

# A Channel Model for Wireless Underground Sensor Networks Using Lateral Waves

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**Abstract**—Wireless Underground Sensor Networks (WUSNs) are an emerging type of wireless sensor networks (WSNs), where sensor nodes are located under the ground and communicate through soil. The major challenge in the development of efficient communication protocols for WUSNs is the characterization of the underground channel. So far, none of the existing models fully capture all the components of electromagnetic signal propagation in the soil medium. In this paper, a closed-form channel model is developed based on electromagnetic propagation principles of signals through soil. Accordingly, three major components that influence underground communication are identified: direct, reflected, and lateral waves, where the latter has not been analyzed for WUSNs so far. The closed-form channel model is shown to agree well with both underground testbed experiments and electromagnetic analysis based on Maxwell's equations, which cannot be represented in closed-form.

## I. INTRODUCTION

In the development of wireless sensor networks (WSNs), applications in constrained environments have gained considerable interest. One such area is wireless underground sensor networks (WUSNs), where the sensor nodes are buried under soil and communicate with each other through soil. The novel applications of WUSNs include intelligent irrigation, environment monitoring, infrastructure monitoring, localization, and border patrol [1]. Especially in precision agriculture, WUSNs are envisioned to be a critical factor in improving water use efficiency by providing real-time information about soil properties [14].

For the design of WUSNs, an underground-to-underground channel model, which captures the impacts of the soil medium on communication, is essential. Accordingly, the topology of the network, its communication protocols, and application parameters can be determined. Moreover, a channel model is critical for the evaluation of WUSN solutions. Compared to terrestrial WSNs, the lossy communication medium in WUSNs, which contains soil, air and water, incurs significantly higher attenuation. Moreover, the permittivity of the medium changes over time and space according to soil moisture [11], [13]. Thus, the established channel models for airwave communication cannot be directly applied to underground situations. We have developed a two-path underground channel model for WUSNs in [9], [17]. However, this model does not capture lateral waves, which manifest themselves in shallow deployments. In this work, we provide a closed-form channel model for underground

communication this specific phenomenon and validate it with experimental and analytical results.

The deployment of WUSNs is generally limited to depths of less than 50 cm [2], [14]. In these cases, a portion of the transmitted electromagnetic waves travel from soil to air, propagate along the soil-air interface, and thereafter penetrate the soil again and reach the receiver. These electromagnetic waves are called *lateral waves* [8], which are a major component of underground communication. Thus, for the modeling of WUSN communication channel, the propagation of the lateral waves must be included.

In [8], an electromagnetic field analysis of underground communication provided using Maxwell's equations [8]. However, this model is computationally complex and difficult to use in practical applications, such as on-board channel evaluation by the sensor nodes or large-scale simulations. In this paper, we develop a *closed-form underground channel model* to capture the characteristics of the underground-to-underground communication based on electromagnetic principles. The resulting model is compared with our earlier two-path channel model in [17] and validated through testbed experiments in [13].

The rest of the paper is organized as follows: First, related work is discussed in Section II. In Section III, dielectric properties of soils and the relation between soil permittivity and soil moisture are introduced as well as the electromagnetic analysis of the underground communication. The developed closed-form underground channel model is described in detail in Section IV. Testbed validations and numerical evaluations of the model are presented in Section V. Finally, concluding remarks are provided in Section VI.

## II. RELATED WORK

Wireless sensor communication in soil medium is a recently evolving field and there exist limited number of models to capture this phenomenon. In [9], [17], we developed a two-path channel model for WUSNs to capture the direct and reflected paths between underground sensors. Moreover, multipath fading is modeled as Rayleigh fading. However, the lateral wave component of the electromagnetic field, which manifests itself when the transceivers are buried near surface, is not considered. In [3] and [16], models for underground-to-aboveground communication are developed. These models,

however, do not capture wireless communication between underground nodes. Channel modeling for underground mines and road tunnels has been studied in [15]. Even though communications in underground mines and tunnels differ from terrestrial applications, the communication still takes in place in air and these models cannot capture propagation through soil. In addition, lateral waves are not observed for communication in mines and tunnels.

