

CSCE  
496/896

Lecture 5:  
Autoencoders

Stephen Scott

Introduction

Basic Idea

Stacked AE

Denoising AE

Sparse AE

Contractive  
AE

Variational AE

GAN

# CSCE 496/896 Lecture 5: Autoencoders

Stephen Scott

(Adapted from Paul Quint and Ian Goodfellow)

[sscott@cse.unl.edu](mailto:sscott@cse.unl.edu)

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- **Autoencoding** is training a network to replicate its input to its output
- Applications:
  - Unlabeled pre-training for semi-supervised learning
  - Learning **embeddings** to support information retrieval
  - Generation of new instances similar to those in the training set
  - Data compression

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- Basic idea
- Stacking
- Types of autoencoders
  - Denoising
  - Sparse
  - Contractive
  - Variational
  - Generative adversarial networks

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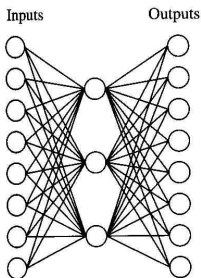
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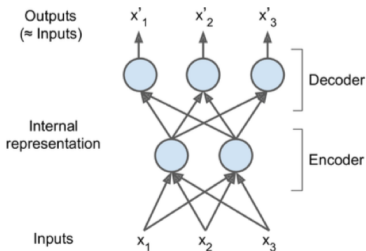
GAN



Input		Hidden Values				Output
10000000	→	.89	.04	.08	→	10000000
01000000	→	.15	.99	.99	→	01000000
00100000	→	.01	.97	.27	→	00100000
00010000	→	.99	.97	.71	→	00010000
00001000	→	.03	.05	.02	→	00001000
00000100	→	.01	.11	.88	→	00000100
00000010	→	.80	.01	.98	→	00000010
00000001	→	.60	.94	.01	→	00000001

- Sigmoid activation functions, 5000 training epochs, square loss, no regularization
- What's special about the hidden layer outputs?

- An **autoencoder** is a network trained to learn the **identity function**: output = input



- Subnetwork called **encoder**  $f(\cdot)$  maps input to an **embedded representation**
  - Subnetwork called **decoder**  $g(\cdot)$  maps back to input space
- Can be thought of as **lossy compression** of input
  - Need to identify the important attributes of inputs to reproduce faithfully

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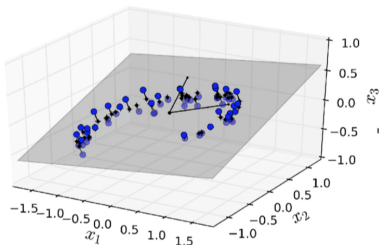
GAN

- General types of autoencoders based on size of hidden layer
  - **Undercomplete** autoencoders have hidden layer size smaller than input layer size
    - ⇒ Dimension of embedded space lower than that of input space
    - ⇒ Cannot simply memorize training instances
  - **Overcomplete** autoencoders have much larger hidden layer sizes
    - ⇒ Regularize to avoid overfitting, e.g., enforce a **sparsity** constraint

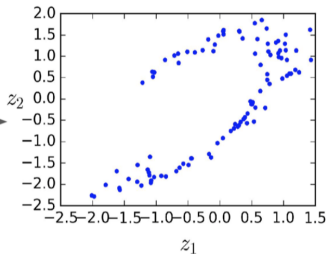
# Basic Idea

## Example: Principal Component Analysis

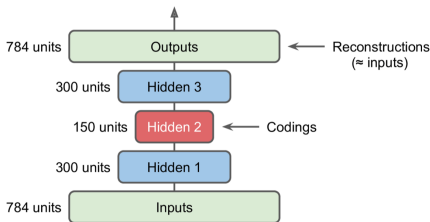
Original 3D dataset



2D projection with max variance



- A 3-2-3 autoencoder with linear units and square loss performs **principal component analysis**: Find linear transformation of data to maximize variance



- A **stacked autoencoder** has multiple hidden layers

- Can share parameters to reduce their number by exploiting symmetry:  $W_4 = W_1^T$  and  $W_3 = W_2^T$

```
weights1 = tf.Variable(weights1_init, dtype=tf.float32, name="weights1")
weights2 = tf.Variable(weights2_init, dtype=tf.float32, name="weights2")
weights3 = tf.transpose(weights2, name="weights3")      # shared weights
weights4 = tf.transpose(weights1, name="weights4")     # shared weights
```



