







Logic

B.Y. Choueiry

Instructor's notes #13 April 2, 2010 Attracts: mathematicians, philosophers and AI people

Advantages:

— allows to represent the world and reason about it

— expresses anything that can be programmed

Non-committal to:

(e.g., King(Gustave), King(Sweden, Gustave), Merciless(King))

- classes, categories, time, events, uncertainty

.. but amenable to extensions: OO FOL, temporal logics, situation/event calculus, modal logic, etc.

 \longrightarrow Some people think FOL *is* the language of AI true/false? donno :—(but it will remain around for some time..















Existential quantification

 $\exists \langle variables \rangle \langle sentence \rangle$

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. . .

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Instructor's notes #13 April 2, 2010 **Example**: some student will talk at the TechFair $\exists xStudent(x) \land TalksAtTechFair(x)$ Pat, Leslie, Chris are students

 $\exists x P$ is equivalent to the disjunction of <u>instantiations</u> of P

 $Student(Pat) \land TalksAtTechFair(Pat)$

 \lor Student(Leslie) \land TalksAtTechFair(Leslie)

 \lor Student(Chris) \land TalksAtTechFair(Chris)

Typically: \wedge is the main connective with \exists **Common mistake**: using \Rightarrow as the main connective with \exists $\exists x Student(x) \Rightarrow TalksAtTechFair(x)$ is true if there is anyone who is not Student







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Tricky example

Someone is loved by everyone

 $\exists \, x \; \forall \, y \; Loves(y,x)$

Someone with red-hair is loved by everyone $\exists x \forall y \ Redhair(x) \land Loves(y, x)$

Alternatively:

 $\exists x \ Person(x) \land Redhair(x) \land (\forall y \ Person(y) \Rightarrow Loves(y, x))$

Equality

 $term_1 = term_2$ is true under a given interpretation if and only if $term_1$ and $term_2$ refer to the same object

Examples

- Father(John)=Henry
- 1 = 2 is satisfiable
- 2 = 2 is valid
 - Useful to distinguish two objects:
 - Definition of (full) Sibling in terms of Parent:
 - $\forall x, y \; Sibling(x, y) \Leftrightarrow [\neg (x = y) \land \exists m, f \neg (m =$
 - $f) \land Parent(m, x) \land Parent(f, x) \land Parent(m, y) \land Parent(f, y)]$
 - Spot has at least two sisters: ...

AIMA, Exercise 8.4 & 8.7

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Prepare for next lecture: AIMA, Exercise 8.24, page 319 Takes(x, c, s): student x takes course c in semester s Passes(x, c, s): student x passes course c in semester s Score(x, c, s): the score obtained by student x in course c in semester s x > y: x is greater that y F and G: specific French and Greek courses Buys(x, y, z): x buys y from z Sells(x, y, z): x sells y from z 28 Shaves(x, y): person x shaves person y Born(x, c): person x is born in country c Parent(x, y): person x is parent of person y $\operatorname{Citizen}(x, c, r)$: person x is citizen of country c for reason r Resident(x, c): person x is resident of country c of person y Fools(x, y, t): person x fools person y at time t Student (x), Person(x), Man(x), Barber(x), Expensive(x), Agent(x), Insured(x), Smart(x), Politician(x),

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AI Limerick

If your thesis is utterly vacuous

Use first-order predicate calculus

With sufficient formality

The sheerest banality

Will be hailed by the critics: "Miraculous!"

Henry Kautz In Canadian Artificial Intelligence, September 1986 (then: University of Rochester then: head of AI at AT&T Labs-Research and Program co-chair of AAAI-2000 Now: Associate Professor at University of Washington, Seattle)

B.Y. Choueiry

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