

CSCE 471/871 Lecture 6: Multiple Sequence Alignments

Stephen Scott

Introduction

Scoring

Multidimensiona DP

Progressive Alignments

MA via Profile HMMs

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- Start with a set of sequences
- In each column, residues are homolgous
 - Residues occupy similar positions in 3D structure
 - Residues diverge from a common ancestral residue
 - Figure 6.1
- Can be done manually, but requires expertise and is very tedious
- Often there is no single, unequivocally "correct" alignment
 - Problems from low sequence identity & structural evolution



Outline

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- Scoring a multiple alignment
 - Minimum entropy scoring
 - Sum of pairs (SP) scoring
- Multidimenisonal dynamic programming
 - Standard MDP algorithm
 - MSA
- Progressive alignment methods
 - Feng-Doolittle
 - Profile alignment
 - CLUSTALW
 - Iterative refinement
- Multiple alignment via profile HMMs
 - Multiple alignment with known profile HMM
 - Profile HMM training from unaligned sequences
 - Initial model
 - Baum-Welch
 - Avoiding local maxima
 - Model surgery





Scoring a Multiple Alignment

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Minimum Entropy
Sum of Pairs

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MA via Profile

- Ideally, is based in evolution, as in e.g., PAM and BLOSUM matrices
- Contrasts with pairwise alignments:
 - Position-specific scoring (some positions more conserved than others)
 - Ideally, need to consider entire phylogenetic tree to explain evolution of entire family
- I.e., build complete probabilistic model of evolution
 - Not enough data to parameterize such a model
 ⇒ use approximations
- Assume columns statistically independent:

$$S(m) = G + \sum_{i} S(m_i)$$

 m_i is column i of MA m, G is (affine) score of gaps in m





Scoring a Multiple Alignment Minimum Entropy Scoring

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Scoring Minimum Entropy

Sum of Pairs

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Progressive Alignments

- m_i^j = symbol in column i in sequence j, c_{ia} = observed count of residue a in column i
- Assume sequences are statistically independent, i.e., residues independent within columns
- Then probability of column m_i is $P(m_i) = \prod_a p_{ia}^{c_{ia}}$, where $p_{ia} =$ probability of a in column i



Scoring a Multiple Alignment Minimum Entropy Scoring (2)

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Minimum Entropy

Sum of Pairs

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Progressive Alignments

MA via Profile **HMMs**

• Set score to be $S(m_i) = -\log P(m_i) = -\sum_a c_{ia} \log p_{ia}$

- Propotional to Shannon entropy
- Define optimal alignment as

$$m^* = \underset{m}{\operatorname{argmin}} \left\{ \sum_{m_i \in m} S(m_i) \right\}$$

 Independence assumption valid only if all evolutionary subfamilies are represented equally; otherwise bias skews results

Scoring a Multiple Alignment Sum of Pairs (SP) Scores

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• Treat multiple alignment as $\binom{N}{2}$ pairwise alignments

• If s(a,b) = substitution score from e.g., PAM or BLOSUM:

$$S(m_i) = \sum_{k < \ell} s(m_i^k, m_i^\ell)$$

• Caveat: s(a,b) was derived for pairwise comparisons, not N-way comparisons

$$\overbrace{\log \frac{p_{abc}}{q_a q_b q_c}}^{\text{correct}} \quad \text{Vs.} \quad \overbrace{\log \frac{p_{ab}}{q_a q_b} + \log \frac{p_{bc}}{q_b q_c} + \log \frac{p_{ac}}{q_a q_c} = \log \frac{p_{ab} p_{bc} p_{ac}}{q_a^2 q_b^2 q_c^2} }^{\text{SP}}$$

Scoring a Multiple Alignment SP Problem

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Sum of Pairs

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 Given an alignment with only "L" in column i, using BLOSUM50 yields an SP score of $S_1 = 5\binom{N}{2} = 5N(N-1)/2$

