Purpose: This assignment allows you to try your hand on program benchmarking and statistical topics discussed in lecture on September 19. *Remember that in order to measure trends you need to average over several inputs of the same size*. This is an individual assignment (not a team assignment) so you should work independently!

1. Write a program to execute the following function, and estimate its execution time on cse:

$$P_x = \prod_{i=1}^N \left(\frac{x}{x+1}\right) \,,$$

where x is the double-precision floating point equivalent of i.

Using data from several runs, find an expression for the CPU time required to execute this process, as a function of N (I anticipate it will be linear, i.e. t(N) = aN + b).

2. Repeat Problem 1 for the function¹:

$$P_{sqrt} = \prod_{i=1}^{N} \sqrt{\frac{x}{x+1}}$$

3. Use the data from Problems 1 and 2 to estimate the CPU time required to execute one invocation of the square-root function.

4. Write a report on your experiment (in a **single** pdf file), detailing your methodology and your results. Be sure to provide a statistical analysis (with confidence intervals) of your numbers sufficient to give credibility to your results. Include the complete, well-documented code as an attachment to your email.

Grading will be based on:

- 1. The correctness and completeness of your experimental approach and your statistical analyses.
- 2. The quality of your writing, including adherence to the style specification.
- 3. The organization, clarity, and completeness of your report, i.e. how well it "documents, explains, and convinces".
- 4. The readability of your source code.

¹ Both of these functions have simple "closed form" solutions that you can use to verify their correctness.