A complete description of the electromagnetic field in underground-to-underground communication is provided in [8]. The analysis is based on Maxwell's equations and can be broken down as three components: the direct wave, the reflected wave and the lateral wave. The resulting equations, however, are not in closed-form and hence, it is computationally intensive to utilize this model. Furthermore, the model in [8] is an approximation for the far field communication and is not accurate for near-field communication, which is common in WUSNs due to the high attenuation of soil. In this paper, we employ these equations as foundations to develop a closed-form channel model.

### III. BACKGROUND

In this section, we discuss fundamental properties of soil and electromagnetic propagation in soil, which constitute the basis of our analysis.

#### A. Dielectric Properties of Soil

Wireless underground communication in soil is significantly affected by soil properties and their dynamics. Hence, it is imperative to capture the relative permittivity of soil-water mixture, which is impacted by several factors, such as soil bulk density, soil composition, soil moisture (Volumetric Water Content), salinity, and temperature. A large number of models have been proposed in literature to capture the characteristics of the relative permittivity [4], [10]. These models capture the relative permittivity of different components of soil-water mixture, namely, soil, air, free water and bounded water [4].

We utilize a semi-empirical dielectric model for soil in [10], which is well-suited for the frequency range of 0.3–1.3 GHz, a communication frequency band used in our system. This model is also employed in [17].

#### B. Electromagnetic Field Analysis in Subsurface Soil

The electromagnetic (EM) field model for underground wave propagation in [8] is derived from Maxwell's equations using Fourier transform techniques. In the following, we provide a brief explanation of the analysis approach and refer the reader to [8] or [5] for details. Considering an infinitesimal dipole buried at the subsurface of the soil as the transmitting antenna, the six components of the electromagnetic field at an observation location in the soil can be derived. These components are expressed in the form of integrations of Bessel functions. Based on the EM field, the time-average Poynting vector, which is the power density at a point, can be obtained as

$$\mathcal{P}_{av} = \frac{1}{2} \text{Re}[\hat{\mathbf{E}} \times \hat{\mathbf{H}}^*], \quad (1)$$

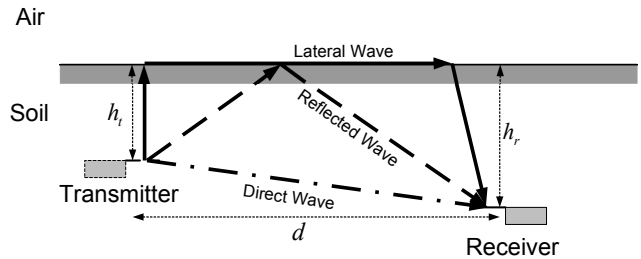


Fig. 1: The three electromagnetic waves at an underground point.

where  $\hat{\mathbf{E}}$  is the electric field intensity and  $\hat{\mathbf{H}}^*$  is the conjugate of the magnetic field intensity. The details of the derivations are provided in [8] and reprinted in [5].

### IV. CLOSED-FORM UNDERGROUND CHANNEL MODEL

The electromagnetic analysis for underground-to-underground communication in [8] is computationally complex. This approach is not suitable for practical applications where fast evaluation of the channel is needed. Especially in WUSNs, computation capacity limited nodes require a simpler way to estimate the channel quality from local sensor measurements to dynamically determine transmission power. In this section, we provide a channel model based on the analysis of the electromagnetic field and Friis equations. The model is in closed-form and has a good approximation as we report in Section V.

