Problem A (2.3:10)

Let \( f : \{a, b, c, d\} \rightarrow \{a, b, c, d\} \), for each of function \( f \) defined below

1. \( f(a) = b, \ f(b) = a, \ f(c) = c, \ f(d) = d. \)
2. \( f(a) = b, \ f(b) = b, \ f(c) = d, \ f(d) = c. \)
3. \( f(a) = d, \ f(b) = a, \ f(c) = c, \ f(d) = d. \)

Determine whether each \( f \) is

a one-to-one (injective)

b onto (surjective)

c one-to-one correspondence (bijective)
Problem B (2.3.12)
For each function $f : \mathbb{Z} \rightarrow \mathbb{Z}$

- $f(n) = n - 1$.
- $f(n) = n^2 + 1$.
- $f(n) = n^3$.
- $f(n) = \lceil \frac{n}{2} \rceil$.

1. Determine whether each $f$ is one-to-one (injective).
2. Determine whether each $f$ is onto (surjective).
3. Determine whether each $f$ is one-to-one correspondence (bijective).
4. Determine whether each $f$ is invertible. If so, give $f^{-1}$.

Problem C
For functions $f(x) = x^2 + x$ and $g(x) = x - 2$ from $\mathbb{R}$ to $\mathbb{R}$, find:

1. $f \circ g$
2. $g \circ f$
3. $f \circ f$
4. $g \circ g$

Note: we have $\text{rng}(f) = \text{rng}(g) = \text{domain}(f) = \text{domain}(g)$. 
Instructions  Follow instructions carefully, failure to do so may result in points being deducted.

- The homework can be submitted on paper or via handin. Homework neatly formatted in \LaTeX will receive a 10 percent bonus. You will not receive the bonus points if you work with a partner (see below).
- Clearly label each problem and submit answers in order.
- Staple this cover page to the front of your assignment for easier grading.
- Late submissions will not be accepted
- When you are asked to prove something, you must give a formal, rigorous, and complete a proof as possible. Each step in your proof must contain explanation that would allow us to understand what theorem/logic you have applied to arrive at that step.
- You are to work individually, and all work should be your own. Check partner policy below.
- The CSE academic dishonesty policy is in effect (see http://cse.unl.edu/ugrad/resources/academic_integrity.php).

Partner Policy  You may work in pairs, but you must follow these guidelines:

1. You must work all problems together. You may not simply partition the work between you.
2. You must use \LaTeX and you may divide the typing duties however you wish.
3. You may not discuss the problems with other groups or individuals.
4. Hand in only one hard copy with both author’s names.