational AE

t-SNE

GAN

Cannot backprop error signal through random samples

• Reparameterization trick emulates $z \sim \mathcal{N}(\mu, \sigma)$ with $\epsilon \sim \mathcal{N}(0, 1), z = \epsilon \sigma + \mu$



Example Generated Images: Random

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

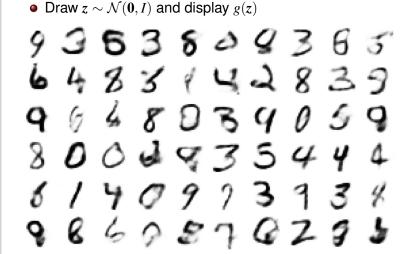
Denoising AE

Sparse AE

Contractive AF

Variational AE

t-SNE GAN





Example Generated Images: Manifold

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AF

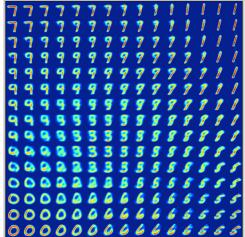
Variational AE

variational 7tL

t-SNE

GAN

 Uniformly sample points in (2-dimensional) z space and decode







Variational Autoencoders 2D Cluster Analysis

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

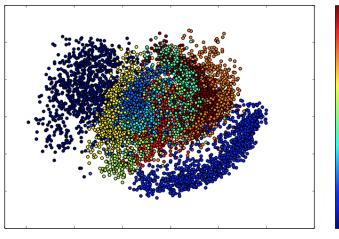
Sparse AE

Contractive

Variational AE

t-SNE GAN

Cluster analysis by digit (2D latent space)





Aside: Visualizing with t-SNE van der Maaten and Hinton (2008)

Lecture 51 Autoencoders

Stephen Scott

Introduction Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE Contractive

Variational AE

t-SNE

GAN

 Visualize high-dimensional data, e.g., embedded representations

 Want low-dimensional representation to have similar neighborhoods as high-dimensional one

• Map each high-dimensional x_1, \ldots, x_N to low-dimensional y_1, \ldots, y_N via matching **pairwise** distributions based on distance

 \Rightarrow Probability p_{ij} pair (x_i, x_i) chosen similar to probability q_{ii} pair (y_i, y_i) chosen

• Set $p_{ij} = (p_{i|i} + p_{i|j})/(2N)$ where

$$p_{j|i} = \frac{\exp\left(-\|\boldsymbol{x}_i - \boldsymbol{x}_j\|^2/(2\sigma_i^2)\right)}{\sum_{k \neq i} \exp\left(-\|\boldsymbol{x}_i - \boldsymbol{x}_k\|^2/(2\sigma_i^2)\right)}$$

and σ_i chosen to control density of the distribution

• I.e., $p_{i|i}$ is probability of x_i choosing x_i as its neighbor if chosen in proportion of Gaussian density centered at x_i

Aside: Visualizing with t-SNE (2) van der Maaten and Hinton (2008)

CSCE 496/896 Lecture 5:

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

Contractive AF

Variational AE

t-SNE

GAN

• Also, define *q* via student's *t* distribution:

$$q_{ij} = \frac{\left(1 + \|\mathbf{y}_i - \mathbf{y}_j\|^2\right)^{-1}}{\sum_{k \neq \ell} \left(1 + \|\mathbf{y}_k - \mathbf{y}_\ell\|^2\right)^{-1}}$$

- Using student's t instead of Gaussian helps address crowding problem where distant clusters in x space squeeze together in y space
- Now choose y values to match distributions p and q via
 Kullback-Leibler divergence:

$$\sum_{i \neq i} p_{ij} \log \frac{p_{ij}}{q_{ij}}$$



Generative Adversarial Network

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction
Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

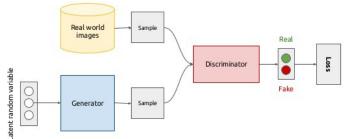
Contractive AE

Variational AE t-SNF

GAN

GANs are also generative models, like VAEs

- Models a game between two players
 - Generator creates samples intended to come from training distribution
 - Discriminator attempts to discern the "real" (original training) samples from the "fake" (generated) ones
- Discriminator trains as a binary classifier, generator trains to fool the discriminator





Generative Adversarial Network How the Game Works

496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction
Basic Idea

Stacked AE

Transpaged

Transposed Convolutions

Denoising AE Sparse AE

Contractive AF

Variational AE

t-SNE

- Let D(x) be discriminator parameterized by $\theta^{(D)}$
 - Goal: Find $\theta^{(D)}$ minimizing $J^{(D)}$ $(\theta^{(D)}, \theta^{(G)})$
- Let G(z) be generator parameterized by $\theta^{(G)}$
 - Goal: Find $\theta^{(G)}$ minimizing $J^{(G)}\left(\theta^{(D)},\theta^{(G)}\right)$
- A Nash equilibrium of this game is $(\theta^{(D)}, \theta^{(G)})$ such that each $\theta^{(i)}$, $i \in \{D, G\}$ yields a local minimum of its corresponding J



Generative Adversarial Network Training

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE Sparse AE

Contractive

Variational AE

t-SNE

- Each training step:
 - Draw a minibatch of x values from dataset
 - Draw a minibatch of z values from prior (e.g., $\mathcal{N}(\mathbf{0}, I)$)
 - Simultaneously update $\theta^{(G)}$ to reduce $J^{(G)}$ and $\theta^{(D)}$ to reduce $J^{(D)}$, via, e.g., Adam
- ullet For $J^{(D)}$, common to use cross-entropy where label is 1 for real and 0 for fake
- Since generator wants to trick discriminator, can use $J^{(G)} = -J^{(D)}$
 - Others exist that are generally better in practice, e.g., based on ML



Generative Adversarial Network DCGAN: Radford et al. (2015)

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea Stacked AE

Transposed

Convolutions

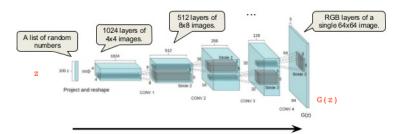
Denoising AE Sparse AE

Contractive AF

Variational AE

t-SNF

- "Deep, convolution GAN"
- Generator uses transposed convolutions (e.g., tf.layers.conv2d_transpose) without pooling to upsample images for input to discriminator





Generative Adversarial Network

DCGAN Generated Images: Bedrooms

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AE

Variational AE

t-SNE

GAN

Trained from LSUN dataset, sampled *z* space





Generative Adversarial Network DCGAN Generated Images: Adele Facial Expressions

Trained from frame grabs of interview, sampled z space

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction
Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AE

Variational AE

t-SNE





Generative Adversarial Network

DCGAN Generated Images: Latent Space Arithmetic

CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Transposed Convolutions

Denoising AE

Sparse AE

Contractive AE

Variational AE

t-SNE

GAN

Performed semantic arithmetic in *z* space!











(Non-center images have noise added in z space; center is noise-free)