Title: Logical Agents

AIMA: Chapter 7 (Sections 7.1, 7.2, and 7.3)

Introduction to Artificial Intelligence

CSCE 476-876, Spring 2012

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Outline

- Knowledge bases
- Wumpus world
- Logic for Knowledge Representation & Reasoning
  - Syntax
  - Semantics
  - Inference mechanisms: complexity, completeness

  Propositional logic/sentential logic

  Predicate logic/first-order logic

Knowledge Base

A fact in the world: A representation of a fact in the world

A sentence= a representation of a fact in the world in a <u>formal language</u>

A Knowledge Based (KB): A set sentences

A set (of representations) of facts about the world

Issues: Access to KB, Representation (language), Reasoning (inference)

Level of Knowledge

Agents can be viewed at various levels:

1. **Epistemological**:
   Abstract description of what the agent knows about the world

2. **Logical**:
   Encoding of knowledge into sentences

3. **Implementation**:
   Actual implementation (lists, arrays, hash tables, etc.)
   - Very important for performance of agent
   - Irrelevant for higher levels of knowledge

A simple KB-agent

```
function KB-AGENT( percept) returns an action
  static: KB, a knowledge base
          t, a counter, initially 0, indicating time

  TELL(KB, MAKE-PERCEPT-SENTENCE( percept, t))
  action ← ASK(KB, MAKE-ACTION-QUERY(t))
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t ← t + 1
  return action
```

The agent must be able to:

- represent states, actions, etc.
- incorporate new percepts
- update internal representations of the world
- deduce hidden properties of the world
- deduce appropriate actions

Knowledge-Based Agent

function KB-AGENT(*percept*) **returns** an *action*
  static: *KB*, a knowledge base
    t, a counter, initially 0, indicating time

  TELL(*KB*, MAKE-PERCEPT-SENTENCE(*percept*, *t*))
  action ← ASK(*KB*, MAKE-ACTION-QUERY(*t*))
  TELL(*KB*, MAKE-ACTION-SENTENCE(*action*, *t*))
  $t \leftarrow t + 1$
  return *action*

Perceives: Tells KB about new percepts (new sentences)
  Representation: MAKE-PERCEPT-SENTENCE

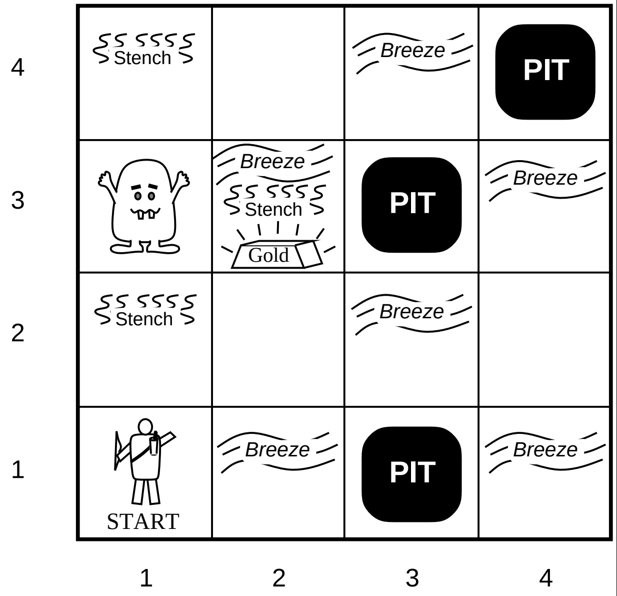
Access to KB: Asks KB about actions to take (inference)
  Two primitives: ASK and TELL hide reasoning details

Acts: Tells KB about actions (new sentences)
  Representation: MAKE-ACTION-SENTENCE,
  MAKE-ACTION-QUERY

Motivating example: The Wumpus world

Early computer game

Agent explores a cave with:



- bottomless pits
- a beast that eats anyone who enters the room, and
- heap of gold to trap

PEAS description of the Wumpus world

Performance measure: gold +1000, death -1000, -1 per step, -10 for using the arrow

Environment: Squares adjacent to Wumpus are smelly
Squares adjacent to pit are breezy
Glitter iff gold is in the same square
Shooting kills Wumpus if you are facing it
Shooting uses up the only arrow
Grabbing picks up gold if in same square
Releasing drops the gold in same square

Sensors: Breeze, Glitter, Smell

Actuators: Left turn, Right turn, Forward, Grab, Release, Shoot

Wumpus World: Characterization

Is the world:

