

## Prerequisite Test

August 23, 2004

Due Date: September 3

**No collaboration is allowed, but you may use any resources you wish, so long as you cite them. Show all work and state all assumptions. submit your solutions to all 5 parts (in a single pdf file) via the web-based handin program. If you do not know the definitions to some terms, consult the instructor, TA, or the Mathworld link on the course home page.**

- (10 pts)** Give the equation for a hyperplane (i.e., a 4-dimensional plane in this case) that separates the set of points  $A = \{(0, 0, 0), (1, 1, 0), (0, 2, 1)\}$  from  $B = \{(0, 0, 4), (3, 3, 1), (4, 2, 0), (1, 6, 0)\}$ . Describe how you derived the equation and verify that your hyperplane actually does separate the two sets of points.
- (5 pts)** Given the set of numbers  $A = \{2, 3, 4, 5, 7, 9\}$ , what is its mean? What is its variance?
- (5 pts)** What is the power set of the set  $A = \{a, b, c\}$ ? In general, if a set has  $n$  elements, what is the size of its power set?
- (10 pts)** Let  $\vec{a} = [a_1, \dots, a_n]$  be a vector and

$$B = \{\vec{b}_1, \dots, \vec{b}_m\} = \{[b_{11}, b_{21}, \dots, b_{n1}], [b_{12}, \dots, b_{n2}], \dots, [b_{1m}, \dots, b_{nm}]\}$$

be a set of vectors. Solve

$$\frac{\partial}{\partial a_i} \sum_{\vec{b}_j \in B} (c - \vec{a} \cdot \vec{b}_j)^2,$$

where  $c$  is a constant and  $\vec{a} \cdot \vec{b}_j$  is the dot product of  $\vec{a}$  and  $\vec{b}_j$ . Carefully explain each step of your derivation.

- (20 pts)** Write a brief (2–3 pages) essay on any advanced computer science-related topic that you are familiar with, e.g. virtual memory, Ethernet, NP-completeness or any other topic covered in a 4XX/8XX computer science or applied math class. Assume that the reader of this essay has a basic computer science and math background, but is unfamiliar with the topic that you are writing about. Thus you want to convey the fundamental ideas and applications of this topic, *but do not overwhelm the reader with enormous amounts of detail!* Cite all references you use in a style such as that found in any ACM or IEEE journal. Do *not* simply copy the material from these sources, but instead *write this in your own words*. Only your presentation and writing style will be graded, so have someone proofread this for you before handing it in.