Nebraska Basic Idea

CSCE 496/896 Lecture 5: **Autoencoders**

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(Adapted from Eleanor Quint and Ian Goodfellow)

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Introduction

Basic Idea

Denoising AE parse AE

-SNE

input to its output Applications:

• Unlabeled pre-training for semi-supervised learning

Autoencoding is training a network to replicate its

- Learning embeddings to support information retrieval
- Generation of new instances similar to those in the training set
- Data compression

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-SNE

Outline

Introduction

Stacked AE

Sparse AE

GAN

Basic idea

- Stacking
- Types of autoencoders
 - Denoising
 - Sparse
 - Contractive
 - Variational
 - Generative adversarial networks

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Basic Idea



Hidden Output Input Values 10000000 10000000 .04 01000000 01000000 00100000 .15 .01 .99 .99 .97 .27 00100000 00010000 .99 .97 00010000 .03 .05 .02 00001000 00001000 00000100 .01 .11 .88 00000100 00000010 00000010 .80 .01 98 00000001 .60 .94 .01 00000001

- Sigmoid activation functions, 5000 training epochs, square loss, no regularization
- What's special about the hidden layer outputs?



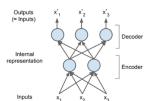
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Basic Idea

Basic Idea enoising AE

-SNE

• An autoencoder is a network trained to learn the identity function: output = input



 Subnetwork called $\mathbf{encoder}\, f(\cdot) \text{ maps input}$ to an **embedded** representation

40 × 40 × 40 × 40 × 00 × 00 00

Subnetwork called **decoder** $g(\cdot)$ maps back to input space

- Can be thought of as lossy compression of input
- Need to identify the important attributes of inputs to reproduce faithfully

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GAN

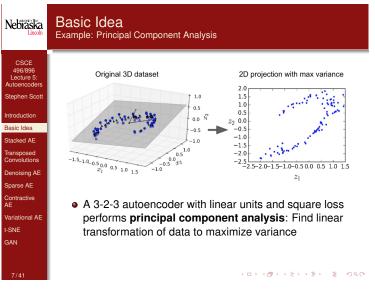
Basic Idea

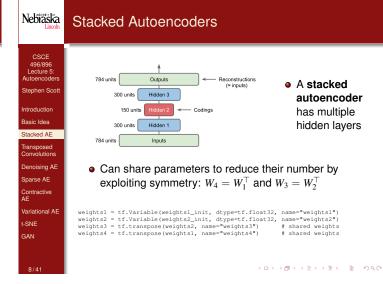
Basic Idea ransposed Convolutions enoising AE

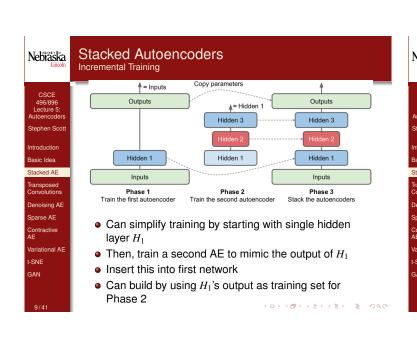
arse AE

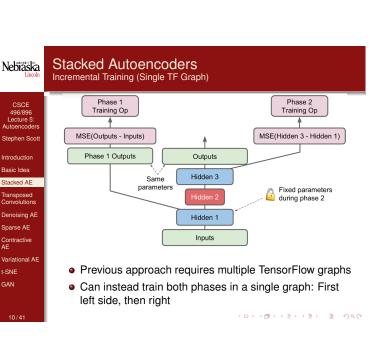
-SNE

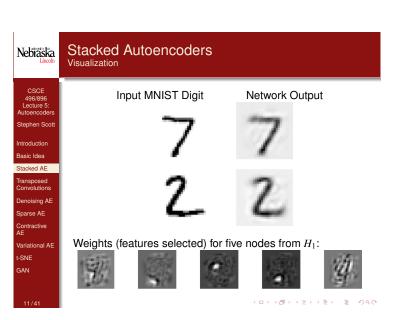
- General types of autoencoders based on size of hidden layer
 - Undercomplete autoencoders have hidden layer size smaller than input layer size
 - ⇒ Dimension of embedded space lower than that of input
 - ⇒ Cannot simply memorize training instances
 - Overcomplete autoencoders have much larger hidden layer sizes
 - ⇒ Regularize to avoid overfitting, e.g., enforce a sparsity constraint

