

CSCE 479/879 Lecture 8: word2vec and node2vec Stephen Scott Introduction word2vec

node2vec

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Stephen Scott

(Adapted from Haluk Dogan)

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Introduction

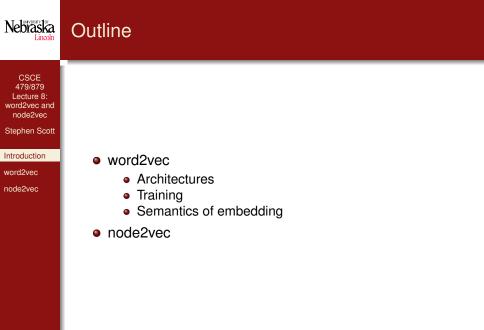
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Introduction

word2vec

- To apply recurrent architectures to text (e.g., NLM), need numeric representation of words
 - The "Embedding lookup" block
- Where does the embedding come from?
 - Could train it along with the rest of the network
 - Or, could use "off-the-shelf" embedding
 - E.g., word2vec or GloVe
- Embeddings not limited to words: E.g., biological sequences, graphs, ...
 - Graphs: node2vec
- The xxxx2vec approach focuses on training embeddings based on context



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Word2vec (Mikolov et al.)

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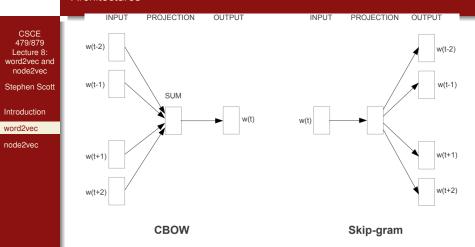
Introduction

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- Training is a variation of autoencoding
- Rather than mapping a word to itself, learn to map between a word and its **context**
 - Context-to-word: Continuous bag-of-words (CBOW)
 - Word-to-context: Skip-gram

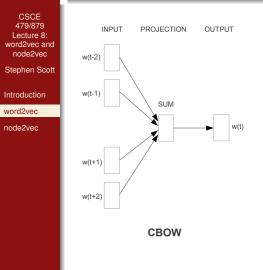
Word2vec (Mikolov et al.)



- CBOW: Predict current word *w*(*t*) based on context
- Skip-gram: Predict context based on w(t)
- One-hot input, hidden linear activation, softmax output

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Word2vec (Mikolov et al.)



- *N* = vocabulary size, *d* = embedding dimension
- *N* × *d* matrix *W* is shared weights from input to hidden
- *d* × *N* matrix *W'* is weights from hidden to output
- When one-hot context vectors x_{t-2}, x_{t-1},..., x_{t+2} input, corresponding rows from W are summed to v̂
- Then get score vector v' and softmax it
- Train with cross-entropy

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Use ith column of W' as embedding



Word2vec (Mikolov et al.) Skip-gram

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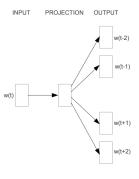
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- Symmetric to CBOW: use *i*th row of W as embedding
- Goal is to maximize $P(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2} \mid w_t)$
- Same as minimizing $-\log P(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2} \mid w_t)$
- Assume words are independent given w_t : $P(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2} | w_t) =$ $\prod_{j \in \{-2, -1, 1, 2\}} P(w_{t+j} | w_t)$



Skip-gram

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Word2vec (Mikolov et al.) _{Skip-gram}

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• Equivalent to maximizing log probability

$$\sum_{j \in \{-c, -(c-1), \dots, (c-1), c\}, j \neq 0} \log P(w_{t+j} \mid w_t)$$

Softmax output and linear activation imply

$$P(w_O \mid w_I) = \frac{\exp\left(\boldsymbol{\nu}_{w_O}^{\prime \top} \boldsymbol{\nu}_{w_I}\right)}{\sum_{i=1}^{N} \exp\left(\boldsymbol{\nu}_i^{\prime \top} \boldsymbol{\nu}_{w_I}\right)}$$

where v_{w_I} is w_I 's (input word) row from W and v'_i is w_i 's (output word) column from W'