# Stacked Autoencoders

## Incremental Training

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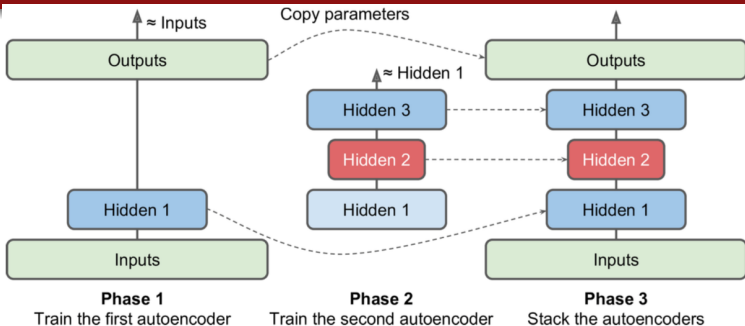
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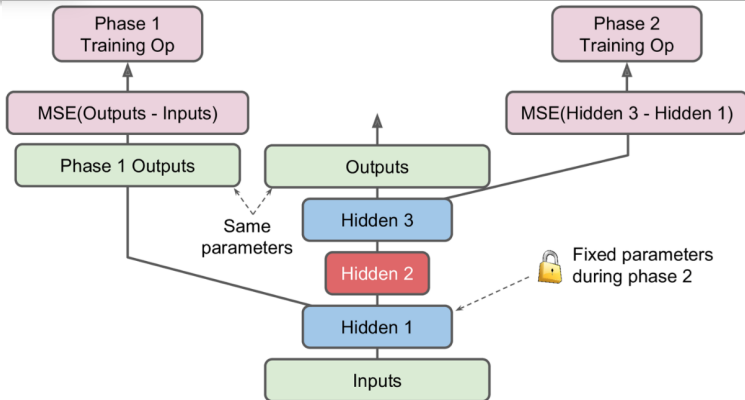
GAN



- Can simplify training by starting with single hidden layer  $H_1$
- Then, train a second AE to mimic the output of  $H_1$
- Insert this into first network
- Can build by using  $H_1$ 's output as training set for Phase 2

# Stacked Autoencoders

## Incremental Training (Single TF Graph)



- Previous approach requires multiple TensorFlow graphs
- Can instead train both phases in a single graph: First left side, then right

# Stacked Autoencoders

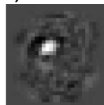
## Visualization

Input MNIST Digit

Network Output



Weights (features selected) for five nodes from  $H_1$ :



# Stacked Autoencoders

## Semi-Supervised Learning

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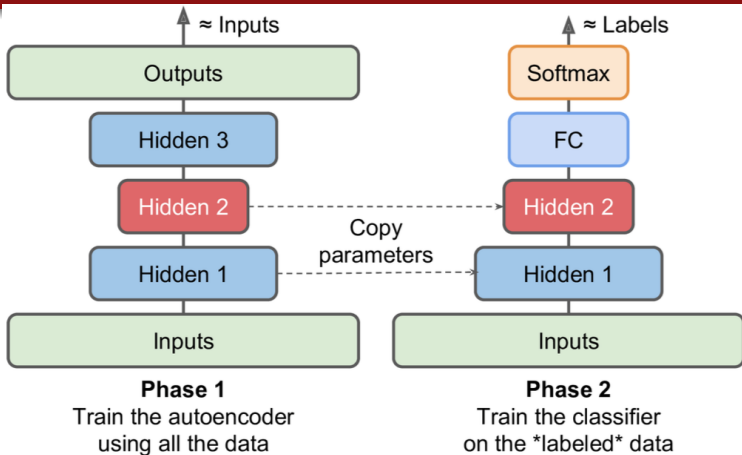
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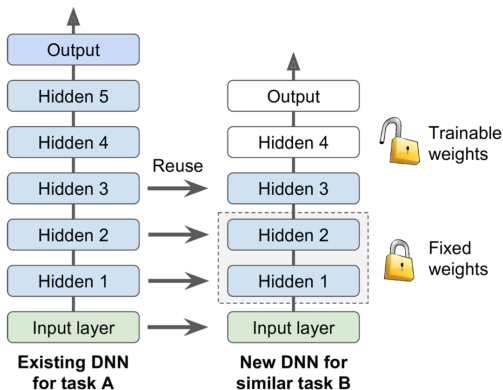
Variational AE

