

CSCE 471/871 Lecture 5: Building Phylogenetic Trees

Stephen Scott

Phylogenetic Trees

Building Trees

Parsimony

Hein's Algorithm

CSCE 471/871 Lecture 5: Building Phylogenetic Trees

Stephen Scott

sscott@cse.unl.edu



Outline

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Parsimony

- Phylogenetic trees
- Building trees from pairwise distances
- Parsimony
- Simultaneous sequence alignment and phylogeny



Phylogenetic Trees

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- Assumption: all organisms on Earth have a common ancestor
 - ⇒ all species are related in some way
- Relationships represented by phyogenetic trees
- Trees can represent relationships between orthologs or paralogs
 - Othorlogs: Genes in different species that evolved from a common ancestral gene by **speciation** (evolution of one species out of another)
 - Normally, orthologs retain the same function in the course of evolution
 - Paralogs: genes related by duplication within a genome
 - In contrast to orthologs, paralogs evolve new functions



Phylogenetic Trees (2)

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Hein's Algorithm We'll use binary trees, both rooted and unrooted

- Rooted for when we know the direction of evolution (i.e., the common ancestor)
- Can sometimes find the root by adding a distantly related organism/sequence to an existing tree (Fig 7.1)



Phylogenetic Trees (3)

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- A weighted tree, where each weight (edge length) is an estimate of evolutionary time between events
 - Based on distance measure (e.g., substitution scoring matrices) between sequences
 - Gives a reasonably accurate approximation of relative evolutionary times, despite the fact that sequences can evolve at different rates
- Number of possible binary trees on n nodes grows exponentially in n
 - E.g., n = 20 has about 2.2×10^{20} trees
 - We'll use hueristics, of course



Building Trees from Pairwise Distances

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LIPGMA

Neighbor Joining

Parsimony

Hein's Algorithm Start with some distance measure between sequences, e.g., Jukes-Cantor:

$$d_{ij} = -0.75 \log(1 - 4f_{ij}/3) ,$$

where f_{ij} is fraction of residues that differ between sequences x_i and x_j when pairwise aligned

UPGMA (unweighted pair group method average) algorithm

- One of a family of hierarchical clustering algorithms
- Basic idea of algorithmic family: Find minimum inter-cluster distance d_{ij} in current distance matrix, merge clusters i and j, then update distance matrix
- Differences among algorithms lie in matrix update
- For phylogenetic trees, also add edge lengths





Building Trees from Pairwise Distances UPGMA (2)

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UPGMA Neighbor Joining

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Hein's Algorithm

- While there are more than two clusters
 - Find minimum d_{ij} in distance matrix
 - 2 Add to the clustering cluster $C_k = C_i \cup C_j$ and delete C_i and C_i
 - **3** For each cluster $C_{\ell} \notin \{C_k, C_i, C_j\}$

$$d_{k\ell} = \frac{1}{|C_k|} \sum_{p \in C_k, q \in C_\ell} d_{pq}$$

[Shortcut: Eq. (7.2)]

- 4 Add to the tree node k with children i and j, with height $d_{ij}/2$
- **1** When only C_i and C_j remain, place root at height $d_{ij}/2$

Example: Fig 7.4





Building Trees from Pairwise Distances UPGMA (3)

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- If the rate of evolution is the same at all points in original (target) phylogenetic tree, then UPGMA will recover the correct tree
 - This occurs iff length of all paths from root to leaves are equal in terms of evolutionary time
- If this is not the case, then UPGMA may find incorrect topology (Fig. 7.5, p. 170)
- Can avoid this if distances satisfy <u>ultrametric</u> condition: for any three sequences x_i, x_j, x_k , the distances d_{ij}, d_{jk}, d_{ik} are either all equal, or two are equal and one is smaller



Building Trees from Pairwise Distances Neighbor Joining

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UPGMA
Neighbor Joining

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Parsimony

Hein's Algorithm If ultrametric property doesn't hold, can still recover original tree if additivity holds

 If, in original tree, distance between any pair of leaves = sum of lengths of edges of path connecting them

If additivity holds, neighbor joining finds the original tree

- First, find a pair of neighboring leaves i and j, assign them parent k, then replace i and j with k, where for all other leaves m, $d_{km} = (d_{im} + d_{im} d_{ii})/2$
- But it does NOT work to simply choose pair (i,j) with minimum d_{ii} (Fig. 7.7)
- Instead, choose (i,j) minimizing $D_{ij} = d_{ij} (r_i + r_j)$, where L is current set of "leaves" and

$$r_i = rac{1}{|L|-2} \sum_{k \in L} d_{ik}$$



Building Trees from Pairwise Distances Neighbor Joining (2)

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Neighbor Joining

Parsimony

- Initialize L = T = set of leaves
- **2** While |L| > 2
 - Choose i and j minimizing D_{ij}
 - ② Define new node k and set $d_{km} = (d_{im} + d_{jm} d_{ij})/2$ for all $m \in L$
 - **3** Add k to T with edges of lengths $d_{ik} = (d_{ij} + r_i r_j)/2$ and $d_{ik} = d_{ii} d_{ik}$
- **3** Add final, length- d_{ij} edge between final nodes i and j