 I.e., trying to maximize dot product (similarity) between words in same context

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• Problem: N is big ($\approx 10^5 - 10^7$)

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Word2vec (Mikolov et al.) Skip-gram

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- Speed up evaluation via negative sampling
- Update the weight of each target word and only a small number (5–20) of negative words
- I.e., do not update for all N words
- To estimate $P(w_O \mid w_I)$, use

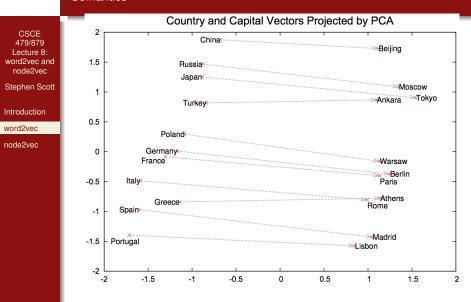
$$\log \sigma \left(\boldsymbol{v}_{w_{O}}^{'\top} \boldsymbol{v}_{w_{I}} \right) + \sum_{i=1}^{k} \mathbb{E}_{w_{i} \sim P_{n}(w)} \left[\log \sigma \left(-\boldsymbol{v}_{w_{i}}^{'\top} \boldsymbol{v}_{w_{I}} \right) \right]$$

• I.e., learn to distinguish target word *w_O* from words drawn from **noise distribution**

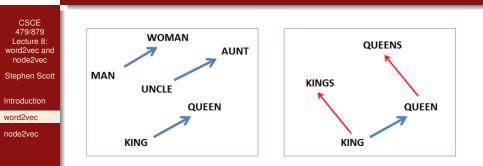
$$P_n(w_i) = \frac{f(w_i)^{3/4}}{\sum_{j=1}^N f(w_j)^{3/4}} ,$$

where f(w_i) is frequency of word w_i in corpus
I.e., P_n(w_i) is a unigram distribution

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Nebraska Lincon Word2vec (Mikolov et al.) Semantics



- Analogies: *a* is to *b* as *c* is to *d*
- Given normalized embeddings x_a, x_b, and x_c, compute
 y = x_b x_a + x_c
- Find *d* maximizing cosine: $\mathbf{x}_d \mathbf{y}^\top / (\|\mathbf{x}_d\| \| \mathbf{y} \|)$

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Node2vec (Grover and Leskovec, 2016)

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- Word2vec's approach generalizes beyond text
- All we need to do is represent the context of an instance to embed together instances with similar contexts
 - E.g., biological sequences, nodes in a graph
- Node2vec defines its context for a node based on its local neighborhood, role in the graph, etc.

Nebraska Lincol Node2vec (Grover and Leskovec, 2016) Notation

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- $\mathcal{G} = (\mathcal{V}, \mathcal{E})$
- $\mathcal{A} \text{ is a } |\mathcal{V}| \times |\mathcal{V}| \text{ adjacency matrix }$
- $f: \mathcal{V} \to \mathbb{R}^d$ is a mapping function from individual nodes to feature representations
 - $|\mathcal{V}| \times d$ matrix
- *N_S(u)* ⊂ *V* denotes a neighborhood of node *u* generated through a neighborhood sampling strategy *S*
- Objective: Preserve local neighborhoods of nodes

Node2vec (Grover and Leskovec, 2016)

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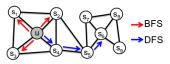
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Organization of nodes is based on:

 Homophily: Nodes that are highly interconnected and cluster together should embed near each other



- Structural roles: Nodes with similar roles in the graph (e.g., hubs) should embed near each other
- *u* and *s*₁ belong to the same community of nodes
- *u* and *s*⁶ in two distinct communities share same structural role of a hub node

Goal

- Embed nodes from the same network community closely together
- Nodes that share similar roles have similar embeddings



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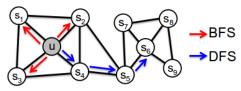
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Key Contribution: Defining a flexible notion of a node's network neighborhood.

