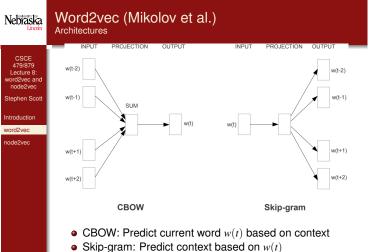


Nebraska

CBOW

INPUT



479/879 Lecture •  $N \times d$  matrix W is shared w(t-2) weights from input to hidden Stephen Sco •  $d \times N$  matrix W' is weights w(t-1) SUM from hidden to output word2vec ode2vec When one-hot context vectors  $x_{t-2}, x_{t-1}, ..., x_{t+2}$ w(t+1) input, corresponding rows from W are summed to  $\hat{v}$ w(t+2 • Then get score vector v' and softmax it CBOW Train with cross-entropy • Use *i*th column of *W*' as embedding

Word2vec (Mikolov et al.)

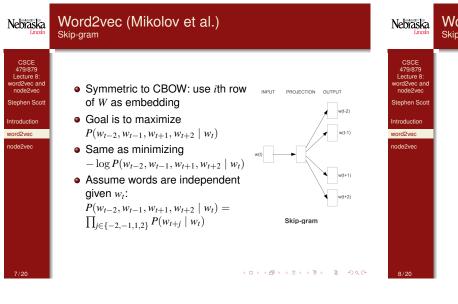
OUTPUT

PROJECTION

- One-hot input, hidden linear activation, softmax output

• N = vocabulary size, d =

embedding dimension



## Word2vec (Mikolov et al.) Skip-gram

Equivalent to maximizing log probability

$$\sum_{j \in \{-c, -(c-1), \dots, (c-1), c\}, j \neq 0} \log P(w_{t+j} \mid w_t)$$

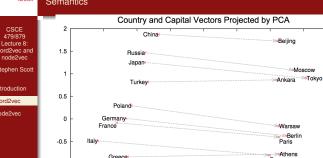
Softmax output and linear activation imply

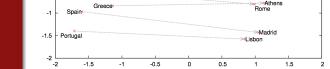
$$P(w_O \mid w_I) = \frac{\exp\left(\boldsymbol{v}_{w_O}^{\prime \top} \boldsymbol{v}_{w_I}\right)}{\sum_{i=1}^{N} \exp\left(\boldsymbol{v}_i^{\prime \top} \boldsymbol{v}_{w_I}\right)}$$

where  $v_{w_i}$  is  $w_i$ 's (input word) row from W and  $v'_i$  is  $w_i$ 's (output word) column from W'

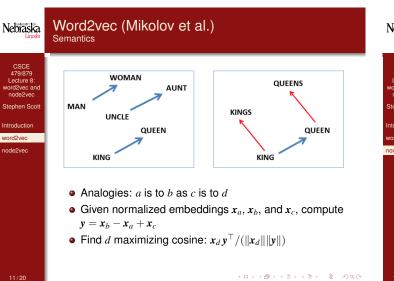
- I.e., trying to maximize dot product (similarity) between words in same context
- **Problem:** N is big ( $\approx 10^5 10^7$ )

Nebraska Lincoln	Word2vec (Mikolov et al.) <sub>Skip-gram</sub>	Nebraska Lincoln	Word2vec (Mikolov et al.) Semantics	
CSCE 479/879 Lecture 8: word2vec and node2vec Stephen Scott Introduction word2vec node2vec	<ul> <li>Speed up evaluation via negative sampling</li> <li>Update the weight of each target word and only a small number (5–20) of negative words</li> <li>I.e., do not update for all N words</li> <li>To estimate P(w<sub>0</sub>   w<sub>I</sub>), use</li> <li>log σ (v<sup>'</sup><sub>w<sub>0</sub></sub>v<sub>w<sub>I</sub></sub>) + ∑<sup>k</sup><sub>i=1</sub> E<sub>w<sub>i</sub>~P<sub>n</sub>(w)</sub> [log σ (-v<sup>'</sup><sub>w<sub>i</sub></sub>v<sub>w<sub>I</sub></sub>)]</li> </ul>	CSCE 479/879 Lecture 8: word2vec and node2vec Stephen Scott Introduction word2vec node2vec	Country and Capital Vector	
	• I.e., learn to distinguish target word $w_0$ from words drawn from <b>noise distribution</b> $P_n(w_i) = \frac{f(w_i)^{3/4}}{\sum_{j=1}^N f(w_j)^{3/4}} ,$ where $f(w_i)$ is frequency of word $w_i$ in corpus • I.e., $P_n(w_i)$ is a <b>unigram distribution</b>		-1 -1 - Spain -1.5 - Portugal -2 -2 -1.5 -1 -0.5 0	
9/20	· · · · · · · · · · · · · · · · · · ·	10/20	<ul> <li>Distances between countries</li> </ul>	