We consider the model depicted in Fig. 1, where a transmitter and a receiver located at a distance of  $d$  and depths  $h_t$  and  $h_r$ , respectively. Underground communication between this pair consists of three EM waves: (1) The direct wave is the result of sight-of-line wave propagation from the transmitter to the receiver through soil. (2) The reflected wave is the wave reflected by the air-soil interface and also propagates through soil. (3) The lateral wave is the result of wave propagating in air and penetrating back to soil. In the following, the Poynting vectors for the three components are derived first. Then, for a specific receiving antenna model, the derived Poynting vectors are used to find the received power. This leads to a closed-form channel model, 3-wave model, that can be used to evaluate wireless underground communication.

#### A. The Direct Wave

The direct wave is the spherical wave traveling outward radially from the transmitter to the receiver in a line-of-sight path. In over-the-air communication, direct waves are the dominant part of the received power. However, in wireless underground communications, the direct wave is attenuated much faster in especially wet soils due to soil conductivity. Nonetheless, the direct wave can still be modeled based on the well known Friis equations. The time-average Poynting vector of the direct wave is

$$\mathcal{P}_{av}^d = \left( \frac{D_d}{4\pi r_1^2} \right) e^{i2k_s r_1} G_t, \quad (2)$$

where  $r_1$  is the distance between the source and the observation point;  $k_s = \beta_s + i\alpha_s = \omega\sqrt{\mu_0\epsilon_s}$  is the wave number in

soil, where  $\beta_s$  accounts for phase shifting and  $\alpha_s$  accounts for attenuation;  $\omega = 2\pi f$ , where  $f$  is the frequency of the wave;  $\mu_0$  and  $\hat{\epsilon}_s$  are the permeability and permittivity of the soil, respectively. We assume the soil is nonmagnetic, thus the permeability of vacuum,  $\mu_0$ , is employed. In (2),  $G_t$  is the antenna gain of the transmitter and  $D_d$  is a constant related to soil permittivity, which will be discussed in Section V. The component  $e^{i2k_s r_1}$  accounts for the attenuation and phase shifting of wave propagation in soil. The attenuation is due to the fact that  $k_s$  is a complex number instead of a real number. Note that (2) is different from Friis equation because it only describes the power density in a location, and the receiving area of the receive antenna is not considered. To calculate the received power, this Poynting vector should be multiplied by the receiving area of a given antenna, which is defined as [7]:  $A = \left(\frac{\lambda_s^2}{4\pi}\right) G_r$ , where  $\lambda_s$  is the wavelength in soil and  $G_r$  is the antenna gain of the receiver. Based on Fig. 1,  $r_1 = \sqrt{(h_t - h_r)^2 + d^2}$  and the wavelength in soil is calculated as  $\lambda_s = 2\pi/\beta_s$ .

The direct gain of an antenna depends on the propagation pattern of the given antenna. For the purpose of comparing with the electromagnetic analysis, an infinitesimal dipole is assumed, whose direct gain is calculated as  $G_t = \sin \alpha$ , where  $\alpha$  is the angle related to the extension line of the dipole.

### B. The Reflected Wave

Due to the different dielectric constants of air and soil, the traveling wave incident to the air-soil interface is reflected as shown in Fig. 1. For the tractability of the analysis, the air-soil interface is assumed to be flat. Thus, the reflected wave can be modeled as a spherical wave traveling from an image source symmetric of the real source according to the air-soil interface and the whole space is filled with soil. Then, the time-average Poynting vector of this wave is

$$\mathcal{P}_{av}^r = D_r \left( \frac{1}{4\pi r_2^2} \right) e^{i2k_s r_2} G_t \Gamma^2, \quad (3)$$

where  $D_r$  is a constant related to soil permittivity,  $r_2$  is the length of the reflection path,  $r_2 = \sqrt{(h_t + h_r)^2 + d^2}$ , and  $\Gamma$  is the reflection coefficient given by [7]:

$$\Gamma = \frac{\frac{1}{n} \cos \theta_{ri} - \cos \theta_{rt}}{\frac{1}{n} \cos \theta_{ri} + \cos \theta_{rt}}, \quad (4)$$

where  $n$  is the refractive index of soil,  $\theta_{ri}$  and  $\theta_{rt}$  are the incident angle and the refracted angle, respectively. Based on Snell's law,

$$\begin{aligned} \sin \theta_{ri} &= \frac{d}{r_2}, & \cos \theta_{ri} &= \frac{h_t + h_r}{r_2}, \\ \sin \theta_{rt} &= n \sin \theta_{ri}, & \cos \theta_{rt} &= \sqrt{1 - \sin^2 \theta_{rt}}. \end{aligned} \quad (5)$$

