

CSCE 496/896 Lecture 6: Recurrent Architectures Stephen Scott Introduction Basic Idea I/O Mappings Examples Training Deep RNNs LSTMs GRUs

CSCE 496/896 Lecture 6: Recurrent Architectures

Stephen Scott

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Introduction

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- All our architectures so far work on fixed-sized inputs
- Recurrent neural networks work on sequences of inputs
- E.g., text, biological sequences, video, audio
- Can also try 1D convolutions, but lose long-term relationships in input
- Especially useful for NLP applications: translation, speech-to-text, sentiment analysis
- Can also **create novel output:** e.g., Shakespearean text, music



Outline

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Basic RNNs

Input/Output Mappings

• Example Implementations

Training

Long short-term memory

Gated Recurrent Unit



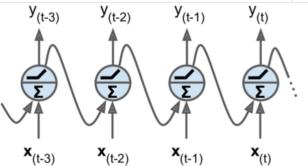
Basic Recurrent Cell

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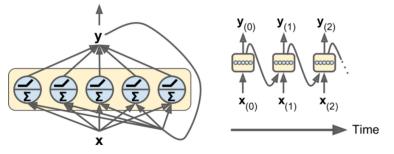
- A recurrent cell (or recurrent neuron) has connections pointing **backward** as well as forward
- At time step (frame) *t*, neuron receives input vector *x*_(t) as usual, but also receives its own output y_(t-1) from previous step





Nebraska Basic Recurrent Layer

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- Can build a layer of recurrent cells, where each node gets both the vector x_(t) and the vector y_(t-1)



Nebraska Basic Recurrent Layer

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- Each node in the recurrent layer has independent weights for both x_(t) and y_(t-1)
- For a single recurrent node, denote by w_x and w_y
- For the entire layer, combine into matrices W_x and W_y
- For activation function \(\phi\) and bias vector \(b\), output vector is

$$\mathbf{y}_{(t)} = \phi \left(W_{\mathbf{x}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{y}}^{\top} \mathbf{y}_{(t-1)} + \mathbf{b} \right)$$

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Memory and State

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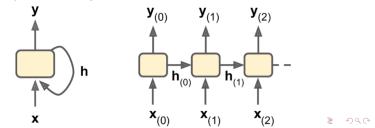
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- Since a node's output depends on its past, it can be thought of having **memory** or **state**
- State at time *t* is $\boldsymbol{h}_{(t)} = f(\boldsymbol{h}_{(t-1)}, \boldsymbol{x}_{(t)})$ and output $\boldsymbol{y}_{(t)} = g(\boldsymbol{h}_{(t-1)}, \boldsymbol{x}_{(t)})$
- State could be the same as the output, or separate
- Can think of *h*_(t) as storing important information about input sequence
- Analogous to convolutional outputs summarizing important image features





Input/Output Mappings Sequence to Sequence

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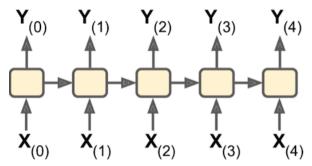
Deep RNNs

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Many ways to employ this basic architecture:

- Sequence to sequence: Input is a sequence and output is a sequence
- E.g., series of stock predictions, one day in advance





Input/Output Mappings Sequence to Vector

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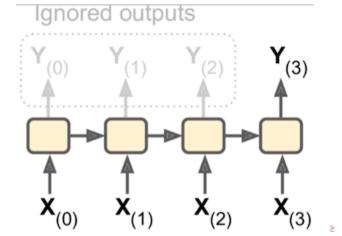
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- Sequence to vector: Input is sequence and output a vector/score/ classification
- E.g., sentiment score of movie review



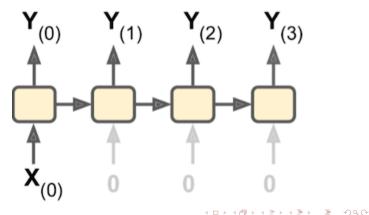


Input/Output Mappings Vector to Sequence

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- Vector to sequence: Input is a single vector (zeroes for other times) and output is a sequence
- E.g., image to caption





Input/Output Mappings Encoder-Decoder Architecture

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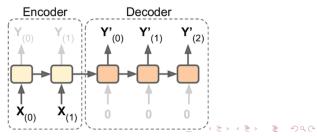
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- Encoder-decoder: Sequence-to-vector (encoder) followed by vector-to-sequence (decoder)
- Input sequence (x_1, \ldots, x_T) yields hidden outputs (h_1, \ldots, h_T) , then mapped to **context vector** $c = f(h_1, \ldots, h_T)$
- Decoder output $y_{t'}$ depends on previously output $(y_1, \ldots, y_{t'-1})$ and c
- Example application: neural machine translation