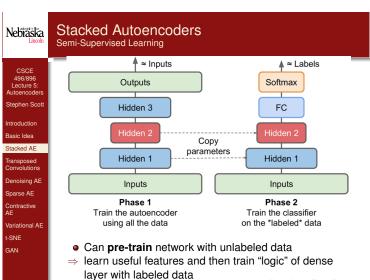


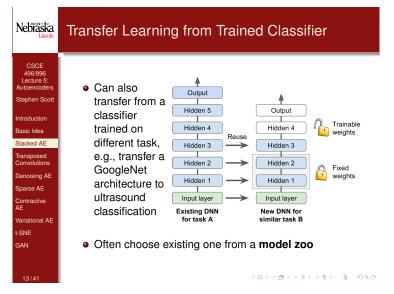


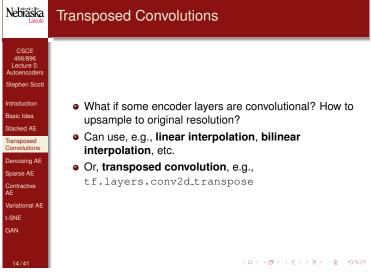


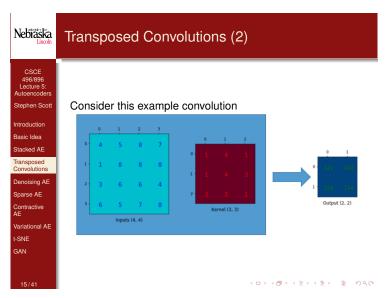


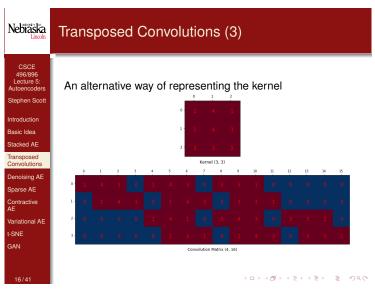


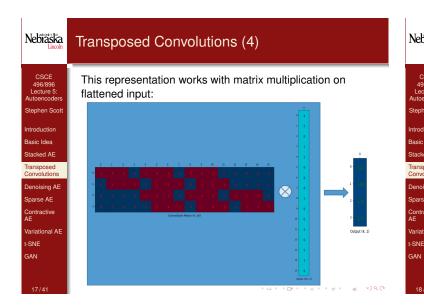


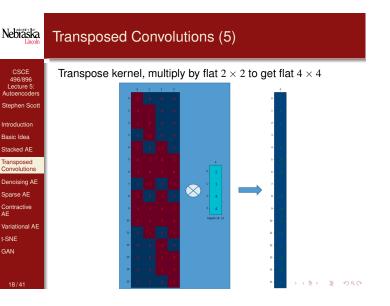












Denoising Autoencoders Vincent et al. (2010)

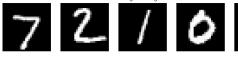
 Can train an autoencoder to learn to denoise input by giving input **corrupted** instance \tilde{x} and targeting uncorrupted instance x

- Example noise models:
 - Gaussian noise: $\tilde{x} = x + z$, where $z \sim \mathcal{N}(\mathbf{0}, \sigma^2 I)$
 - Masking noise: zero out some fraction ν of components of x
 - Salt-and-pepper noise: choose some fraction ν of components of x and set each to its min or max value (equally likely)

Nebraska **Denoising Autoencoders** ♠ ≈ Inputs **↑** ≈ Inputs Outputs Outputs Hidden 3 Hidden 3 Hidden 1 Hidden 1 + **Gaussian Noise Dropout** Inputs Inputs



Denoising Autoencoders Example

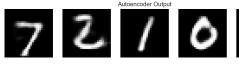


















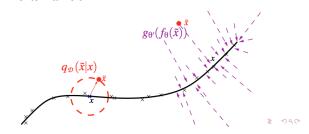


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Denoising Autoencoders

How does it work?

- Even though, e.g., MNIST data are in a 784-dimensional space, they lie on a low-dimensional manifold that captures their most important features
- Corruption process moves instance x off of manifold
- Encoder f_{θ} and decoder $g_{\theta'}$ are trained to project \tilde{x} back onto manifold



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Sparse Autoencoders

-SNE

An overcomplete architecture

Regularize outputs of hidden layer to enforce sparsity:

$$\tilde{\mathcal{J}}(\mathbf{x}) = \mathcal{J}(\mathbf{x}, g(f(\mathbf{x}))) + \alpha \Omega(\mathbf{h})$$
,

where \mathcal{J} is loss function, f is encoder, g is decoder, ${\pmb h}=f({\pmb x}),$ and Ω penalizes non-sparsity of ${\pmb h}$

