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Title: Solving Problems by Searching AIMA: Chapter 3 (Sections 3.4, 3.5, and 3.6)

> Introduction to Artificial Intelligence CSCE 476-876, Spring 2009 URL: www.cse.unl.edu/~choueiry/S09-476-876

Berthe Y. Choueiry (Shu-we-ri) choueiry@cse.unl.edu, (402)472-5444 **function** GENERAL-SEARCH(*problem*, *strategy*) **returns** a solution, or failure initialize the search tree using the initial state of *problem*

loop do

if there are no candidates for expansion then return failurechoose a leaf node for expansion according to *strategy*if the node contains a goal state then return the corresponding solution

else expand the node and add the resulting nodes to the search tree

end

Essence of search: which node to expand first?

 \longrightarrow search strategy

A strategy is defined by picking the order of node expansion

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Types of Search

Uninformed: use only information available in problem definition

Heuristic: exploits some knowledge of the domain

Uninformed search strategies

- 1. Breadth-first search
- 2. Uniform-cost search
- 3. Depth-first search
- 4. Depth-limited search
- 5. Iterative deepening depth-first search
- 6. Bidirectional search

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Search strategies

Criteria for evaluating search:

- 1. Completeness: does it always find a solution if one exists?
- 2. Time complexity: number of nodes generated/expanded
- 3. Space complexity: maximum number of nodes in memory
- 4. Optimality: does it always find a least-cost solution?

Time/space complexity measured in terms of:

- b: maximum branching factor of the search tree
- d: depth of the least-cost solution
- m: maximum depth of the search space (may be ∞)

Breadth-first search (I)

- \rightarrow Expand root node
- \rightarrow Expand <u>all</u> children of root
- \rightarrow Expand *each* child of root
- \rightarrow Expand successors of each child of root, etc.



 \longrightarrow Expands nodes at depth d before nodes at depth d + 1 \longrightarrow Systematically considers all paths length 1, then length 2, etc. \longrightarrow Implement: put successors at end of queue.. FIFO

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Breadth-first search (3)

 \longrightarrow One solution?

 \longrightarrow Many solutions? Finds shallowest goal first

- 1. Complete? Yes, if b is finite
- 2. Optimal? provided cost increases monotonically with depth, not in general (e.g., actions have same cost)

3. Time?
$$1 + b + b^2 + b^3 + \ldots + b^d + b(b^d - 1) = O(b^{d+1})$$

 $O(b^{d+1}) \begin{cases} \text{branching factor } b \\ \text{depth } d \end{cases}$

4. Space? same, $O(b^{d+1})$, keeps every node in memory, big problem

can easily generate nodes at 10MB/sec so 24hrs = 860GB

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Uniform-cost search (I)

 \longrightarrow Breadth-first does not consider path cost g(x)

 \longrightarrow Uniform-cost expands first lowest-cost node on the fringe

 \longrightarrow Implement: sort queue in decreasing cost order

When $g(x) = \text{Depth}(x) \longrightarrow \text{Breadth-first} \equiv \text{Uniform-cost}$

S O S в 🔘 сÒ Α (15 S А вО АQ cÒ 15 G В S 11 S G в 🗘 ĊΟ A (15 G GO 10 11 (a) (b)

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Uniform-cost search (2)

- 1. Complete? Yes, if $\cos t \ge \epsilon$
- 2. Optimal?

If the cost is a monotonically increasing function When cost is added up along path, an operator's cost?

3. Time?

of nodes with $g \leq \text{cost}$ of optimal solution, $O(b^{\lceil C^*/\epsilon \rceil})$ where C^* is the cost of the optimal solution

4. Space?

of nodes with $g \leq \text{cost}$ of optimal solution, $O(b^{\lceil C^*/\epsilon \rceil})$

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Depth-first search (3)

Time complexity:

We may need to expand all paths, $O(b^m)$

When there are many solutions, DFS may be quicker than BFS When m is big, much larger than d, ∞ (deep, loops), .. troubles

 \longrightarrow Major drawback of DFS: going deep where there is no solution..

Properties:

- 1. Complete? Not in infinite spaces, complete in finite spaces
- 2. Optimal?
- 3. Time? $O(b^m)$ Woow.. terrible if m is much larger than d, but if solutions are dense, may be much faster than breadth-first
- 4. Space? O(bm), linear!

Woow..

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Depth-limited search (I)

→ DFS is going too deep, put a threshold on depth! For instance, 20 cities on map for Romania, any node deeper than 19 is cycling. Don't expand deeper!

 \longrightarrow Implement: nodes at depth l have no successor

Properties:

- 1. Complete?
- 2. Optimal?
- 3. Time? (given l depth limit)
- 4. Space? (given l depth limit)

Problem: how to choose *l*?

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Iterative-deepening search (3) \rightarrow combines benefits of DFS and BFS **Properties**: 1. Time? $(d+1).b^0 + (d).b + (d-1).b^2 + \ldots + 1.b^d = O(b^d)$ 2. Space? O(bd), like DFS 3. Complete? like BFS 4. Optimal? like BFS (if step cost = 1)

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Iterative-deepening search (4)

 $\longrightarrow \text{Some nodes are expanded several times, wasteful?} \\ N(BFS) = b + b^2 + b^3 + \ldots + b^d + (b^{d+1} - d) \\ N(IDS) = (d)b + (d-1)b^2 + \ldots + (1)b^d$

Numerical comparison for b = 10 and d = 5: N(IDS) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450N(BFS) = 10 + 100 + 1,000 + 10,000 + 100,000 + 999,990 = 1,111,100

 \longrightarrow IDS is preferred when search space is large and depth unknown

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Bidirectional search (I)

 \rightarrow Given initial state and the goal state, start search from both ends and meet in the middle



→ Assume same b branching factor, \exists solution at depth d, time: $O(2b^{d/2}) = O(b^{d/2})$ b = 10, d = 6, DFS = 1,111,111 nodes, BDS = 2,222 nodes!