 If one "L" is replaced with "G", then SP score is $S_2 = S_1 - 9(N-1)$

Problem:

$$\frac{S_2}{S_1} = 1 - \frac{9(N-1)}{5N(N-1)/2} = 1 - \frac{18}{5N}$$
,

i.e., as *N* increases, $S_2/S_1 \rightarrow 1$

• But large N should give more support for "L" in m_i relative to S_2 , not less (i.e., should have S_2/S_1 decreasing)



Multidimensional Dynamic Programming

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Algorithm

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MA via Profile HMMs

- Generalization of DP for pairwise alignments
- Assume statistical independence of columns and linear gap penalty (can also handle affine gap penalties)
- $S(m) = \sum_i S(m_i)$, and $\alpha_{i_1,i_2,...,i_N} = \max$ score of alignment of subsequences $x_{1...i_1}^1, x_{1...i_2}^2, \ldots, x_{1...i_N}^N$

$$\alpha_{i_{1},i_{2},...,i_{N}} = \max \left\{ \begin{array}{cccc} \alpha_{i_{1}-1,i_{2}-1,i_{3}-1,...,i_{N}-1} & + & S\left(x_{i_{1}}^{1},x_{i_{2}}^{2},x_{i_{3}}^{3},\ldots,x_{i_{N}}^{N}\right), \\ \alpha_{i_{1},i_{2}-1,i_{3}-1,...,i_{N}-1} & + & S\left(-,x_{i_{2}}^{2},x_{i_{3}}^{3},\ldots,x_{i_{N}}^{N}\right), \\ \alpha_{i_{1}-1,i_{2},i_{3}-1,...,i_{N}-1} & + & S\left(x_{i_{1}}^{1},-,x_{i_{3}}^{3},\ldots,x_{i_{N}}^{N}\right), \\ & \vdots & \\ \alpha_{i_{1}-1,i_{2}-1,i_{3}-1,...,i_{N}} & + & S\left(x_{i_{1}}^{1},x_{i_{2}}^{2},x_{i_{3}}^{3},\ldots,-\right), \\ \alpha_{i_{1},i_{2},i_{3}-1,...,i_{N}-1} & + & S\left(-,-,x_{i_{3}}^{3},\ldots,x_{i_{N}}^{N}\right), \\ \vdots & \vdots & \\ \end{array} \right.$$

In each column, take all gap-residue combinations except 100% gaps



Multidimensional Dynamic Programming (2)

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Multidimensiona DP

Algorithm MSA

Progressive Alignments

MA via Profile

Assume all N sequences are of length L

- Space complexity = $\Theta($
- Time complexity = $\Theta($
- Is it practical?



MSA [Carrillo & Lipman 88; Lipman et al. 89]

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Multidimensiona DP

Algorithm MSA

Progressive Alignments

- Uses MDP, but eliminates many entries from consideration to save time
- Can optimally solve problems with L=300 and N=7 (old numbers), L=150 and N=50, L=500 and N=25, and L=1000 and N=10 (newer numbers)
- Uses SP scoring: $S(a) = \sum_{k < \ell} S(a^{k\ell})$, where a is any MA and $a^{k\ell}$ is PA between x^k and x^ℓ induced by a
- If $\hat{a}^{k\ell}$ is optimal PA between x^k and x^ℓ (easily computed), then $S(a^{k\ell}) \leq S(\hat{a}^{k\ell})$ for all k and ℓ

MSA (2)

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Algorithm

MSA

Progressive MA via Profile

Alignments **HMMs**

• Assume we have lower bound $\sigma(a^*)$ on score of optimal alignment a^* :

$$\sigma(a^*) \leq S(a^*) = \sum_{k < \ell} S(a^{*k\ell})$$

$$= S(a^{*k\ell}) + \sum_{\substack{k' < \ell' \\ (k',\ell') \neq (k,\ell)}} S(a^{*k'\ell'}) \leq S(a^{*k\ell}) + \sum_{\substack{k' < \ell' \\ (k',\ell') \neq (k,\ell)}} S(\hat{a}^{k'\ell'})$$