• Observable?	No, only local perception
• Deterministic?	Yes, outcome exactly specified
• Episodic?	No, sequential at the level of actions
• Static?	Yes, Wumpus/Pits don't move
• Discrete?	Yes
• Single-agent?	Yes, Wumpus considered a natural feature

Empirical evaluations: single/multiple configuration

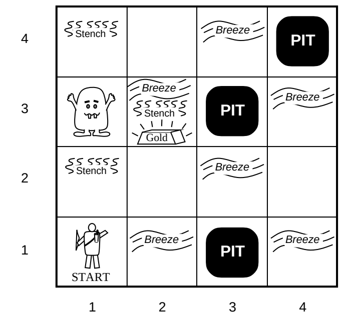
An agent can do well in a single environment: learns the environment, executes rules.

Agent must be tested in a complete class of environments and its average performance must be determined → empirical experiments

- Constraints: start from position [1,1], limited to 4×4 grid
- Location of Wumpus and Gold chosen randomly with a uniform distribution (all squares are possible except [1,1])
- Each square, except [1,1], can be a pit with probability 0.2
- Terribly bad cases: gold in a pit or surrounded by pits

Wumpus World: Acting & Reasoning

- After receiving initial percepts, agent knows it is in [1,1] and it is OK
- No stench or breeze in [1,1] $\Rightarrow$ [1,2] and [2,1] are danger-free
- Cautious agent moves only to square it knows it is OK
- Agent moves only to square [2,1], detects breeze y $\Rightarrow \exists$ a pit in neighboring squares [1,1], [2,2] and [3,1]. Agent knows no pit in [1,1] $\rightarrow$ Pit indicated in [2,2] and [3,1] with `P?`
- Not visited OK squares? Only [1,2]. Agent goes to [1,1], proceeds to [1,2]



Wumpus World: Acting & Reasoning

1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
1,2 **OK**	2,2	3,2	4,2
1,1 $\boxed{\text{A}}$ **OK**	2,1 **OK**	3,1	4,1

(a)

- $\boxed{\text{A}}$ = *Agent*
- **B** = *Breeze*
- **G** = *Glitter, Gold*
- **OK** = *Safe square*
- **P** = *Pit*
- **S** = *Stench*
- **V** = *Visited*
- **W** = *Wumpus*

1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
1,2 **OK**	2,2 **P?**	3,2	4,2
1,1 **V** **OK**	2,1 $\boxed{\text{A}}$ **B** **OK**	3,1 **P?**	4,1

(b)

Wumpus World: Acting & Reasoning

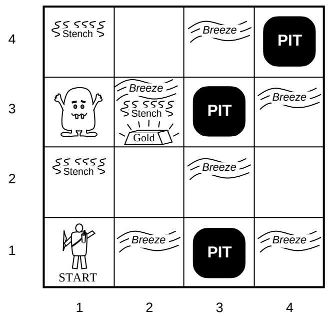
- Agents detects stench in [1,2] $\Rightarrow$ Wumpus nearby!
  Possibilities: [1,1], [1,3] or [2,2].
  Agent knows [1,1] is Wumpus-free (Agent was there!)
  Agent can infer [2,2] is Wumpus-free ($\nexists$ stench in [2,1])
  Agent infers Wumpus is in [1,3] (`W!`)

- Lack of breeze in [1,2] $\Rightarrow$ [2,2] is pit-free
  But, $\exists$ a pit in either [2,2] or [3,1] $\Rightarrow$ $\exists$ pit in [3,1] (`P!`)
  Inference combines knowledge gained at different times and places, beyond the abilities of most animals, but Logical Inference can handle this

- Since [2,2] is `OK` and not visited, Agent moves there

- etc.

Wumpus World: Acting & Reasoning



1,4	2,4	3,4	4,4
1,3 **W!**	2,3	3,3	4,3
1,2 $\boxed{\text{A}}$ **S** **OK**	2,2 **OK**	3,2	4,2
1,1 **V** **OK**	2,1 **B** **V** **OK**	3,1 **P!**	4,1

(a)

$\boxed{\text{A}}$ = *Agent*
B = *Breeze*
G = *Glitter, Gold*
OK = *Safe square*
P = *Pit*
S = *Stench*
V = *Visited*
W = *Wumpus*

1,4	2,4 **P?**	3,4	4,4
1,3 **W!**	2,3 $\boxed{\text{A}}$ **S G** **B**	3,3 **P?**	4,3
1,2 **S** **V** **OK**	2,2 **V** **OK**	3,2	4,2
1,1 **V** **OK**	2,1 **B** **V** **OK**	3,1 **P!**	4,1

(b)

The point of the Wumpus world

In each case where the agent draws a conclusion from the available information, that conclusions is guaranteed to be correct if the available information is correct.