GAN



- Can **pre-train** network with unlabeled data
- ⇒ learn useful features and then train “logic” of dense layer with labeled data

- Can also transfer from a classifier trained on different task, e.g., transfer a GoogleNet architecture to ultrasound classification



- Often choose existing one from a **model zoo**

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- Can train an autoencoder to learn to **denoise** input by giving input **corrupted** instance  $\tilde{x}$  and targeting **uncorrupted** instance  $x$
- Example noise models:
  - **Gaussian noise:**  $\tilde{x} = x + z$ , where  $z \sim \mathcal{N}(\mathbf{0}, \sigma^2 I)$
  - **Masking noise:** zero out some fraction  $\nu$  of components of  $x$
  - **Salt-and-pepper noise:** choose some fraction  $\nu$  of components of  $x$  and set each to its min or max value (equally likely)

# Denoising Autoencoders

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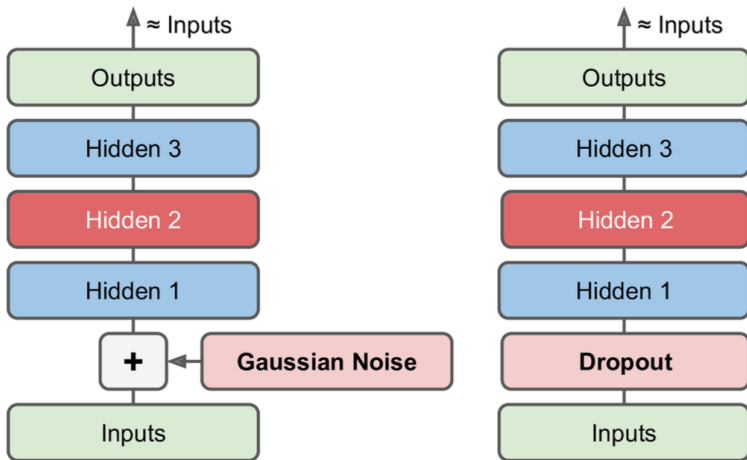
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# Denoising Autoencoders

## Example

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**Denoising AE**

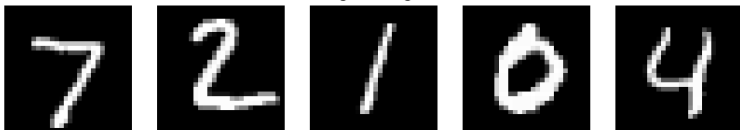
Sparse AE

Contractive AE

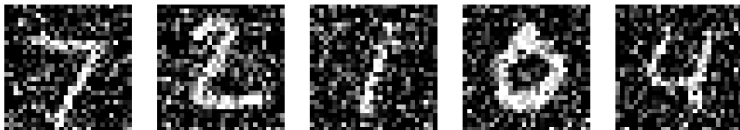
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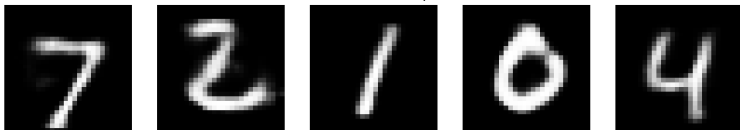
Original Images



Noisy Input



Autoencoder Output





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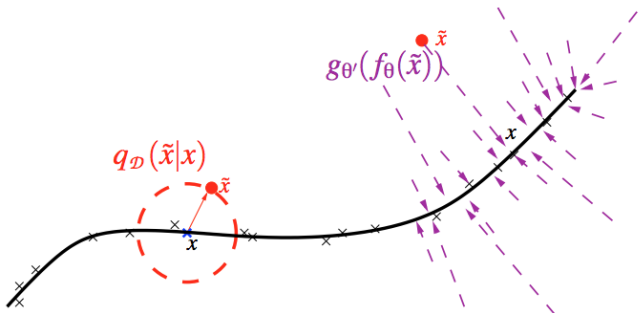
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- How does it work?
- Even though, e.g., MNIST data are in a 784-dimensional space, they lie on a low-dimensional **manifold** that captures their most important features
- **Corruption process** moves instance  $x$  off of manifold
- **Encoder**  $f_\theta$  and **decoder**  $g_{\theta'}$  are trained to project  $\tilde{x}$  back onto manifold