- Thus $S(a^{*k\ell}) \ge \beta^{k\ell} = \sigma(a^*) \sum_{\substack{k' < \ell' \ (k',\ell') \ne (k,\ell)}} S(\hat{a}^{k'\ell'})$
- When filling in matrix, only need to consider PAs that score at least $\beta^{k\ell}$ (Figure 6.3)
- Can get $\sigma(a^*)$ from other (heuristic) alignment methods



Progressive Alignment Methods

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Progressive Alignments

Feng-Doolittle Profile Alignment CLUSTALW Iterative Refinement

MA via Profile HMMs

- Repeatedly perform pairwise alignments until all sequences are aligned
- Start by aligning the most similar pairs of sequences (most reliable)
 - Often start with a "guide tree"
- Heuristic method (suboptimal), though generally pretty good
- Differences in the methods:
 - Choosing the order to do the alignments
 - Are sequences aligned to alignments or are sequences aligned to sequences and then alignments aligned to alignments?
 - Methods used to score and build alignments

Progressive Alignment Methods Feng-Doolittle

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Feng-Doolittle Profile Alignment CLUSTALW Iterative Refinement

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- Compute a distance matrix by aligning all pairs of sequences
 - Convert each pairwise alignment score to distance:

$$D = -\log \frac{S_{obs} - S_{rand}}{S_{max} - S_{rand}}$$

- S_{obs} = observed alignment score between the two sequences, S_{max} = average score of aligning each of the two sequences to itself, $S_{rand} =$ expected score of aligning two random sequences of same composition and length
- Use a hierarchical clustering algorithm [Fitch & Margoliash 67] to build guide tree based on distance matrix



Progressive Alignment Methods Feng-Doolittle (2)

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Progressive

Alignments
Feng-Doolittle
Profile Alignment
CLUSTALW

- Build multiple alignment in the order that nodes were added to the guide tree in Step 2
 - Goes from most similar to least similar pairs
 - Aligning two sequences is done with DP
 - Aligning sequence x with existing alignment a done by pairwise aligning x to each sequence in a
 - Highest-scoring PA determines how to align x with a
 - Aligning existing alignment a with existing alignment a' is done by pairwise aligning each sequence in a to each sequence in a'
 - ullet Highest-scoring PA determines how to align a with a^\prime
 - After each alignment formed, replace gaps with "X" character that scores 0 with other symbols and gaps
 - "Once a gap, always a gap"
 - Ensures consistency between PAs and corresponding MAs

Progressive Alignment Methods Profile Alignment

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Progressive Alignments Feng-Doolittle

Profile Alignment
CLUSTALW
Iterative Refinement

- Allows for position-specific scoring, e.g.:
 - Penalize gaps more in a non-gap column than in a gap-heavy column
 - Penalize mismatches more in a highly-conserved column than a heterogeneous column
- If gap penalty is linear, can use SP score with s(-,a) = s(a,-) = -g and s(-,-) = 0
- Given two MAs (profiles) a_1 (over x^1, \ldots, x^n) and a_2 (over x^{n+1}, \ldots, x^N), align a_1 with a_2 by not altering the fundamental structure of either
 - Insert gaps into entire columns of a₁ and a₂
 - s(-,-)=0 implies that this doesn't affect score of a_1 or a_2

Progressive Alignment Methods

Profile Alignment (2)

Score:

optimized

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$$\sum_{i} S(m_i) = \sum_{i} \sum_{k,\ell: 1 \le k < \ell \le N} s(m_i^k, m_i^\ell)$$

$$=\sum_{i}\sum_{k_{1},\ell_{1}\in a_{1}}s(m_{i}^{k_{1}},m_{i}^{\ell_{1}})+\sum_{i}\sum_{k_{2},\ell_{2}\in a_{2}}s(m_{i}^{k_{2}},m_{i}^{\ell_{2}})+\sum_{i}\sum_{k\in a_{1},\ell\in a_{2}}s(m_{i}^{k},m_{i}^{\ell})$$