$\longrightarrow$ Fundamental property of logical reasoning.

Logic in general

Logics are formal languages for representing information such that conclusions can be drawn

Syntax defines the sentences in the language (grammar)

Semantics define the "meaning" of sentences; *i.e.*, define truth of a sentence in a world

Example: the language of arithmetic

- Syntax: $x + 2 \geq y$ is a sentence; $x2 + y >$ is not a sentence
- Semantics:
  – $x + 2 \geq y$ is true iff the number $x + 2$ is no less than the number y
  – $x + 2 \geq y$ is true in a world where $x = 7,\ y = 1$
  – $x + 2 \geq y$ is false in a world where $x = 0,\ y = 6$

Types of logic

Logics are characterized by what they commit to as "primitives"

Ontological commitment :

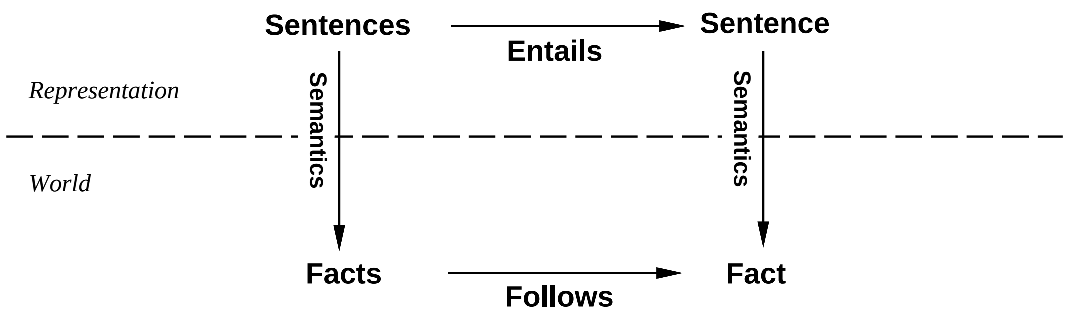
what exists—facts? objects? time? beliefs?

Epistemological commitment :

what states of knowledge?

Language	Ontological Commitment (What exists in the world)	Epistemological Commitment (What an agent believes about facts)
Propositional logic	facts	true/false/unknown
First-order logic	facts, objects, relations	true/false/unknown
Temporal logic	facts, objects, relations, times	true/false/unknown
Probability theory	facts	degree of belief 0…1
Fuzzy logic	degree of truth	degree of belief 0…1

Knowledge representation & reasoning



Facts: in the world

Representations: in the computer

Reasoning: process of constructing new representations from old ones

Proper Reasoning: ensures new representations correspond to facts that actually follow from facts in the world

Entailment

Entailment means that one thing follows from another:

$(\text{KB} \models \alpha)$

Knowledge base KB entails sentence α

iff α is true in all worlds where KB is true

Example: KB: $\{a \wedge b\}$, then

KB $\models a$; KB $\models b$; KB $\models a \vee b$

Entailment is a relationship between sentences (i.e., syntax) that is based on semantics

$(\alpha \models \beta)$: the truth of β contains the truth of α

For example: (x+y=4) $\models$ (4=x+y)

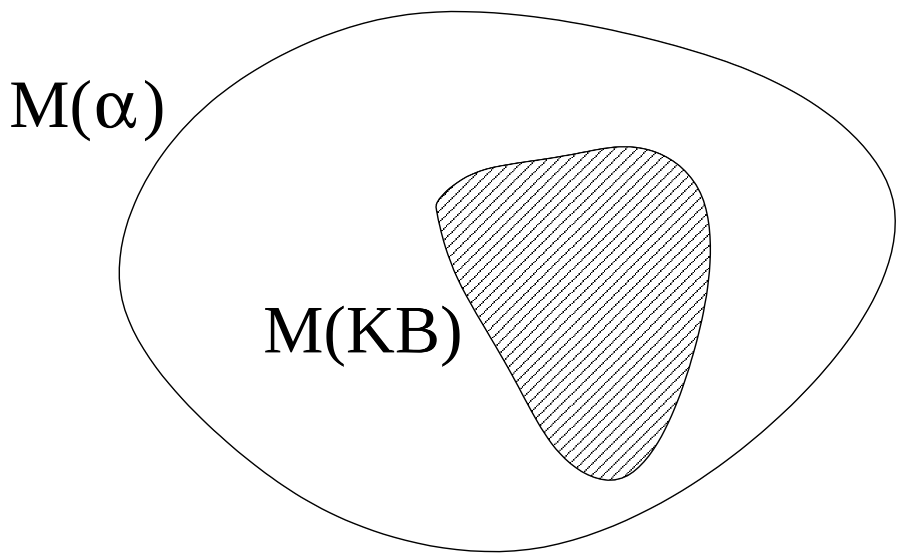
Models

Logicians typically think in terms of **models**, which are formally structured worlds with respect to which truth can be evaluated