Input/Output Mappings Encoder-Decoder Architecture: NMT Example

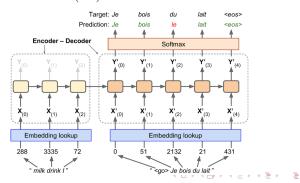
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- Pre-trained word embeddings fed into input
- Encoder maps word sequence to vector, decoder maps to translation via softmax distribution
- After training, do translation by feeding previous translated word y'_(t-1) to decoder





Input/Output Mappings Encoder-Decoder Architecture

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- Works through an embedded space like an autoencoder, so can represent the entire input as an embedded vector prior to decoding
- Issue: Need to ensure that the context vector fed into decoder is sufficiently large in dimension to represent context required
- Can address this representation problem via **attention mechanism** mechanism
 - Encodes input sequence into a vector sequence rather than single vector
 - As it decodes translation, decoder focuses on relevant subset of the vectors



Input/Output Mappings E-D Architecture: Attention Mechanism (Bahdanau et al., 2015)

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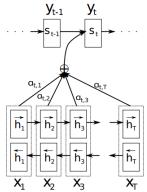
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- Bidirectional RNN reads input forward and backward simultaneously
- Encoder builds **annotation** h_j as concatenation of \overrightarrow{h}_j and \overleftarrow{h}_j
 - ⇒ *h_j* summarizes preceding and following inputs
- ith context vector
 - $m{c}_i = \sum_{j=1}^T lpha_{ij} m{h}_j$, where $lpha_{ij} = rac{\exp(e_{ij})}{\sum_{k=1}^T \exp(e_{ik})}$



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and e_{ij} is an **alignment score** between inputs around *j* and outputs around *i*



Input/Output Mappings E-D Architecture: Attention Mechanism (Bahdanau et al., 2015)

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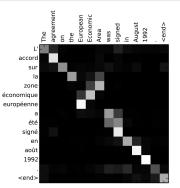
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 The *i*th element of attention vector α_j tells us the probability that target output y_i is aligned to (or translated from) input x_i

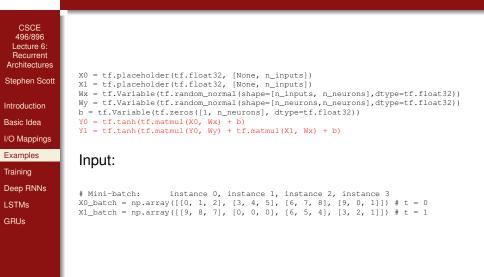
 Then c_i is expected annotation over all annotations with probabilities α_j



- Alignment score *e_{ij}* indicates how much we should focus on word encoding *h_j* when generating output *y_i* (in decoder state *s_{i-1}*)
- Can compute e_{ij} via dot product $h_j^{\top} s_{i-1}$, bilinear function $h_j^{\top} W s_{i-1}$, or nonlinear activation

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Example Implementation Static Unrolling for Two Time Steps



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Example Implementation Static Unrolling for Two Time Steps



LSTMs

GRUs

Can achieve the same thing more compactly via ${\tt static_rnn}\left(\right)$

Automatically unrolls into length-2 sequence RNN

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Example Implementation Automatic Static Unrolling

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Can avoid specifying one placeholder per time step via tf.stack and tf.unstack

- Uses static_rnn() again, but on all time steps folded into a single tensor
- Still forms a large, static graph (possible memory issues)

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Example Implementation Dynamic Unrolling

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Even better: Let TensorFlow unroll dynamically via a while_loop() in dynamic_rnn()

X = tf.placeholder(tf.float32, [None, n_steps, n_inputs])

```
basic_cell = tf.contrib.rnn.BasicRNNCell(num_units=n_neurons)
outputs, states = tf.nn.dynamic_rnn(basic_cell, X, dtype=tf.float32)
```

Can also set swap_memory=True to reduce memory problems

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Example Implementation Variable-Length Sequences

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Training Deep RNNs

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• May need to handle variable-length inputs

- Use 1D tensor sequence_length to set length of each input (and maybe output) sequence
- Pad smaller inputs with zeroes to fit input tensor
- Use "end-of-sequence" symbol at end of each output

```
seg length = tf.placeholder(tf.int32, [None])
. . .
outputs, states = tf.nn.dvnamic rnn(basic cell, X, dtvpe=tf.float32,
                                      sequence_length=seq_length)
X batch = np.array([
   # step 0
            step 1
  [[0, 1, 2], [9, 8, 7]], # instance 0
   [[3, 4, 5], [0, 0, 0]], # instance 1 (padded with a zero vector)
   [[6, 7, 8], [6, 5, 4]], # instance 2
   [[9, 0, 1], [3, 2, 1]], # instance 3
  1)
seq\_length\_batch = np.array([2, 1, 2, 2])
with tf.Session() as sess:
   init.run()
   outputs_val, states_val = sess.run(
       [outputs, states], feed_dict={X: X_batch, seq_length: seq_length_batch})
```