- Only the last term is affected by the alignment procedure, so it's the only one that needs to be
- Thus alignment of profiles is similar to pairwise alignment, solved optimally via DP
- One profile can be single sequence

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Profile Alignment CLUSTALW Iterative Refinement

MA via Profile **HMMs**



Progressive Alignment Methods CLUSTALW

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Progressive Alignments

Profile Alignment CLUSTALW

Iterative Refinement

MA via Profile HMMs Similar to Feng-Doolittle, but tuned to use profile alignment methods

- Compute distance matrix via pairwise DP and convert to distances via Kimura [83]
 - Score with substitution matrix based on expected similarity of final alignment
- Use hierarchical clustering algorithm [Saitou & Nei 87] to build guide tree



Progressive Alignment Methods CLUSTALW (2)

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Progressive Alignments Feng-Doolittle Profile Alignment

Iterative Refinement

- Build multiple alignment in the order that nodes were added to the guide tree in Step 2
 - Use sequence-sequence, sequence-profile, or profile-profile as necessary
 - Weight sequences to compensate for bias in SP scoring
 - Use position-specific gap-open profile penalties; e.g., more likely to allow new gap in hydrophilic regions
 - Adjusts gap penalties to concentrate gaps in a few regions
 - Dynamically adjusts guide tree to defer low-scoring alignments until later



Progressive Alignment Methods

Iterative Refinement Methods [Barton & Sternberg 87]

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Iterative Refinement

- Start with MA, then iteratively remove one sequence (or subset) x at a time and realign to profile of remaining sequences
 - ⇒ will increase score or not change it
- Repeat with other sequences until alignment remains unchanged
- Guaranteed to reach local max if all sequences tried



Progressive Alignment Methods

Iterative Refinement Methods (2)

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Iterative Refinement

- Pairwise align the two most similar sequences
- Sequence-profile align the profile of current MA to most similar sequence; repeat until all sequences aligned
- **3** Remove sequence x^1 and sequence-profile realign it to profile of rest; repeat for x^2, \ldots, x^N
- Repeat above step until convergence



MA via Profile HMMs

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MA via Profile HMMs

- Replace SP scoring with more statistically valid HMM scheme
- But don't we need a multiple alignment to build the profile HMM?
 - Use heuristics to set architecture, Baum-Welch to find parameters



Multiple Alignment with Known Profile HMM

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Progressive Alignments MA via Profile

HMMs HMM Known

- Find most likely (Viterbi) path and line up residues from same match states
- Insert state emissions are not aligned (Figs. 6.4–6.6)
 - OK so long as residues are true insertions (not conserved or meaningfully alignable)
 - Other MA algorithms align <u>entire</u> sequences



Profile HMM Training from Unaligned Sequences

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MA via Profile HMMs

HMM Unknown
Local Maxima
Simulated Annealing
Model Surgery

Used by SAM

- Choose length of model (number of match states) and initialize parameters
- Set parameters via Baum-Welch
 - Use heuristics to avoid local optima
- Check length of model from Step 1 and update if necessary
 - Repeat Step 2 if model length changed
- Align all sequences to final model using Viterbi algorithm and build MA



Profile HMM Training from Unaligned Sequences

Choosing Initial Model

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MA via Profile HMMs

- Architecture completely set once we choose number match states M
- When we started with MA, we applied heuristics to set M
- But we don't have MA!
 - Heuristic: Let M = average sequence length
 - If prior information known, use that instead
- For initial parameters, complexity of B-W search makes us want to start near good local optimum
 - Start with reasonable initial values of parameters (e.g., transitions into match states relatively large):
 - Sample from Dirichlet prior
 - Start with guess of MA



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Baum-Welch: Forward Equations