We say m **is a model of** a sentence α if α is true in m

$M(\alpha)$ is the set of all models of α

Then $KB \models \alpha$ if and only if $M(KB) \subseteq M(\alpha)$



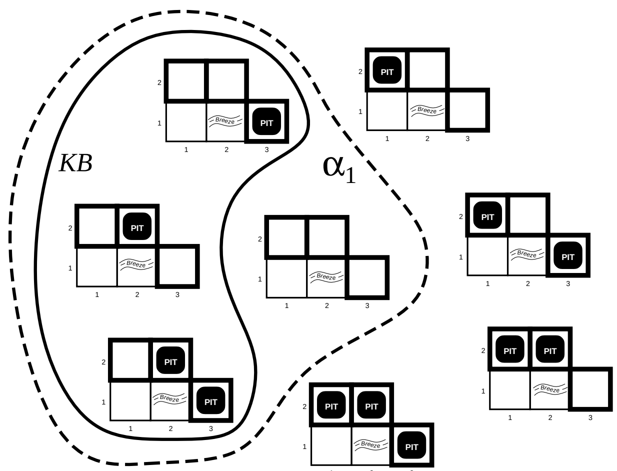
Entailment in the Wumpus world

Situation: Agent detected nothing in [1,1], breeze in [2,1]
2^3=8 possible models

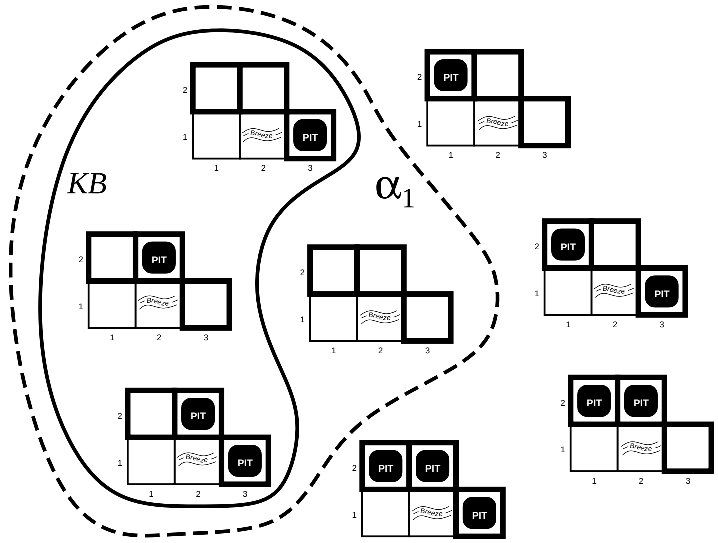
Percepts + the PEAS description = KB

Agent wonders whether pit is in [1,2], [2,2], and [3,1]:
Only 3 models where the KB is true

α_1 = no pit in [1,2]:
α_1 is true in 4 models.



Entailment in the Wumpus world



Consider: α_1 = no pit in [1,2], α_2 = no pit in [2,2]

Model checking: KB $\models \alpha_1$, KB $\not\models \alpha_2$

Given KB, agent cannot conclude whether α_2 holds or not

Entailment can be used to derive conclusions: Inference

Inference here is done by model checking

Inference

$$\text{KB} \vdash_i \alpha \equiv \alpha \text{ is derived from KB by procedure } i$$

Consequences of KB are a haystack; α is a needle.
Entailment = needle in haystack; inference = finding it

Soundness: i is sound if
whenever KB $\vdash_i \alpha$, it is also true that KB $\models \alpha$

Completeness: i is complete if
whenever KB $\models \alpha$, it is also true that KB $\vdash_i \alpha$
That is, the procedure will answer any question whose answer follows from what is known by the KB

The record of operation of a sound inference procedure is a **<u>proof</u>**

Next, propositional logic: syntax, semantics, and inference