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Bidirectional search (2)

In practice :---(

- Need to define predecessor operators to search backwards If operator are invertible, no problem
- What if ∃ many goals (set state)?
 do as for multiple-state search
- need to check the 2 fringes to see how they match need to check whether any node in one space appears in the other space (use hashing) need to keep all nodes in a half in memory O(b^{d/2})
- What kind of search in each half space?

Summary

Criterion	Breadth-	Uniform-	Depth-	Depth-	Iterative
	First	Cost	First	Limited	Deepening
Complete?	Yes*	Yes^*	No	Yes, if $l \ge d$	Yes
Time	b^{d+1}	$b^{\lceil C^*/\epsilon \rceil}$	b^m	b^l	b^d
Space	b^{d+1}	$b^{\lceil C^*/\epsilon \rceil}$	bm	bl	bd
Optimal?	Yes^*	Yes^*	No	No	Yes

b branching factor d solution depth

 \boldsymbol{m} maximum depth of tree

l depth limit

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Loops: Avoid repeated states (I)

Avoid expanding states that have already been visited Valid for both infinite and finite trees $\begin{cases} m \text{ maximum depth} \\ m+1 \text{ states} \\ 2^m \text{ possible branches (paths)} \end{cases}$

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Issues:

- 1. Implementation: hash table, access is constant time Trade-off cost of storing+checking vs. cost of searching
- 2. Losing optimality

when new path is cheaper/shorter of the one stored

3. DFS and IDS now require exponential storage

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Summary

<u>**Path</u></u>: sequence of actions leading from one state to another</u>**

<u>Partial solution</u>: a path from an initial state to another state <u>Search</u>: develop a sets of partial solutions

- Search tree & its components (node, root, leaves, fringe)
- Data structure for a search node
- Search space vs. state space
- Node expansion, queue order
- Search types: uninformed vs. heuristic
- 6 uninformed search strategies
- 4 criteria for evaluating & comparing search strategies

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Searching with partial information (I)

So far, we assumed:

- Environment fully observable
- Environment deterministic
- Agent knows effects of actions

Thus, agent

- always knows where it is
- can compute state where it will be after a sequence of actions

What happens when knowledge about states and actions is incomplete?

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Searching with partial information (2)

Incompleteness yields 3 types of problems:

- Sensorless (conformant) problems
- Contingency problems
- Exploration problems

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Sensorless problems (conformant)

- Environment not observable, no percepts
- Agent does not know in which exact state it is
 - agent may be in one of more possible initial states
 - an action may lead to one or more possible successor states

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Contingency problems

- environment partially observable or actions are uncertain
- agent's percepts provide new input after each action, a contingency to plan for
- Adverserial problems: uncertainty caused by action of other agents

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Exploration problems

- States and actions of the environment are unknown
- Agent must act to discover them
- Extreme case of contingency problem

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Sensorless problems (I)

Vacuum cleaner: no sensors, but agent knows effects of actions

Agent may be in any state $\{1, 2, 3, 4, 5, 6, 7, 8\}$

- [Right] always ends in $\{2, 4, 6, 8\}$
- [Right, Suck] always ends in $\{4, 8\}$
- [Right, Suck, Left, Suck] always works, coerces the world into 7

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Sensorless problems (2)

Environment not (fully) observable:

- Agent must think about sets of states,
- Agent has a belief state (set of possible states)

Environment fully observable: 1 belief state has 1 state Solving sensorless problems: search in space of beliefs

- initial state is a belief state (all possible states)
- actions map 1 belief state into another
- belief state is union of applying action to each state in initial belief state
- goal is reached when all states in belief state are goal states

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Sensorless problems (3)

So far assumed deterministic environment Approach/results hold for nondeterministic environment

Example: Murphy's law, *Suck* sometimes deposits dirt on carpet but only if there is no dirt there already

- [Suck] applied to State 4 leads to $\{2, 4\}$
- [Suck] applied to $\{1, 2, 3, 4, 5, 6, 7, 8\}$ leads to ...
- Problem is unsolvable (Exercise 3.18)!! Agent cannot tell whether state is dirty and cannot predict whether *Suck* is going to make it dirty or clean

Contingency problems (I)

Environment partially observable or actions are uncertain

When agent can get some information:

- about environment
- from sensors
- after acting

Solution to a contingency problem is not a path, but a tree \longrightarrow branches are selected depending on percepts

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Contingency problems (2)

Example: vacuum cleaner

- has 'local dirt' sensor, no 'remote dirt' sensor
- has location sensor
- Murphy's law

Now,

- Agent perceives [L, Dirty], thinks in state $\{1, 3\}$
- Action [Suck] leads to $\{5, 7\}$
- Action [Suck, Right] leads to $\{6, 8\}$
- Action [Suck, Right, Suck] leads to {8, 6} Plan can succeed (8), or fail (6)

Thus, action [Suck, Right, if[R, Dirty]thenSuck] leads to $\{8, 6\}$ Solution is a tree

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Contingency problems (3)

Example: vacuum cleaner

- has 'local dirt' sensor and 'remote dirt' sensor
- has location sensor (fully observable)
- Murphy's law

Solution is a sequence of actions

Agent can proceed...

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Contingency problems (4)

In general, agent

• acts before having a guaranteed plan (solution is a tree)

• needs to consider every possibility that might arise \longrightarrow may be an overkill

It is (sometimes) necessary to start acting, and deal with contingencies as they arise

- \longrightarrow Interleave Search and Execution
- \longrightarrow Useful for game playing and exploration problems

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