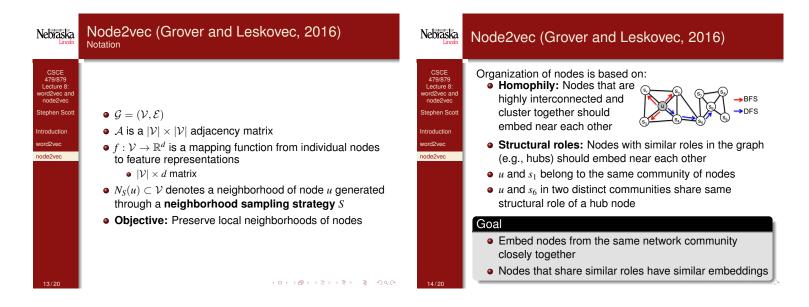


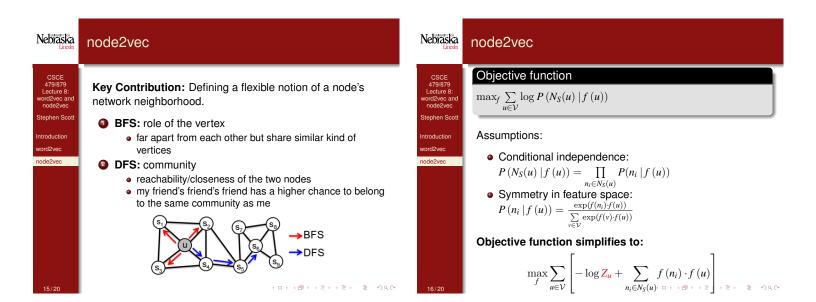


Distances between countries and capitals similar = oscer



Nebraska Lincoln	Node2vec (Grover and Leskovec, 2016)
CSCE 479/879 Lecture 8: word2vec and node2vec Stephen Scott Introduction word2vec node2vec	<ul> <li>Word2vec's approach generalizes beyond text</li> <li>All we need to do is represent the context of an instance to embed together instances with similar contexts <ul> <li>E.g., biological sequences, nodes in a graph</li> </ul> </li> <li>Node2vec defines its context for a node based on its local neighborhood, role in the graph, etc.</li> </ul>







## Node2vec (Grover and Leskovec, 2016) Neighborhood Sampling

Given a source node *u*, we simulate a random walk of fixed length  $\ell$ :

$$P(c_{i} = x \mid c_{i-1} = v) = \begin{cases} \frac{\pi_{vx}}{Z} & \text{if } (v, x) \in \mathcal{E} \\ 0 & \text{otherwise} \end{cases}$$

•  $c_0 = u$ 

P

- $\pi_{vx}$  is the unnormalized transition probability
- Z is the normalization constant.
- 2<sup>nd</sup> order Markovian

Node2vec (Grover and Leskovec, 2016) Nebraska Neighborhood Sampling CSCE 479/879 Lecture 8 Search bias  $\alpha$ :  $\pi_{vx} = \alpha_{pq}(t, x) w_{vx}$  where  $\alpha_{pq}(t,x) = \begin{cases} \frac{1}{p} & \text{if } d_{tx} = 0\\ 1 & \text{if } d_{tx} = 1\\ \frac{1}{a} & \text{if } d_{tx} = 2 \end{cases}$ rd2vec de2vec Return parameter p: Controls the likelihood of immediately revisiting a node in the walk • If  $p > \max(q, 1)$ • less likely to sample an already visited node avoids 2-hop redundancy in sampling • If  $p < \min(q, 1)$  backtrack a step keep the walk local

Nebraska Lincoln	Node2vec (Grover and Leskovec, 2016)	Nebraska Lincoln	Node2vec (Grover and Leskovec, 2016)	
CSCE 479/879 Lecture 8: word2vec and node2vec Stephen Scott Introduction word2vec node2vec	<ul> <li>In-out parameter q:</li> <li>If q &gt; 1 inward exploration <ul> <li>Local view</li> <li>BFS behavior</li> </ul> </li> <li>If q &lt; 1 outward exploration <ul> <li>Global view</li> <li>DFS behavior</li> </ul> </li> </ul>	CSCE 479/876 Lecture 8: word2vec Stephen Scott Introduction word2vec node2vec	Algorithm 1 The node2vec algorithm. LargerTeatures (Graph $G = (V, E, W)$ . Dimensions $d$ . Walks per node $r$ , Walk length $I$ . Constative $k$ . Return $p$ . In-out $q$ ) $\pi$ = PreprocessModifiedWeights( $G$ , $p$ , $q$ ) $G' = (V, E, \pi)$ Initialize walks to Empty for <i>i</i> ( <i>t</i> = 1 to <i>t</i> of for all nodes $u \in V$ (de) u = 1 ( $u = 1$ ( $u = 1$ ) f = u = 0 ( $u = 1$ ( $u = 1$ ) f = u = 0 ( $u = 1$ ) u = 1 ( $u = 1$ ) node2vecWalk (Graph $G' = (V, E, \pi)$ . Start node $u$ . Length 1) Initialize walks $u = 1$ ( $u = 1$ ) u = 0 ( $u = 1$ ( $u = 1$ ) u = 0 ( $u =$	<ul> <li>Implicit bias due to choice of the start node u</li> <li>Simulating r random walks of fixed length ℓ starting from every node</li> </ul>
19/20	<□><♂→<२><२> ३ √२(৮	20/20	<ul> <li>Preprocessing to compute transition probabilities</li> <li>Random walks</li> <li>Optimization using SGD</li> <li>Each phase is parallelizable and executed asynchronously one</li> </ul>	