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- An overcomplete architecture
- Regularize outputs of hidden layer to enforce **sparsity**:

$$\tilde{\mathcal{J}}(\mathbf{x}) = \mathcal{J}(\mathbf{x}, g(f(\mathbf{x}))) + \alpha \Omega(\mathbf{h}) ,$$

where  $\mathcal{J}$  is loss function,  $f$  is encoder,  $g$  is decoder,  $\mathbf{h} = f(\mathbf{x})$ , and  $\Omega$  penalizes non-sparsity of  $\mathbf{h}$

- E.g., can use  $\Omega(\mathbf{h}) = \sum_i |h_i|$  and ReLU activation to force many zero outputs in hidden layer
- Can also measure average activation of  $h_i$  across mini-batch and compare it to user-specified **target sparsity** value  $p$  (e.g., 0.1) via square error or **Kullback-Leibler divergence**:

$$p \log \frac{p}{q} + (1 - p) \log \frac{1 - p}{1 - q} ,$$

where  $q$  is average activation of  $h_i$  over mini-batch

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- Similar to sparse autoencoder, but use

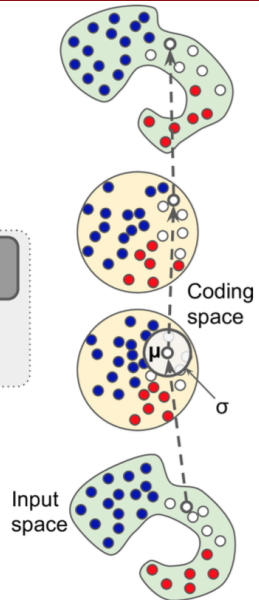
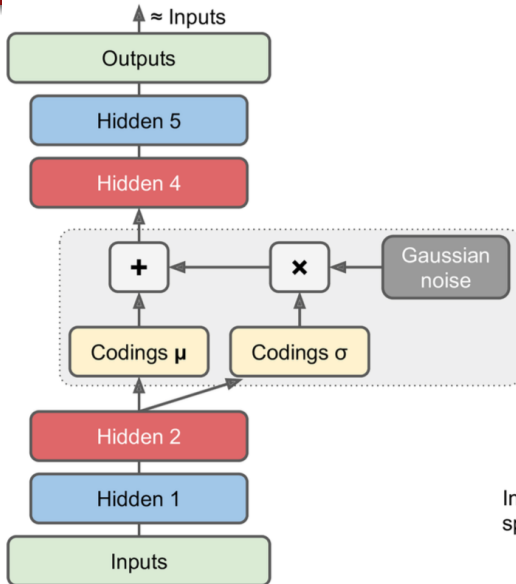
$$\Omega(\mathbf{h}) = \sum_{j=1}^m \sum_{i=1}^n \left( \frac{\partial h_i}{\partial x_j} \right)^2$$

- I.e., penalize large partial derivatives of encoder outputs wrt input values
- This **contracts** the output space by mapping input points in a neighborhood near  $x$  to a smaller output neighborhood near  $f(x)$ 
  - ⇒ Resists perturbations of input  $x$
- If  $\mathbf{h}$  has sigmoid activation, encoding near binary and a CE pushes embeddings to corners of a hypercube