Since the permittivity of soil is a complex number, the refractive index of soil is calculated as

$$n = \sqrt{\frac{\sqrt{\epsilon'^2 + \epsilon''^2} + \epsilon'}{2}}, \quad (6)$$

in which  $\epsilon'$  and  $\epsilon''$  are the real and imaginary parts of the relative permittivity of the soil.

For the attenuation and phase shifting, since the whole path of the reflected wave is still in soil, only the wave number in soil,  $k_s$ , is employed.

### C. The Lateral Wave

In the previous underground-to-underground channel models, only direct waves and reflected waves have been considered. However, due to the fact that the sensor motes are buried near the air-soil interface, lateral waves are one of the tree major components of the EM field [8], and also dominate communication in the far field. The path of the lateral wave is shown in Fig. 1. From soil to air, the wave travels vertically from the transmitter to the interface. At the interface, it resembles a new source and propagates horizontally along the interface as a spherical wave. At an incidence angle of  $\sim \pi/2$ , the wave penetrates into the soil. The refracted wave is a portion of the original wave and it travels downward from the air-soil interface to the receiver in soil. The corresponding time-average Poynting vector of the lateral wave is

$$\mathcal{P}_{av}^L = \left( \frac{D_l}{4\pi d^4} \right) e^{i2k_s(h_t+h_r)} e^{i2k_0 d} T^2 G_t, \quad (7)$$

where  $T$  is the refraction coefficient when the wave travels from air to soil and  $D_l$  is a constant for the diffusion along air-soil interface. Note, the refraction coefficient from soil to air is not considered since all the energy is refracted to the air. However, from air to soil, only part of the wave is refracted to the soil, thus  $T$  is less than 1 and is defined as

$$T = \frac{2 \cos \theta_{li}}{n \cos \theta_{li} + \cos \theta_{lt}}, \quad (8)$$

where  $n$  is the refractive index of the soil as shown in (6).

Since the motes are very close to soil-air interface, the diffusion in the soil is negligible. Thus, the diffusion is only related to the horizontal distance of the transceiver pair. Also, the diffusion cannot be modeled as inversely proportional to  $d^2$  because of the interface. Based on the analysis of the electromagnetic wave, both the  $\mathbf{E}$  field and the  $\mathbf{H}$  field of the lateral wave are functions of  $\frac{1}{d^2}$ . Thus, the power density, which is a product of  $\mathbf{E}$  and  $\mathbf{H}$ , is a function of  $\frac{1}{d^4}$ . Therefore,  $d^4$  is used in (7) and a constant  $D_l$  is employed.

The path of the lateral wave consists two sections in soil and one section in air. Accordingly, the attenuation and phase shifting are calculated in two parts in (7):  $e^{i2k_0 d}$  is the attenuation and phase shifting in the air, while  $e^{i2k_s(h_t+h_r)}$  is the attenuation and phase changing in the soil. Due to the high refractive index of soil, the refraction angle is quite small. For volumetric water content (VWC) in the range of 10%–40%, the refraction angle is in the range of  $10^\circ$ – $20^\circ$ . Therefore, the wave path length in the soil is approximated by the sum of the burial depths of the transmitter and the receiver.