- E.g., can use $\Omega(\mathbf{h}) = \sum_i |h_i|$ and ReLU activation to force many zero outputs in hidden layer
- Can also measure average activation of h_i across mini-batch and compare it to user-specified target **sparsity** value p (e.g., 0.1) via square error or Kullback-Leibler divergence:

$$p\log\frac{p}{q}+(1-p)\log\frac{1-p}{1-q}\ ,$$

where q is average activation of h_i over mini-batch

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Contractive Autoencoders

-SNE

Similar to sparse autoencoder, but use

$$\Omega(\boldsymbol{h}) = \sum_{j=1}^{m} \sum_{i=1}^{n} \left(\frac{\partial h_i}{\partial x_j} \right)^2$$

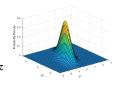
- I.e., penalize large partial derivatives of encoder outputs wrt input values
- This contracts the output space by mapping input points in a neighborhood near x to a smaller output neighborhood near f(x)
 - ⇒ Resists perturbations of input x
- If h has sigmoid activation, encoding near binary and a CE pushes embeddings to corners of a hypercube

Variational Autoencoders

Basic Idea

• VAE is an autoencoder that is also generative model

- ⇒ Can generate new instances according to a probability distribution
- . E.g., hidden Markov models, Bayesian networks
- Contrast with discriminative models, which predict classifications
- Encoder f outputs $[\mu, \sigma]^{\top}$
 - Pair (μ_i, σ_i) parameterizes Gaussian distribution for dimension $i = 1, \ldots, n$
 - Draw $z_i \sim \mathcal{N}(\mu_i, \sigma_i)$
 - Decode this latent variable z to get g(z)



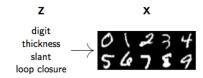
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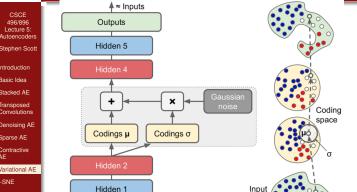
Variational Autoencoders Latent Variables

• Independence of z dimensions makes it easy to generate instances wrt complex distributions via decoder g

- Latent variables can be thought of as values of attributes describing inputs
 - E.g., for MNIST, latent variables might represent "thickness", "slant", "loop closure"



Nebraska Variational Autoencoders Architecture **≜** ≈ Inputs



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Variational Autoencoders Optimization

Stacked AF

Variational AE

 Maximum likelihood (ML) approach for training generative models: find a model (θ) with maximum probability of generating the training set ${\mathcal X}$

- Achieve this by minimizing the sum of:
 - End-to-end AE loss (e.g., square, cross-entropy)
 - Regularizer measuring distance (K-L divergence) from latent distribution $q(z \mid x)$ and $\mathcal{N}(\mathbf{0}, I)$ (= standard multivariate Gaussian)
- $\mathcal{N}(\mathbf{0}, I)$ also considered the **prior distribution** over z (= distribution when no x is known)

eps = 1e-10 latent_loss = 0.5 * tf.reduce_sum(tf.square(hidden3_sigma) + tf.square(hidden3_mean)
- 1 - tf.log(eps + tf.square(hidden3_sigma))) 4 D > 4 AP > 4 B > 4 B > 9 Q A

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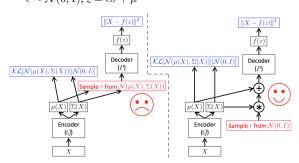
GAN

Variational Autoencoders Reparameterization Trick

Inputs

Basic Idea

- Cannot backprop error signal through random samples
- Reparameterization trick emulates $z \sim \mathcal{N}(\mu, \sigma)$ with $\epsilon \sim \mathcal{N}(0,1), z = \epsilon \sigma + \mu$



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Variational Autoencoders

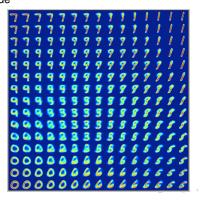
• Draw $z \sim \mathcal{N}(\mathbf{0}, I)$ and display g(z)

Example Generated Images: Random

-SNE

Variational Autoencoders Example Generated Images: Manifold

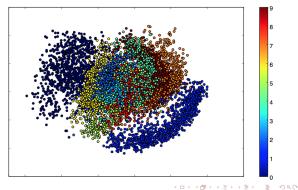
 Uniformly sample points in (2-dimensional) z space and decode



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Variational Autoencoders 2D Cluster Analysis

Cluster analysis by digit (2D latent space)



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Aside: Visualizing with t-SNE van der Maaten and Hinton (2008)