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DP Progressive

Alignments

MA via Profile

HMMs HMM Known

$$f_{M_0}(0) = 1$$

$$f_{M_k}(i) = e_{M_k}(x_i) \left[f_{M_{k-1}}(i-1) a_{M_{k-1}M_k} + f_{I_{k-1}}(i-1) a_{I_{k-1}M_k} + f_{D_{k-1}}(i-1) a_{D_{k-1}M_k} \right]$$

$$f_{I_k}(i) = e_{I_k}(x_i) \left[f_{M_k}(i-1) a_{M_kI_k} + f_{I_k}(i-1) a_{I_kI_k} + f_{D_k}(i-1) a_{D_kI_k} \right]$$

$$f_{D_k}(i) = f_{M_{k-1}}(i) a_{M_{k-1}D_k} + f_{I_{k-1}}(i) a_{I_{k-1}D_k} + f_{D_{k-1}}(i) a_{D_{k-1}D_k}$$

$$f_{M_{M+1}}(L+1) = f_{M_M}(L) a_{M_MM_{M+1}} + f_{I_M}(L) a_{I_MM_{M+1}} + f_{D_M}(L) a_{D_MM_{M+1}}$$



Profile HMM Training from Unaligned

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Baum-Welch: Backward Equations

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MA via Profile

HMMs HMM Known

$$\begin{split} b_{M_{M+1}}(L+1) &= 1 \; ; \; b_{M_{M}}(L) = a_{M_{M}M_{M+1}} \\ b_{I_{M}}(L) &= a_{I_{M}M_{M+1}} \; ; \; b_{D_{M}}(L) = a_{D_{M}M_{M+1}} \\ b_{M_{k}}(i) &= b_{M_{k+1}}(i+1) \, a_{M_{k}M_{k+1}} \, e_{M_{k+1}}(x_{i+1}) + b_{I_{k}}(i+1) \, a_{M_{k}I_{k}} \, e_{I_{k}}(x_{i+1}) \\ &\quad + b_{D_{k+1}}(i) \, a_{M_{k}D_{k+1}} \\ b_{I_{k}}(i) &= b_{M_{k+1}}(i+1) \, a_{I_{k}M_{k+1}} \, e_{M_{k+1}}(x_{i+1}) + b_{I_{k}}(i+1) \, a_{I_{k}I_{k}} \, e_{I_{k}}(x_{i+1}) \\ &\quad + b_{D_{k+1}}(i) \, a_{I_{k}D_{k+1}} \\ b_{D_{k}}(i) &= b_{M_{k+1}}(i+1) \, a_{D_{k}M_{k+1}} \, e_{M_{k+1}}(x_{i+1}) + b_{I_{k}}(i+1) \, a_{D_{k}I_{k}} \, e_{I_{k}}(x_{i+1}) \\ &\quad + b_{D_{k+1}}(i) \, a_{D_{k}D_{k+1}} \end{split}$$



Profile HMM Training from Unaligned

Sequences

Baum-Welch: Re-estimation Equations

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HMMs HMM Known

$$E_{M_k}(a) = \frac{1}{P(x)} \sum_{i:x_i=a} f_{M_k}(i) b_{M_k}(i)$$

$$E_{I_k}(a) = \frac{1}{P(x)} \sum_{i:x_i=a} f_{I_k}(i) b_{I_k}(i)$$

$$A_{X_k M_{k+1}} = \frac{1}{P(x)} \sum_i f_{X_k}(i) a_{X_k M_{k+1}} e_{M_{k+1}}(x_{i+1}) b_{M_{k+1}}(i+1)$$

$$A_{X_k I_k} = \frac{1}{P(x)} \sum_i f_{X_k}(i) a_{X_k I_k} e_{I_k}(x_{i+1}) b_{I_k}(i+1)$$

$$A_{X_k D_{k+1}} = \frac{1}{P(x)} \sum_i f_{X_k}(i) a_{X_k D_{k+1}} b_{D_{k+1}}(i)$$