- BFS: role of the vertex
 - far apart from each other but share similar kind of vertices
- OFS: community
 - reachability/closeness of the two nodes
 - my friend's friend's friend has a higher chance to belong to the same community as me





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Objective function

 $\max_{f} \sum_{u \in \mathcal{V}} \log P\left(N_{S}(u) \mid f(u)\right)$

Assumptions:

- Conditional independence: $P(N_{S}(u) | f(u)) = \prod_{n_{i} \in N_{S}(u)} P(n_{i} | f(u))$
- Symmetry in feature space: $P(n_i | f(u)) = \frac{\exp(f(n_i) \cdot f(u))}{\sum_{v \in \mathcal{V}} \exp(f(v) \cdot f(u))}$

Objective function simplifies to:

$$\max_{f} \sum_{u \in \mathcal{V}} \left[-\log \mathbf{Z}_{u} + \sum_{n_{i} \in N_{S}(u)} f(n_{i}) \cdot f(u) \right]$$

Node2vec (Grover and Leskovec, 2016) Nebraska Neighborhood Sampling

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Given a source node
$$u$$
, we simulate a random walk of fixed length ℓ :

$$P(c_i = x \mid c_{i-1} = v) = \begin{cases} \frac{\pi_{vx}}{Z} & \text{if } (v, x) \in \mathcal{E} \\ 0 & \text{otherwise} \end{cases}$$

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• $c_0 = u$

- π_{vx} is the unnormalized transition probability
- Z is the normalization constant.
- 2nd order Markovian

Node2vec (Grover and Leskovec, 2016) Neighborhood Sampling

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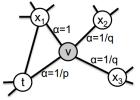
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Search bias α : $\pi_{vx} = \alpha_{pq}(t, x) w_{vx}$ where

$$\alpha_{pq}(t,x) = \begin{cases} \frac{1}{p} & \text{if } d_{tx} = 0\\ 1 & \text{if } d_{tx} = 1\\ \frac{1}{q} & \text{if } d_{tx} = 2 \end{cases}$$



Return parameter p:

- Controls the likelihood of immediately revisiting a node in the walk
- If *p* > max(*q*, 1)
 - less likely to sample an already visited node
 - avoids 2-hop redundancy in sampling
- If $p < \min(q, 1)$
 - backtrack a step
 - keep the walk local

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Node2vec (Grover and Leskovec, 2016) Neighborhood Sampling

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In-out parameter *q*:

- If q > 1 inward exploration
 - Local view
 - BFS behavior
- If q < 1 outward exploration
 - Global view
 - DFS behavior



Node2vec (Grover and Leskovec, 2016) Algorithm

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Algorithm 1 The node2vec algorithm. LearnFeatures (Graph G = (V, E, W), Dimensions d, Walks per node r, Walk lengt h. Context size k, Return p. In-out q) $\pi = PreprocessModifiedWeights(<math>G, p, q$) $G' = (V, E, \pi)$ Initialize walks to Empty for iter = 1 to r do for all nodes $u \in V$ do walk = node2vecWalk(G', u, l) Append walk to walks f = StochasticGradientDescent(k, d, walks) return fnode2vecWalk (Graph $G' = (V, E, \pi)$, Start node u, Length l) Initialize walk to [u]for walk i ter = 1 to l do

- Implicit bias due to choice of the start node u
 - Simulating *r* random walks of fixed length ℓ starting from every node

Phases:

curr = walk[-1] $V_{curr} = \text{GetNeighbors}(curr, G')$ $s = \text{AliasSample}(V_{curr}, \pi)$ Append s to walk return walk

- Preprocessing to compute transition probabilities
- Pandom walks
- Optimization using SGD

Each phase is parallelizable and executed asynchronously