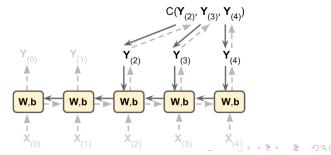
Training Backpropagation Through Time (BPTT)

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- Unroll through time and use BPTT
- Forward pass mini-batch of sequences through unrolled network yields output sequence Y_(t_{min}),..., Y_(t_{max})
- Output sequence evaluated using cost $C(Y_{(t_{\min})}, \dots, Y_{(t_{\max})})$
- Gradients propagated backward through unrolled network (summing over all time steps), and parameters





Training

Issues

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- When comparing two sequences, can use squence loss: tf.contrib.seq2seq.sequence_loss
 - Weighted average of cross entropy across sequence
 - Weights can emphasize parts of target sequence, e.g., more on nouns than articles
- BPTT means that gradient is flowing through longer paths in graph ⇒ exploding or vanishing gradients
 - Can happen with any network, but RNNs very susceptible
 - **Clipping** gradients to range [-1,+1] can mitigate explosions: tf.clip_by_value
 - Batch normalization useful as well



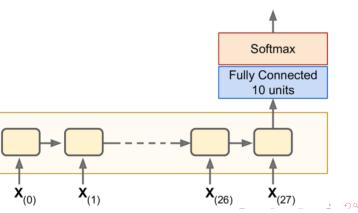
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- Consider MNIST inputs provided as sequence of 28 inputs of 28-dimensional vectors
- Feed in input as usual, then compute loss between target and softmax output after 28th input









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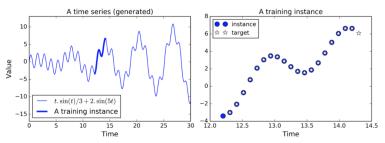
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Training Example: Training on Time Series Data

Input is time series

- Target is same as input, but shifted one into the future
- E.g., stock prices, temperature



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Training Example: Training on Time Series Data

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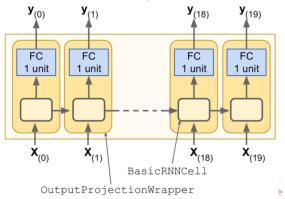
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- Use sequences of length n_steps=20 and n neurons=100 recurrent neurons
- Since output size = 100 > 1 = target size, use OutputProjectionWrapper to feed recurrent layer output into a linear unit to get a scalar

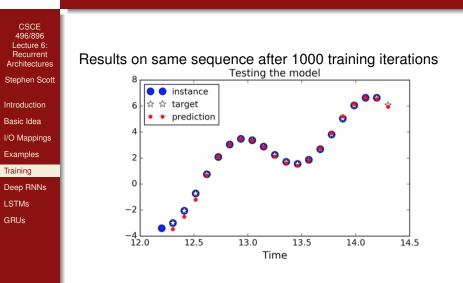




Training Example: Training on Time Series Data

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Introduction Basic Idea I/O Mappings Examples Training Deep RNNs LSTMs GRUs	<pre>n_steps = 20 n_inputs = 1 n_neurons = 100 n_outputs = 1 X = tf.placeholder(tf.float32, [None, n_steps, n_outputs]) y = tf.placeholder(tf.float32, [None, n_steps, n_outputs]) cell = tf.contrib.rnn.OutputProjectionWrapper(</pre>
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Training Example: Creating New Time Series

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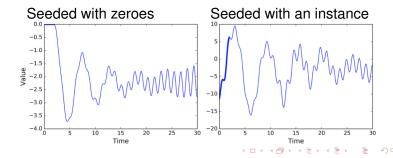
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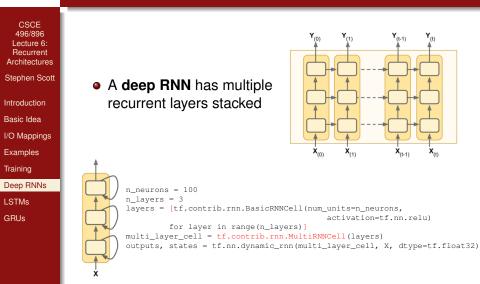
• Feed to trained model **seed sequence** of size n_steps, append predicted value to sequence, feed last n_steps back in to predict next value, etc.

```
sequence = [0.] * n_steps
for iteration in range(300):
    X_batch = np.array(sequence[-n_steps:]).reshape(1, n_steps, 1)
    y_pred = sess.run(outputs, feed_dict={X: X_batch})
    sequence.append(y_pred[0, -1, 0])
```