# Variational Autoencoders Architecture



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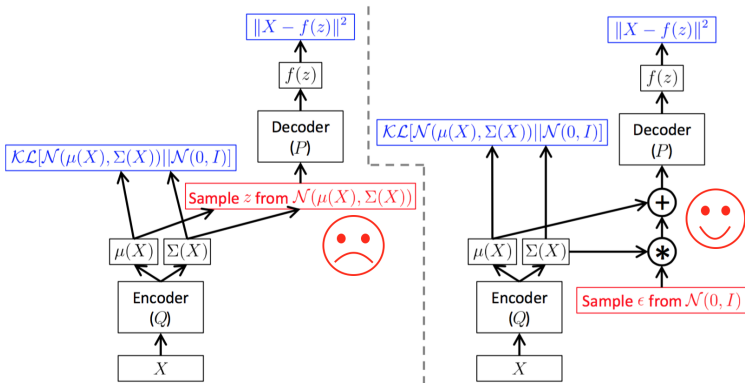
- **Maximum likelihood** (ML) approach for training generative models: find a model ( $\theta$ ) with maximum probability of generating the training set  $\mathcal{X}$
- Achieve this by minimizing the sum of:
  - End-to-end AE loss (e.g., square, cross-entropy)
  - **Regularizer** measuring distance (K-L divergence) from latent distribution  $q(z | x)$  and  $\mathcal{N}(\mathbf{0}, I)$  (= standard multivariate Gaussian)
- $\mathcal{N}(\mathbf{0}, I)$  also considered the **prior distribution** over  $z$  (= distribution when no  $x$  is known)

```
eps = 1e-10
latent_loss = 0.5 * tf.reduce_sum(
    tf.square(hidden3_sigma) + tf.square(hidden3_mean)
    - 1 - tf.log(eps + tf.square(hidden3_sigma)))
```

# Variational Autoencoders

## Reparameterization Trick

- Cannot backprop error signal through random samples
- **Reparameterization trick** emulates  $z \sim \mathcal{N}(\mu, \sigma)$  with  $\epsilon \sim \mathcal{N}(0, 1)$ ,  $z = \epsilon\sigma + \mu$





# Variational Autoencoders

Example Generated Images: Random

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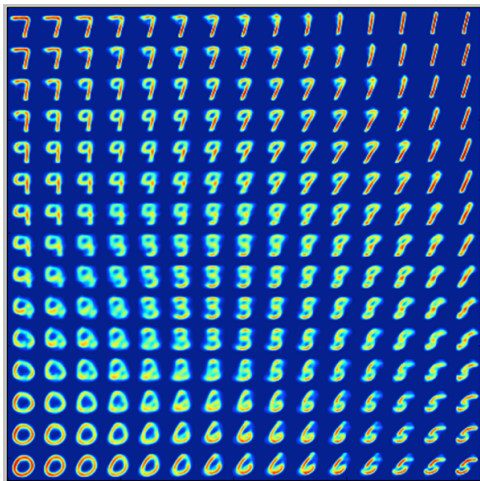
- Draw  $z \sim \mathcal{N}(\mathbf{0}, I)$  and display  $g(z)$



# Variational Autoencoders

Example Generated Images: Manifold

- Uniformly sample points in  $z$  space and decode



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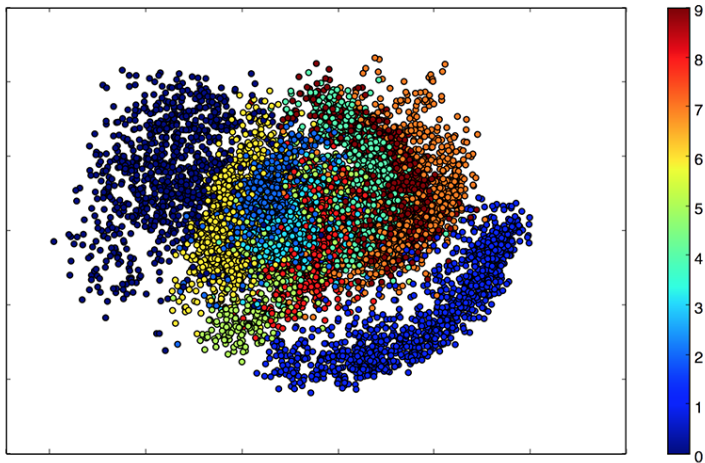
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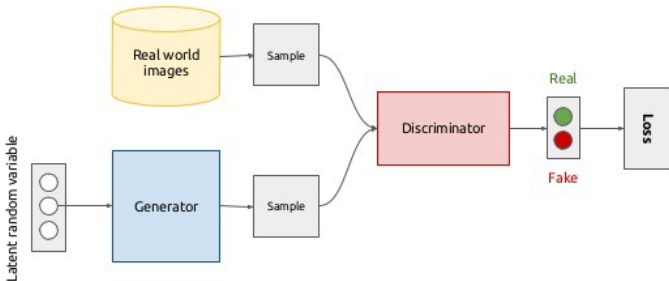
Variational AE