### D. The Composed Field

The total power density  $\mathcal{P}_{av}$  can then be derived as the superposition of the three components. Namely,

$$\mathcal{P}_{av} = \mathcal{P}_{av}^d + \mathcal{P}_{av}^r + \mathcal{P}_{av}^L. \quad (9)$$

Note the sum is a vector sum since the three components have different directions as shown in Fig. 1. To calculate the received power of a receiving antenna, power density is multiplied by the receiving area of a specific antenna. Here, to compare with the electromagnetic field analysis, we map the total power density into Cartesian coordinates,

$$\begin{aligned} \mathcal{P}_{av}^x &= (\mathcal{P}_{av}^d \times \frac{d}{r_1} + \mathcal{P}_{av}^r \times \frac{d}{r_2} + \mathcal{P}_{av}^L \times \sin \theta_{lt}) \cos \phi, \\ \mathcal{P}_{av}^y &= (\mathcal{P}_{av}^d \times \frac{d}{r_1} + \mathcal{P}_{av}^r \times \frac{d}{r_2} + \mathcal{P}_{av}^L \times \sin \theta_{lt}) \sin \phi, \quad (10) \\ \mathcal{P}_{av}^z &= \mathcal{P}_{av}^d \times \frac{|h_t - h_r|}{r_1} + \mathcal{P}_{av}^r \times \frac{h_t + h_r}{r_2} + \mathcal{P}_{av}^L \times \cos \theta_{lt}, \end{aligned}$$

where  $\phi$  is the azimuth angle of the receiver in the cylindrical coordinates.

### E. The Received Power of an Isotropic Antenna Pair

In traditional channel models, isotropic antennas are assumed [7]. In this section, we derive the received power when isotropic antennas are used for transmitting and receiving. For isotropic antennas,  $G_t = G_r = 1$ . Thus, the receiving area becomes  $A_{iso} = \lambda_s^2 / 4\pi$ .

The three components of the received power, written in logarithmic form, are

$$\begin{aligned} P_r^d &= P_t + 20 \log_{10} \lambda_s - 20 \log_{10} r_1 - 8.69 \alpha_s r_1 - 45, \\ P_r^r &= P_t + 20 \log_{10} \lambda_s - 20 \log_{10} r_2 - 8.69 \alpha_s r_2 \\ &\quad + 20 \log_{10} \Gamma - 45, \quad (11) \\ P_r^L &= P_t + 20 \log_{10} \lambda_s - 40 \log_{10} d - 8.69 \alpha_s (h_t + h_r) \\ &\quad + 20 \log_{10} T - 30, \end{aligned}$$

where  $\Gamma$  and  $T$  are given in (4) and (8), respectively,  $\alpha_s$  is the imaginary part of the wave number in soil and  $\lambda_s$  is the wavelength in soil. For isotropic antenna, the overall received power is the sum of the three components. Thus,

$$P_r = 10 \log_{10} (10^{\frac{P_r^d}{10}} + 10^{\frac{P_r^r}{10}} + 10^{\frac{P_r^L}{10}}). \quad (12)$$

## V. MODEL COMPARISON AND VERIFICATION

In this section, we compare the developed 3-wave model (3W model) with the electromagnetic field analysis [8] to show its performance of approximation. In addition, the model is also compared with the two-path model [9], [17] and testbed results for verification.

### A. Comparison with Electromagnetic Analysis

A comparison of the electromagnetic field analysis and the closed-form 3W model is shown in Fig. 2, where an approximation of the EM field from [8] is used. Two values of volumetric water content (VWC) are assumed: (1) dry soil with VWC at 10%, and (2) wet soil with VWC at 35%. The

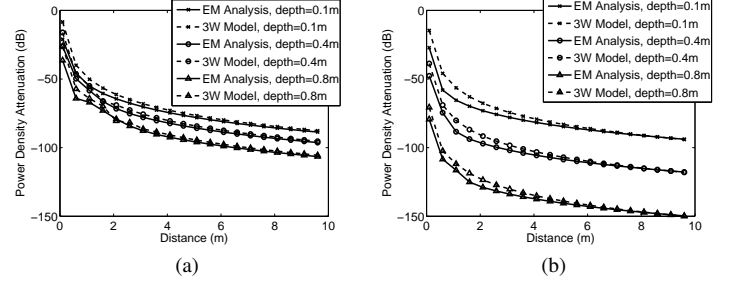


Fig. 2: Comparison of the results of the electromagnetic analysis and the 3W model with different burial depths. (a) VWC=10%; (b) VWC=35%

VWC values are from field measurements and reported in [6]. For each of the situations, three burial depths, 0.1 m, 0.4 m and 0.8 m, are investigated. The figures show the attenuation of the underground channel versus horizontal distance between the transmitter and the receiver.