- Visualize high-dimensional data, e.g., embedded representations
- Want low-dimensional representation to have similar neighborhoods as high-dimensional one
- Map each high-dimensional x_1, \ldots, x_N to low-dimensional y_1,\ldots,y_N via matching **pairwise** distributions based on distance
 - \Rightarrow Probability p_{ij} pair $(\mathbf{x}_i, \mathbf{x}_j)$ chosen similar to probability q_{ij} pair (y_i, y_i) chosen
- Set $p_{ij} = (p_{i|i} + p_{i|j})/(2N)$ where

$$p_{j|i} = \frac{\exp\left(-\|\boldsymbol{x}_i - \boldsymbol{x}_j\|^2/(2\sigma_i^2)\right)}{\sum_{k \neq i} \exp\left(-\|\boldsymbol{x}_i - \boldsymbol{x}_k\|^2/(2\sigma_i^2)\right)}$$

and σ_i chosen to control density of the distribution

• I.e., $p_{i|i}$ is probability of x_i choosing x_i as its neighbor if chosen in proportion of Gaussian density centered at x_i

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Aside: Visualizing with t-SNE (2) van der Maaten and Hinton (2008)

arse AE

Also, define q via student's t distribution:

 $q_{ij} = \frac{\left(1 + \|\mathbf{y}_i - \mathbf{y}_j\|^2\right)^{-1}}{\sum_{k \neq \ell} \left(1 + \|\mathbf{y}_k - \mathbf{y}_\ell\|^2\right)^{-1}}$

- Using student's t instead of Gaussian helps address **crowding problem** where distant clusters in x space squeeze together in y space
- Now choose y values to match distributions p and q via Kullback-Leibler divergence:

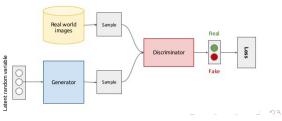
$$\sum_{i\neq j} p_{ij} \log \frac{p_{ij}}{q_{ij}}$$



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Generative Adversarial Network

- GANs are also generative models, like VAEs
- Models a game between two players
 - Generator creates samples intended to come from training distribution
 - Discriminator attempts to discern the "real" (original training) samples from the "fake" (generated) ones
- Discriminator trains as a binary classifier, generator trains to fool the discriminator



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Generative Adversarial Network How the Game Works

• Let
$$D(x)$$
 be discriminator parameterized by $oldsymbol{ heta}^{(D)}$

- Goal: Find $\theta^{(D)}$ minimizing $J^{(D)}$ ($\theta^{(D)}$, $\theta^{(G)}$)
- Let G(z) be generator parameterized by $\theta^{(G)}$
 - Goal: Find $\theta^{(G)}$ minimizing $J^{(G)}(\theta^{(D)}, \theta^{(G)})$
- ullet A **Nash equilibrium** of this game is $(m{ heta}^{(D)}, m{ heta}^{(G)})$ such that each $\theta^{(i)}$, $i \in \{D, G\}$ yields a local minimum of its corresponding J

Generative Adversarial Network

Each training step:

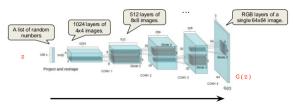
- Draw a minibatch of x values from dataset
- Draw a minibatch of z values from prior (e.g., $\mathcal{N}(\mathbf{0}, I)$)
- Simultaneously update $\theta^{(G)}$ to reduce $J^{(G)}$ and $\theta^{(D)}$ to reduce $J^{(D)}$, via, e.g., Adam
- ullet For $J^{(D)}$, common to use cross-entropy where label is 1 for real and 0 for fake
- Since generator wants to trick discriminator, can use $J^{(G)} = -J^{(D)}$
 - Others exist that are generally better in practice, e.g., based on ML

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Generative Adversarial Network DCGAN: Radford et al. (2015)

"Deep, convolution GAN"

• Generator uses transposed convolutions (e.g., tf.layers.conv2d_transpose) without pooling to upsample images for input to discriminator



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Generative Adversarial Network DCGAN Generated Images: Bedrooms

Trained from LSUN dataset, sampled z space



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Generative Adversarial Network DCGAN Generated Images: Adele Facial Expressions

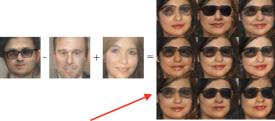
Trained from frame grabs of interview, sampled z space



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Generative Adversarial Network DCGAN Generated Images: Latent Space Arithmetic

Performed semantic arithmetic in z space!



(Non-center images have noise added in z space; center is noise-free)

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