Due: Monday, March 6, 2017 Written by Daniel Geschwender

Programmatically Generating the PL sentence of a Sudoku in CNF (Part 1 of 3):

The goal of this homework is to write a simple program to generate the text file, in the DIMACS CNF 'format,' of a Sudoku instance. The homework is broken into three parts as follows:

- Part 1: Manually write a simple CNF file in the DIMACS format; solve with MiniSAT; and write code to generate the first set of clauses that model a Sudoku puzzle.
- Part 2: Write code to generate a CNF file expressing all the rules of an empty Sudoku board and solve with MiniSAT.
- Part 3: Write code to parse a string representing a partially filled instance of Sudoku. Add the corresponding clauses to the CNF file and solve with MiniSAT.

In this homework, you have to do only Part 1.

Grading Rubric for Part 1:

Dessert problem CNF file is properly formatted	3
MiniSAT gives correct solution when run on the dessert CNF file	3
Code and README are clear and commented	3
Program generates the correct output	6
Total:	15

General Instructions:

- The program may be written in any language that can be compiled and run on cse.unl.edu.
- You are free to use file input/output or standard input (stdin) and standard output (stdout). If using stdout (printing to the console) you can write to a file by redirecting the output. (./yourProgram > outputFilename.cnf)
- A README file must be included. It should clearly describe all necessary steps to compile and run the program.
- The model should follow the Sudoku CNF formulation from the textbook (see page 33) and reproduced below.
- The generated output should conform to the DIMACS CNF file specifications described below.
- Submit your code, the README file, and all accompanying files via handin. No hard copy is required. All submitted files should include your last name using the following filename format: <lastname>-<filename>.<extension>
- This homework must be completed individually. LATEX bonus and partner policy do not apply.

The Sudoku CNF Formulation:

We will adopt the following formulation of the Sudoku problem to generate the CNF file:

- The proposition p(i, j, n) indicates that the cell in row i and column j is given value n. In the CNF file, represent p(i, j, n) by ijn. (e.g., $\neg p(3, 8, 7)$ corresponds to -387 in the CNF file)
- Every row contains every number:

$$\bigwedge_{i=1}^{9} \bigwedge_{n=1}^{9} \bigvee_{j=1}^{9} p(i,j,n) \tag{1}$$

• Every column contains every number:

$$\bigwedge_{i=1}^{9} \bigwedge_{n=1}^{9} \bigvee_{i=1}^{9} p(i,j,n) \tag{2}$$

• Every 3x3 block contains every number:

$$\bigwedge_{r=0}^{2} \bigwedge_{s=0}^{2} \bigwedge_{n=1}^{9} \bigvee_{i=1}^{3} \bigvee_{j=1}^{3} p(3r+i,3s+j,n)$$
(3)

• No cell contains more than one number:

$$\bigwedge_{i=1}^{9} \bigwedge_{j=1}^{9} \bigwedge_{n=1}^{8} \bigwedge_{m=n+1}^{9} (\neg p(i,j,n) \vee \neg p(i,j,m))$$
 (4)

DIMACS CNF Format Specification:

- Comment lines begin with the character 'c'.
- A problem line must be included before any clauses. The problem line uses the following format: p cnf <# variables><# clauses>.
- Each clause is given by a line of non-null numbers, separated by spaces, and ending with a '0'. The numbers correspond to variables. A negative number represents a negated variable in the clause.

Note on MiniSAT Variables:

Because of the way the variables are specified in our Sudoku model, there are gaps in the numbering of the variables. MiniSAT will see that the highest variable is 999 and will assume that there are 999 variables. This is a 'feature' of MiniSAT. The solution generated by MiniSAT will include all the variables in 1...999. The additional variables (1...110, 120, 130, etc.) should simply be ignored.

Tasks for Part I

Problem A:

Consider the following dessert problem:

There are four choices of desserts: ice cream, fruit bowl, cake, pie. Exactly one dessert must be selected (i.e., one and only one).

```
(iceCream \lor fruitBowl \lor cake \lor pie)
\land \quad (\neg iceCream \lor \neg fruitBowl)
\land \quad (\neg iceCream \lor \neg cake)
\land \quad (\neg iceCream \lor \neg pie)
\land \quad (\neg fruitBowl \lor \neg cake)
\land \quad (\neg fruitBowl \lor \neg pie)
\land \quad (\neg cake \lor \neg pie)
```

Manually write a DIMACS file of the CNF sentence that model the desserts problem described above.

- Add a comment line to the file to describe your variables.
- Make sure you include the problem line.
- Run MiniSAT on the file that you wrote, store the MiniSAT results with the solution in an output file.

Problem B:

Write a program to generate the first set of clauses describing the Sudoku rules (Expression (1)). Use the pseudocode shown in Algorithm 1 to help structure your program. Notice the correspondence between the loops and the iterated conjunction/disjunction operators. The code should produce output resembling Figure 1. Comment/problem lines are *not* required at this point. The output does *not* yet need to be run on MiniSAT.

Algorithm 1: Loop structure for printing clauses in DIMACS CNF format. Note: the '+' symbol represents a string concatenation operator.

```
      111
      121
      131
      141
      151
      161
      171
      181
      191
      0

      112
      122
      132
      142
      152
      162
      172
      182
      192
      0

      113
      123
      133
      143
      153
      163
      173
      183
      193
      0

      114
      124
      134
      144
      154
      164
      174
      184
      194
      0

      115
      125
      135
      145
      155
      165
      175
      185
      195
      0

      116
      126
      136
      146
      156
      166
      176
      186
      196
      0

      117
      127
      137
      147
      157
      167
      177
      187
      197
      0

      118
      128
      138
      148
      158
      168
      178
      188
      198
      0

      119
      129
      139
      149
      159
      169
      179
      189
      199
      0

      211
      221
      231
      241
      251
      261
      271
      281
```

Figure 1: A sample of the expected output.

Files to Submit to Handin:

Use the following filename format: <lastname>-<filename>.<extension>

- The dessert problem CNF file
- $\bullet\,$ The MiniSAT results file for the dessert problem
- Your code
- A README file
- A file containing the output generated from your code