To apply the 3W model, the values of  $D_d$ ,  $D_r$  and  $D_l$  need to be determined. Ideally, those values should be obtained by analyzing extensive empirical evaluations. Here, we compare our model to the electromagnetic model, and employ minimum mean square error (MMSE) to estimate those values, which are found to be  $D_d = D_r = 0.005$  and  $D_l = 0.15$ .

It is observed that the 3W model captures the main components of the electromagnetic field and matches the results of the analysis. Furthermore, the two models match better at the far field than the near field. For the near field ( $d < 1$  m) the results of the 3W model is about 10% higher than the EM model. However, for the far field ( $d > 2$  m), the results are less than 5% higher. For the very far field ( $d > 6$  m), the difference of the two models is less than 1%. This is mainly because the electromagnetic analysis is an approximation for the far field and for the near field it has lower accuracy. Thus, these two models need to be compared with detailed testbed results.

The effects of the soil moisture and burial depth can also be analyzed from the figures. When the transceivers are deeply buried, the path in the soil increases and the attenuation increases. Accordingly, when the VWC is 10% and the motes are buried at 0.1 m (Fig. 2(a)), the attenuation at the distance of 4 m is  $-72$  dB. At the same horizontal distance, the attenuation increases to  $-80$  dB when the motes are buried at 0.4 m and  $-91$  dB if they are buried at 0.8 m.

Another factor that influences underground communication is soil moisture. High moisture soil increases the attenuation of the electromagnetic waves and decreases the signal strength. Based on the analysis, when the burial depth is 0.4 m and the VWC is 10% (Fig. 2(a)), at 2 m away, the signal is attenuated by 70 dB. However, if the VWC increases to 35% (Fig. 2(b)), the attenuation at 2 m will increase to 90 dB. Equally noteworthy is that the effect of the soil moisture varies by burial depth. If the motes are buried shallow (0.1 m), the effect is almost negligible. This occurs because the lateral wave path in soil is very short, and hence the attenuation by soil has small impact

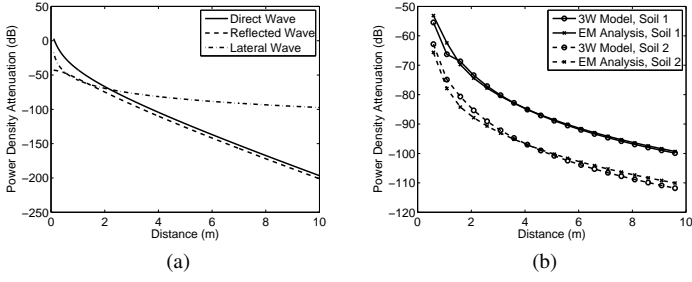


Fig. 3: Analysis of the Model. (a) the comparison of the three components over distance; (b) applying the model to two soil types.

in this situation. Conversely, if the motes are buried deep, the effect of the soil moisture is clearly observed. At the VWC of 35% and the burial depth of 0.8 m, the attenuation increases more than 30 dB compared to the VWC of 10%.

### B. Model Analysis

In Fig. 3(a), the power density of three components, the direct wave, the reflected wave and the lateral wave, over distance are depicted. The transmitter is buried at the depth of 0.4 m and the receiver is buried at the depth of 0.5 m. It is shown that the power density of the reflected wave is about 10 dB lower than the direct wave in the near field but close to the direct wave in the far field since at the far field the path lengths of the two waves are similar. More importantly, at distance less than 2 m, the direct wave has a higher power density than the lateral wave. Yet, for longer distances, the direct wave and the reflected wave are attenuated drastically, such that the lateral wave becomes dominant. For instance, at the distance of 3 m, the density of the direct wave is 10 dB lower than the lateral wave, while at the distance of 4 m it is 20 dB lower.

