Spring Semester, 2009 CSCE 421/821: Foundations of Constraint Processing

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Homework 3

Assigned: Monday, Feb 16, 2009

Due: Monday, Feb 23, 2009

Total value: 80 points for undergrads, 90 for grads. Penalty of 10 points for lack of clarity.

Notes: This homework must be done individually. If you receive help from anyone, you must clearly acknowledge it. Always acknowledge sources of information (URL, book, class notes, etc.). Please inform instructor quickly about typos or other errors.

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1 Configuration and Design: Lot development (Total 10 points)

From Nadel (1989) via Dechter

The map in Figure 1 shows eight lots available for development. Five developments are to be located on these lots: a recreation area, an apartment complex, a cluster of 50 single-family houses, a large cemetery, and a dump site. Assume the following information and conditions:

• The recreation area must be near the lake.



Figure 1: Development map.

- Steep slopes must be avoided for all but the recreation area.
- Poor soil must be avoided for developments that involve construction, namely, the apartments and the houses.
- Because it is noisy, the highway must not be near the apartments, the houses or the recreation area.
- The dump site must not be visible from the apartments, the houses, or the lake.
- Lots 3 and 4 have poor soil.
- Lots 3, 4, 7, and 8 are on steep slopes.
- Lots 2, 3, and 4 are near the lake.
- Lots 1 and 2, are near the highway.

Formulate this problem as a CSP. Define the variables, their domains, the constraints and the query. Clearly state any assumptions you make that are not listed above, otherwise

2 Reduction of 3SAT into a CSP (Total 10 points)

1. Formulate 3SAT as a CSP.

(5 points)

Indications: Your formulation should be as general as possible and should represent each of the elements of the 3SAT and its question in the terminology of a CSP. Consider X, the set of Boolean variables of a 3SAT instance. What are the values that a variable can take? Use this to define the variables of the CSP and their values. A clause is a disjunction of literals. How to represent a clause in the CSP formalism? A 3SAT sentence is a conjunction of clauses. How is the sentence represented in the CSP formalism? Finally, state how the question of

3SAT is reduced as a question to the CSP and prove that a solution to 3SAT exists if and only if a solution to the corresponding CSP exists.

- 2. What is the arity of the constraints of the resulting CSP? (1 points)
- 3. As a direct application of your reduction, transform the following 3SAT problem into a CSP. Specify the variables, their domains, define the constraint in extension, and draw the corresponding constraint graph: (2points)

 $(c_1 \lor c_2 \lor c_3) \land (c_2 \lor c_3 \lor c_4) \land (\neg c_1 \lor c_5) \land (c_1 \lor c_4 \lor c_5)$

4. Knowing how a 3SAT clause (which is a disjunction of at most 3 literals) is represented in the CSP, how do you propose to represent a clause of SAT (which has an arbitrary number of literals in the clause)? (points)

3 Conflict Directed Backtracking (CBJ)

The goal of this exercise is to implement and test CBJ.

- Implement CBJ for finding a single solution. 20 points
- Implement CBJ for finding all solutions (see lecture slides pages 26, 27, and 28). 20 points
- Report the results obtained on the examples of Homework 2 for finding both 1 solution and all solutions. 5 points
- Report the results for finding a *single* solution obtained on the CSP instances provided on the wiki page of Homework3. The results should be reported for the four ordering heuristics. 10 points
- Bonus for undergrads mandatory for grads: Report the results for finding a *all* solution obtained on the CSP instances provided on the wiki page of Homework3. The results should be reported for the four ordering heuristics. 10 points
- Your impressions on the results of BT and CBJ. 5 points

General indications 3.1

- Please make sure that you keep your code and protect your files. Your name, date, and course number must appear in each file of code that you submit.
- All programs must be compiled, run and tested on cse.unl.edu. Programs that do not run correctly in this environment will not be accepted.
- You must submit a README file with precise steps on how to compile, run and test your code. Failure to do so may result in no points for the homework.

3.2 Implementation Notes

Please carefully consider the following requirements in your implementation.

3.2.1 Administrative

Implement the mechanism for reducing the backtracking effort 'conflict-directed backtracking' (CBJ). Your procedure should take the parameters specifying the ordering heuristic: LD, degree, <u>or</u> ddr. You are responsible for the static ordering of the variables.

Specify the search algorithm BT or CBJ by passing parameters to the program. You are required to implement the following flags to specify the algorithm and the ordering heuristic:

- $-\mathbf{aBT}$ for backtrack search
- \bullet -aCBJ for conflict directed backtrack search
- -uLX for lexicographical ordering heuristic
- -uLD for least domain ordering heuristic
- -uDEG for degree domain ordering heuristic
- -uDD for domain degree domain ordering heuristic
- -f <filename> for the file of the CSP problem

Notice that exactly one -a, one -u and one -f flags are passed to the program. Failure to follow the specification of the flags above may results in deduction of substantial amount of points.

3.2.2 Datastructures

The additional information required for CBJ may be stored in an array, linked-list, hashtable, etc. Irrespective of the programing language or the libraries of datastructures you are using, for acceptable performance implement operations on the datastructures that take constant time whenever possible. That is, every time you add or remove an element, the cost should be constant whenever possible. Avoid traversing the list for addition or removal of items unless the cost is negligible.