Parsimony

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Parsimony

- Widely used approach for tree building
- Scores tree based on the cost of substitutions going from node to its child
 - ⇒ Will assign hypothetical ancestral sequences to internal nodes, e.g., Figure 7.9
- Generally consists of two components
 - Computing cost of tree T over n aligned sequences
 - Searching through the space of possible trees for min-cost one
- Treat each site independently of the others, so for a length-m alignment, run scoring algorithm on each of the m sites separately
- Let S(a, b) be cost of substituting b for a
- Scoring site (tree) $u \in \{1, ..., m\}$, let $S_k(a)$ be the minimal cost for the assignment of symbol (residue) a to node k

Parsimony (2)

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Hein's Algorithm

- Initialize k = 2n 1 (index of the root node)
 - Recursively compute $S_k(a)$ for all a in the alphabet:
 - If k is a leaf, set $S_k(a) = 0$ for $a = x_u^k$ and $S_k(a) = \infty$ otherwise
 - \Rightarrow a must match uth symbol in sequence
 - 2 Else $S_k(a) = \min_b(S_i(b) + S(a,b)) + \min_b(S_i(b) + S(a,b)),$ where i and j are k's children
- **3** Return $\min_{a} \{S_{2n-1}(a)\}$ as minimum cost of tree

Can recover ancestral residues by tracking where min comes from in recurisve step



Parsimony (3) Searching for a Tree

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- Not practical to enumerate the entire set of possible trees and score them all
- Will use branch and bound to speed it up (though no guarantee of an efficient algorithm)
 - When incrementally building a tree, adding edges will never decrease its cost
 - Thus if a tree's cost already exceeds the final cost of the best tree so far, we can discard it
- Algorithm: systematically grow existing tree by adding edges, stopping expansion if current tree's cost exceeds final cost of best tree so far



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Hein's Algorithm

Finding Sequences to Align with Leaves Building Sequence Graphs Filling in Ancestors Building Topology

For simultaneously finding alignment and phylogeny

- Similar to parsimony in that, given a topology, it infers ancestral sequences
- But this algorithm uses an affine gap penalty model (separate penalties for opening and extending gaps)
- First, it ascends the tree from the leaves, determining the set of sequences that best align with leaf sequences
 - Represents such a set of sequences as a digraph
- Then it works its way up toward the root, at each step inferring the set of sequences that best align with the child graphs
- Finally, it descends from the root to the leaves, fixing the specific ancestral sequences

Finding Set of Sequences that Best Align with Leaves

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Algorithm
Finding Sequences

to Align with Leaves Building Sequence Graphs

Filling in Ancestors Building Topology • GOAL: Given sequences x and y, find set of sequences such that for each such sequence z, S(x,z) + S(z,y) = S(x,y)

- Use DP to handle affine gap penalties
 - $V^M(i,j) = \min \text{ cost aligning } x_{1...i} \text{ to } y_{1...j}; x_i \text{ aligned to } y_j$

$$V^{M}(i,j) = \min\{V^{M}(i-1,j-1), V^{X}(i-1,j-1), V^{Y}(i-1,j-1)\} + S(x_{i},y_{j})\}$$

• $V^X(i,j) = \min \text{ cost aligning } x_{1...i} \text{ to } y_{1...j}; x_i \text{ aligned to gap}$

$$V^{X}(i,j) = \min\{V^{M}(i-1,j) + d, V^{X}(i-1,j) + e\}$$

• $V^{Y}(i,j) = \min \text{ cost aligning } x_{1...i} \text{ to } y_{1...j}; y_{j} \text{ aligned to gap}$

$$V^{Y}(i,j) = \min\{V^{M}(i,j-1) + d, V^{Y}(i,j-1) + e\}$$

Finding Set of Sequences that Best Align with Leaves (2)

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Finding Sequences to Align with Leaves

Building Sequence Graphs Filling in Ancestors Building Topology

- Dynamic programming example in Fig. 7.13
 - j indexes rows, i indexes columns; seq. x is bottom/horizontal
 - E.g., row j = 0, X entries are costs of opening + extending gaps aligned against x
- Result is a set of paths through the DP table, each corresponding to an optimal alignment between x and y:

• Each alignment implies a set of valid ancestral sequences, where each such sequence z satisfies S(x, z) + S(z, y) = S(x, y)

Finding Set of Sequences that Best Align with Leaves (3)

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Finding Sequences to Align with Leaves

Building Sequence Graphs

Graphs
Filling in Ancestors
Building Topology

- Each alignment implies a set of valid ancestral sequences, where each such sequence z satisfies S(x, z) + S(z, y) = S(x, y)
 - If one position is a match between x_i and y_j , then a valid ancestral sequence z contains either x_i or y_j in that position
 - If a gap is involved, can take the gap or the residue
 - But since cost function is not linear, need to either take the entire gap or none of the gap
 - E.g., in Fig. 7.13, with leaves y = CAC and x = CTCACA, can use as ancestral sequence z = CTC, CAC, CACACA, etc., but not CACAC (why?)



