

# Recitation 9

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- Given the Poset:  $(\{\{1\}, \{2\}, \{4\}, \{1, 2\}, \{1, 4\}, \{2, 4\}, \{3, 4\}, \{1, 3, 4\}, \{2, 3, 4\}\}, \subseteq)$ 
  1. Find the maximal elements:  $\{1, 2\}, \{1, 3, 4\}, \{2, 3, 4\}$  (because these are not subsets of any other sets in the relation right?)
  2. Find the minimal elements:  $\{1\}, \{2\}, \{4\}$  (again, there are no subsets of these sets in the relation)
  3. Is there a maximum (i.e., greatest) element?: No. It does not exist.
  4. Is there a minimum (i.e., least) element?: No. It does not exist.
  5. Find the set of all upper bounds of  $\{\{2\}, \{4\}\}$ :  $\{\{2, 4\}, \{2, 3, 4\}\}$
  6. Find the least upper bound (lub) of  $\{\{2\}, \{4\}\}$ : the element  $\{2, 4\}$
  7. Find the set of all lower bounds of  $\{\{1, 3, 4\}, \{2, 3, 4\}\}$ :  $\{\{3, 4\}, \{4\}\}$
  8. Find the greatest lower bound (glb) of  $\{\{1, 3, 4\}, \{2, 3, 4\}\}$ : the element  $\{3, 4\}$