GAN

- Cluster analysis by digit



- GANs are also generative models, like VAEs
- Models a game between two players
  - **Generator** creates samples intended to come from training distribution
  - **Discriminator** attempts to discern the “real” (original training) samples from the “fake” (generated) ones
- Discriminator trains as a binary classifier, generator trains to fool the discriminator



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- Let  $D(x)$  be discriminator parameterized by  $\theta^{(D)}$ 
  - Goal: Find  $\theta^{(D)}$  minimizing  $J^{(D)}(\theta^{(D)}, \theta^{(G)})$
- Let  $G(z)$  be generator parameterized by  $\theta^{(G)}$ 
  - Goal: Find  $\theta^{(G)}$  minimizing  $J^{(G)}(\theta^{(D)}, \theta^{(G)})$
- A **Nash equilibrium** of this game is  $(\theta^{(D)}, \theta^{(G)})$  such that each  $\theta^{(i)}$ ,  $i \in \{D, G\}$  yields a local minimum of its corresponding  $J$

- Each training step:
  - Draw a minibatch of  $x$  values from dataset
  - Draw a minibatch of  $z$  values from prior (e.g.,  $\mathcal{N}(\mathbf{0}, I)$ )
  - Simultaneously update  $\theta^{(G)}$  to reduce  $J^{(G)}$  and  $\theta^{(D)}$  to reduce  $J^{(D)}$ , via, e.g., Adam
- For  $J^{(D)}$ , common to use cross-entropy where label is 1 for real and 0 for fake
- Since generator wants to trick discriminator, can use  $J^{(G)} = -J^{(D)}$ 
  - Others exist that are generally better in practice, e.g., based on ML

# Generative Adversarial Network

DCGAN: Radford et al. (2015)

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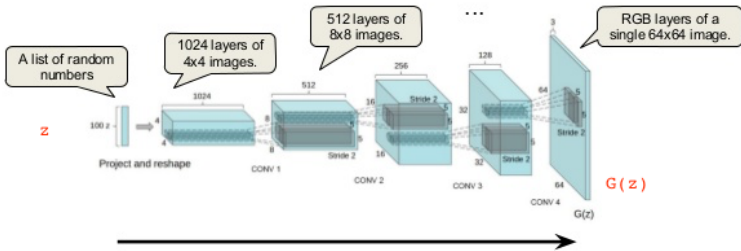
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- “Deep, convolution GAN”
- Generator uses **transposed convolutions** (e.g., `tf.layers.conv2d_transpose`) without pooling to upsample images for input to discriminator



# Generative Adversarial Network

## DCGAN Generated Images: Bedrooms

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Trained from LSUN dataset, sampled  $z$  space





# Generative Adversarial Network

## DCGAN Generated Images: Adele Facial Expressions

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Trained from frame grabs of interview, sampled  $z$  space



# Generative Adversarial Network

## DCGAN Generated Images: Latent Space Arithmetic

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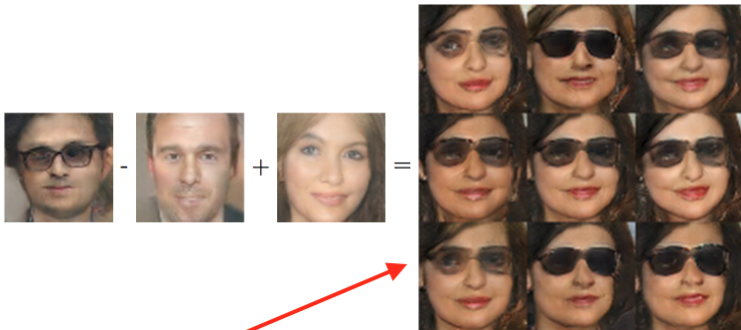
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Performed semantic arithmetic in  $z$  space!



(Non-center images have noise added in  $z$  space; center is noise-free)