Finding Set of Sequences that Best Align with Leaves (3)

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Building Sequence Graphs Filling in Ancestors Building Topology

- Can represent set of sequences as a digraph (e.g., Fig. 7.14(a); edges directed to the right), aka a sequence graph, where each path through the graph corresponds to a valid ancestral sequence
- Null ("dummy") edges (denoted by δ) allow gaps to be entirely skipped



Building Sequence Graphs for Higher-Level Nodes

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Building Sequence Graphs

Filling in Ancestors Building Topology

- Now want to ascend the tree towards the root, building ancestral sequence graphs for internal nodes
- But SG construction previously described ran DP on individual sequences!
- Turns out we can also run DP on SGs
 - In DP equations, "i 1" means the set of previous nodes in the horizontal graph, "j 1" in the vertical graph
 - Now take minimum over entire set of previous nodes that have values defined (non-"-")
 - Scoring function S now defined on sets; it's 0 iff its set-type arguments have non-empty intersection
 - $\bullet \ \, \mathsf{E.g.}, \mathit{S}(\{\mathsf{A}\}, \{\mathsf{A}\!,\!\mathsf{T}\}) = 0 \ \mathsf{due} \ \mathsf{to} \ \mathsf{overlap}$
- Once DP completed, do another traceback and build new SG
 - When labeling edges in new SG, use the intersection of the labels in the two defining edges, or the union if the intersection is empty

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Hein's Algorithm Filling in Ancestral Sequences

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Filling in Ancestors

Building Topology

- Now choose a path in the root's SG, then go to child nodes and trace their SGs with its parent's ancestral sequence, choosing compatible symbols
- In final multiple alignment, need to fill in gaps



Hein's Algorithm **Building the Topology**

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Finding Sequences to Align with Leaves

Building Sequence Filling in Ancestors

Building Topology

- Still need to build the tree to align sequences to
- Hein's tree-building algorithm:
 - Compute an informative subset of the inter-sequence distances
 - Build a "distance tree" by adding sequences to it one by one
 - Perform rearrangements on the tree to improve its fit to the distance data
 - Align sequences to the tree (what we already covered)

Building the Topology (2): Computing Subset of Distances

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Graphs

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 Assume that the distance measure and sequences form a metric space, implying:

- $d(s_1, s_2) = 0 \Leftrightarrow s_1 = s_2$
- $d(s_1, s_2) = d(s_2, s_1)$
- $d(s_1, s) + d(s, s_2) \ge d(s_1, s_2)$
- Can use third eq. to upper- and lower-bound unknown distances
- I.e., if differences between upper and lower bounds is smaller than a paremeter, do not compute the exact value

Building the Topology (3): Computing Distance Tree

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Algorithm Finding Sequences to Align with Leaves **Building Sequence**

Filling in Ancestors **Building Topology**

- Add sequences one at a time
- Choose to add to T_{k-1} the sequence s_k minimizing

$$d(s_k, T_{k-1}) = \min_{s_j \in leaves(T_{k-1})} \{d(s_k, s_j)\}$$



Building the Topology (4): Computing Distance Tree (cont'd)

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to Align with Leaves Building Sequence Graphs

Filling in Ancestors Building Topology Choose s_k 's attachment point as follows:

- Let s_1 be sequence in tree most similar to s_k
- Let A be internal node closest to s_1 , and $S = \{t_1, t_2, t_3\}$ be the set of subtrees leaving A
- For each $t_i, t_j \in S$, compute $d(t_i, s_k)$ and $d(t_i, t_j)$ by computing average distance among pairs of leaves

Building the Topology (5): Computing Distance Tree (cont'd)

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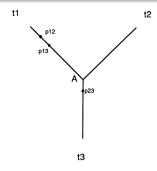
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Building Sequence

Graphs Filling in Ancestors

Filling in Ancestors Building Topology



Hypothetically, if we attached s_k on the path from t_i to t_j , then to preserve additivity, we'd place it at point p_{ij} such that

$$d(t_i, p_{ij}) = (d(t_i, s_k) + d(t_i, t_j) - d(t_i, s_k))/2$$

(I.e., if s_k is at p_{ij} , then $d(t_i, t_i) = d(t_i, s_k) + d(t_i, s_k)$)



Building the Topology (6): Computing Distance Tree (cont'd)

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Building Sequence Graphs Filling in Ancestors

Building Topology

- Now let v₁ = avg distance in direction of t₁ of p₁₂ and p₁₃ from A; similarly define v₂ and v₃
- Maximum of these 3 distances determines attachment point
 - (Intuition: If t_i far from A and near s_k , this is s_k 's home)
- If the max v_i takes us past the root of t_i , then t_i 's root becomes A and the process repeats
- Once all nodes added, look at interchanging neighbors in tree to improve score