Deep RNNs





Training over Many Time Steps

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- Vanishing and exploding gradients can be a problem with RNNs, like with other deep networks
 - Can as usual address with, e.g., ReLU, batch normalization, gradient clipping, etc.
- Can still suffer from long training times with long input sequences
 - Truncated backpropagation through time addresses this by limiting n_steps
 - Lose ability to learn long-term patterns
- In general, also have problem of first inputs of sequence have diminishing impact as sequence grows
 - E.g., first few words of long text sequence
- Goal: Introduce long-term memory to RNNs
- Allow a network to accumulate information about the past, but also decide when to forget information

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Long Short-Term Memory Hochreiter and Schmidhuber (1997)

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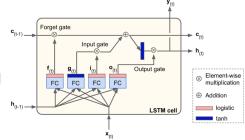
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 At time t, some memories from c_(t-1) are forgotten in the forget gate and new ones (from input gate) added

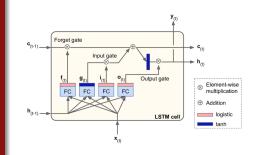


- Result sent out as $c_{(t)}$
- *h*_(t) (and *y*_(t)) comes from processing long-term state in output gate

Long Short-Term Memory Hochreiter and Schmidhuber (1997)



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• $g_{(t)}$ combines input $x_{(t)}$ with state $h_{(t-1)}$

- *f*_(*t*), *i*_(*t*), *o*_(*t*) are gate controllers
- $f_{(t)} \in [0, 1]^n$ controls forgetting of $c_{(t-1)}$
- *i*_(t) controls remembering of *g*_(t)
- **o**_(t) controls what of **c**_(t) goes to output and **h**_(t)
- Output depends on long- and short-term memory
- Network learns what to remember long-term based on $\mathbf{x}_{(t)}$ and $\mathbf{h}_{(t-1)}$

Long Short-Term Memory Hochreiter and Schmidhuber (1997)

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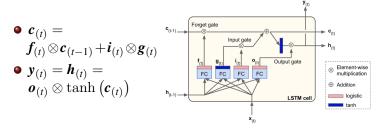
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•
$$\mathbf{i}_{(t)} = \sigma \left(W_{\mathbf{x}\mathbf{i}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{i}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{i}} \right)$$

• $\mathbf{f}_{(t)} = \sigma \left(W_{\mathbf{x}\mathbf{f}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{f}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{f}} \right)$
• $\mathbf{o}_{(t)} = \sigma \left(W_{\mathbf{x}\mathbf{o}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{o}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{o}} \right)$
• $\mathbf{g}_{(t)} = \tanh \left(W_{\mathbf{x}\mathbf{g}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{g}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{g}} \right)$



• Can add **peephole connection:** Let $c_{(t-1)}$ affect $f_{(t)}$ and $i_{(t)}$ and $c_{(t-1)}$ affect $o_{(t)}$



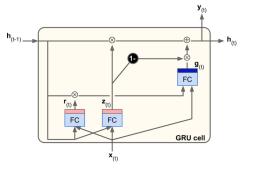
Gated Recurrent Unit

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LSTMs GRUs Simplified LSTM

- Merge $\boldsymbol{c}_{(t)}$ into $\boldsymbol{h}_{(t)}$
- Merge $f_{(t)}$ and $i_{(t)}$ into $z_{(t)}$
 - $z_{(t),i} = 0 \Rightarrow$ forget $h_{(t-1),i}$ and add in $g_{(t),i}$



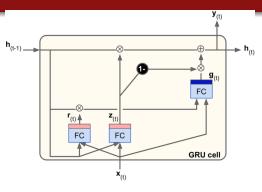
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• $o_{(t)}$ replaced by $r_{(t)} \Rightarrow$ forget part of $h_{(t-1)}$ when computing $g_{(t)}$

gru_cell = tf.contrib.rnn.GRUCell(num_units=n_neurons)

Nebraska Gated Recurrent Unit

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•
$$\mathbf{z}_{(t)} = \sigma \left(W_{\mathbf{x}\mathbf{z}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{z}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{z}} \right)$$

• $\mathbf{r}_{(t)} = \sigma \left(W_{\mathbf{x}\mathbf{r}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{r}}^{\top} \mathbf{h}_{(t-1)} + \mathbf{b}_{\mathbf{r}} \right)$
• $\mathbf{g}_{(t)} = \tanh \left(W_{\mathbf{x}\mathbf{g}}^{\top} \mathbf{x}_{(t)} + W_{\mathbf{h}\mathbf{g}}^{\top} \left(\mathbf{r}_{(t)} \otimes \mathbf{h}_{(t-1)} \right) + \mathbf{b}_{\mathbf{g}} \right)$
• $\mathbf{y}_{(t)} = \mathbf{h}_{(t)} = \mathbf{z}_{(t)} \otimes \mathbf{h}_{(t-1)} + (\mathbf{1} - \mathbf{z}_{(t)}) \otimes \mathbf{g}_{(t)}$