We also apply the 3W model to two different soil types. Soil I is a dry sandy soil with the percentage of sand,  $S = 50\%$ , the percentage of clay,  $C = 15\%$  and VWC = 5%. Soil II is from our testbed, which contains 31% of sand, 29% of clay and VWC = 20%. The channel qualities for these two soil types are shown in Fig. 3(b). For each of the soil types, we compare our model with the electromagnetic analysis. It is shown that for both of them, our model matches the electromagnetic analysis. Similar to the results in Section V-A, in the near field ( $d < 1$  m), the 3W model has results 10% higher than the electromagnetic analysis, and in the far field ( $d > 2$  m), the difference reduces to less than 5%. Moreover, Soil I has a lower attenuation (10 dB) than Soil II. The main reason behind it is that sandy soil is less capable of holding water, a primary factor of wave attenuation.

### C. Comparison with the Two-path Model and Empirical Results

The results of the 3W model, the two-path model [17] and testbed measurements are shown in Fig. 4. The testbed results are from our previous work with Mica2 sensor motes in [13], which are buried at the depth of 0.4 m and the transmission power is set to 10 dBm. For each of the horizontal distance, 50

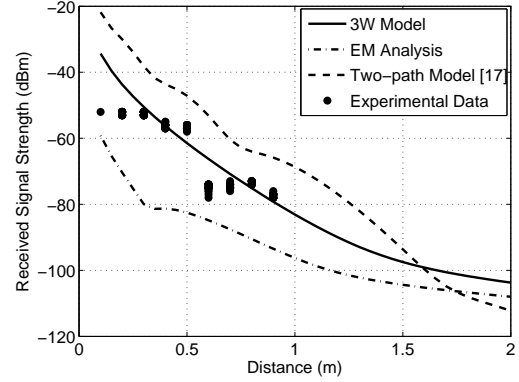


Fig. 4: The comparison of the Proposed Model, the Two-path Model and Testbed Results. (burial depth=0.4 m)

samples are obtained and depicted in the figure. The result of the 3W model is calculated using (12). The properties of the soil, such as the percentage of sand,  $S = 31\%$ , the percentage of the clay,  $C = 29\%$ , are taken from the testbed as the input to the two models.

Due to the limitation of Mica2 motes, the signal strength measurement is not accurate, especially when the received power is higher than -50 dBm, where clipping effect is observed [12]. Nevertheless, it is still clearly shown that the 3W model is more accurate than the two-path model. Comparing the results at 0.3–0.9 m, except the results at 0.6 m, the difference between 3W model and the experiment results is less than 3 dB. The experiment data at 0.6 m is irregularly low, which may be caused by low quality of the specific mote or other environment factors. The results from the two-path model is 10–15 dB higher than the experiment results. As mentioned in Section V-A, the approximation of the EM analysis has low accuracy in the near field, which causes the results to be 10–20 dB lower than the experiment results. These initial comparisons illustrate the accuracy of the model but we also acknowledge the need for further testbed experiments with different soil types to fine tune the model, which is out of the scope of this work.

## VI. CONCLUSIONS

In this paper, we develop a closed-form channel model for communication in soil medium. Compared to previous underground channel models, the model includes all the three components in the field, namely, the direct wave, the reflected wave and more importantly, the lateral wave. Validations with empirical channel measurements show that the 3W model is a good approximation to the electromagnetic analysis.

As a future work, we plan to conduct extensive field experiments to continue validating the 3-wave model in different settings. Especially the relationship between the constants,  $D_d$ ,  $D_r$ ,  $D_l$  and the soil properties will be investigated. Moreover, soils with layers of different properties will also be considered.

## VII. ACKNOWLEDGEMENTS

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