Profile HMM Training from Unaligned Sequences Avoiding Local Maxima

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MA via Profile HMMs

HMM Known HMM Unknown

Local Maxima

Simulated Annealing Model Surgery

- B-W will converge to local maximum likelihood model, but how good is that globally?
- Long sequences ⇒ many parameters to optimize ⇒ increased risk of getting stuck in local minimum
- Methods to avoid this:
 - Multiple runs from random start points (sometimes done in training artificial neural networks)
 - Use random pertubations of current solution to nudge it into different parts of the search space, e.g., simulated annealing



Profile HMM Training from Unaligned Sequences Simulated Annealing

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Simulated Annealing Model Surgery Based on annealing process to crystallize compounds

- In optimization, this involves occasionally selecting worse solutions to allow movement to a region of the search space where a better local optimum exists
- Movement is done probabilistically (so optimization can be thought of as a Markov process), and probability of worse choice decreases as optimization progresses
- Probability of a particular solution x is $P(x) = (1/Z) \exp{(-E(x)/T)}; Z = \int \exp{(-E(x)/T)}$ is normalizer, E(x) is energy (objective) function to be minimized, and T is temperature parameter that is reduced based on annealing schedule
- $T \to \infty \Rightarrow P(x) \to \text{uniform}, T \to 0 \Rightarrow P(x) \to \text{peaks at}$ minimum values of E(x)



Profile HMM Training from Unaligned Sequences

Simulated Annealing (2)

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MA via Profile **HMMs** HMM Known HMM Unknown Local Maxima

Simulated Annealing Model Surgery

• For HMM, use as E(x) the negative log of likelihood: $-\log P(X\mid\theta)$, so

$$P(x) = \frac{\exp\left(-\frac{1}{T}\left(-\log P(X\mid\theta)\right)\right)}{Z} = \frac{P(X\mid\theta)^{1/T}}{\int P(X\mid\theta')^{1/T}d\theta'}$$

- To sample from this distribution, can use noise injection or Viterbi estimation
 - Noise injection: Add noise to counts estimated in forward-backward procedure, decreasing noise rate slowly



Profile HMM Training from Unaligned

Sequences

Simulated Annealing (3): Viterbi Estimation

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HMMS
HMM Known
HMM Unknown
Local Maxima

Simulated Annealing Model Surgery Based on Viterbi alternative to B-W, in which emission and transition counts come from most likely paths rather than forward-backward expectation estimates

 In SA approximation, rather than choosing most likely path, choose a path probabilistically:

$$P(\pi) = \frac{P(\pi, x \mid \theta)^{1/T}}{\sum_{\pi'} P(\pi', x \mid \theta)^{1/T}}$$

- Denominator comes from modified forward algorithm with exponentiated parameters
- Use stochastic traceback to return π : For i = L + 1 down to 1,

$$P(\pi_{i-1} \mid \pi_i) = \frac{f_{i-1,\pi_{i-1}} \hat{a}_{\pi_{i-1},\pi_i}}{\sum_{k} f_{i-1,k} \hat{a}_{i,\pi_i}} ,$$

$$\hat{a}_{ij} = a_{ij}^{1/T}$$





Model Surgery

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HMMS
HMM Known
HMM Unknown
Local Maxima
Simulated Annealing

Model Surgery

- B-W should give reasonably good parameters to fit architecture to data
- But was the architecture accurate in the first place?
 - Too few match states ⇒ overuse of insertion states, incorrectly labeling some parts as non-matches
 - Too many match states ⇒ overuse of deletion states
- Model surgery (heuristically) identifies such problems and updates model
 - Use f-b or Viterbi to compute usage of all the model's transitions
 - If a match state M_i is used too infrequently, delete it and collapse the model
 - If an insert state I_j is used too frequently, expand it to a sequence of match states (number = average length of insertions)
- Have to recompute parameters via B-W after surgery!