

## What is this about?

Context: You are a senior in college

Problem: You need to register in 4 courses for Fall'2006

Possibilities: Many courses offered in Math, CSE, EE, etc.

Constraints: restrict the choices you can make

- Unary: Courses have prerequisites you have/don't have Courses/instructors you like/dislike
- *Binary:* Courses are scheduled at the same time
- *n-ary:* In CompEng, 4 courses from 5 tracks such as at least 3 tracks are covered

You have choices, but are restricted by constraints

 $\longrightarrow$  Make the right decisions

## Constraint Satisfaction

#### Given

• A set of variables

4 courses at UNL

- For each variable, a set of choices (values)
- A set of constraints that restrict the combinations of values the variables can take at the same time

#### Questions

- Does a solution exist? classical decision problem
- How two or more solutions differ? How to change specific choices without perturbing the solution?
- If there is no solution, what are the sources of conflicts? Which constraints should be retracted?

• etc.

Instructor's notes #8 November 20, 2006

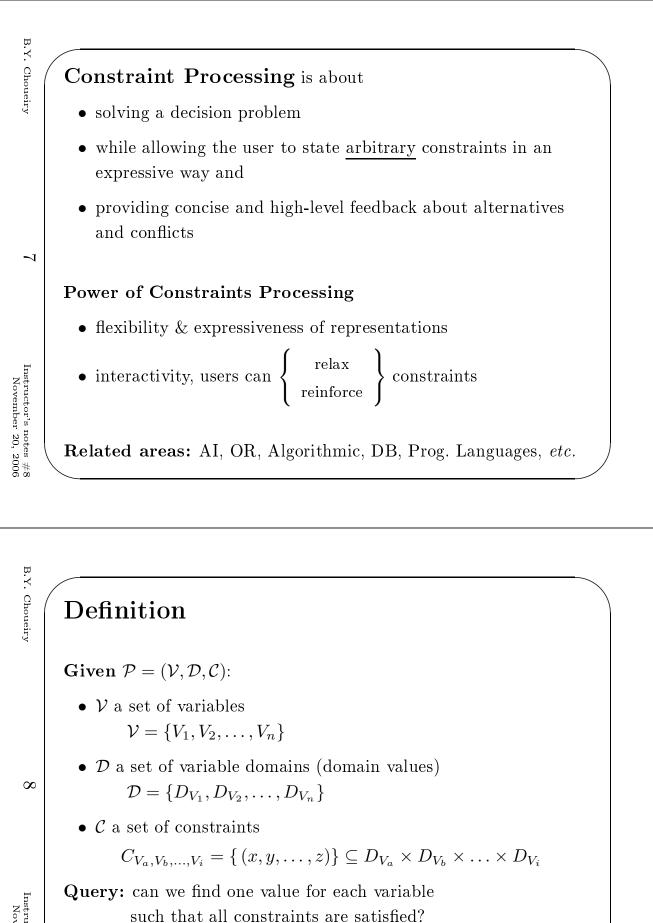
B.Y. Choueiry

6

Instructor's notes #8 November 20, 2006

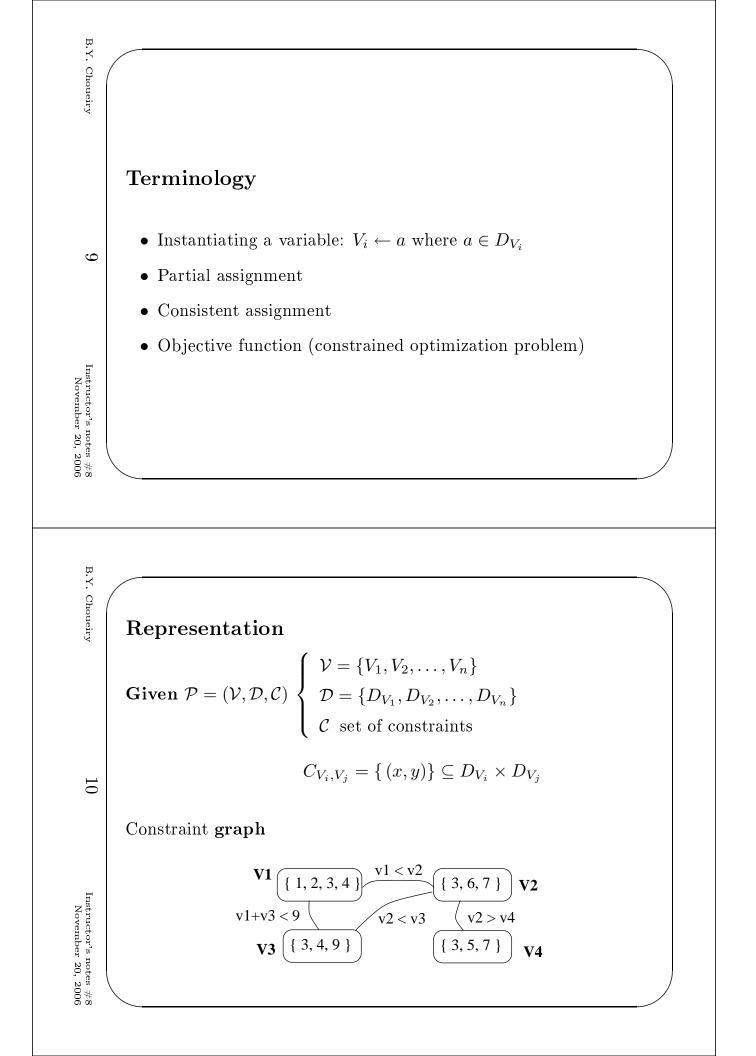
СЛ

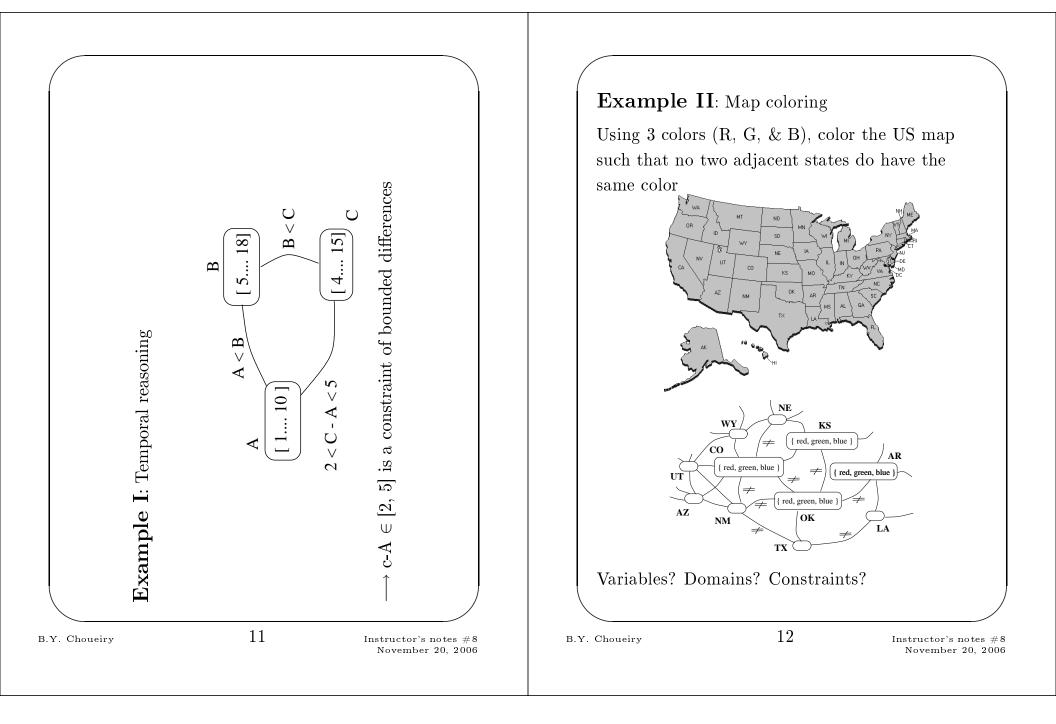
B.Y. Choueiry

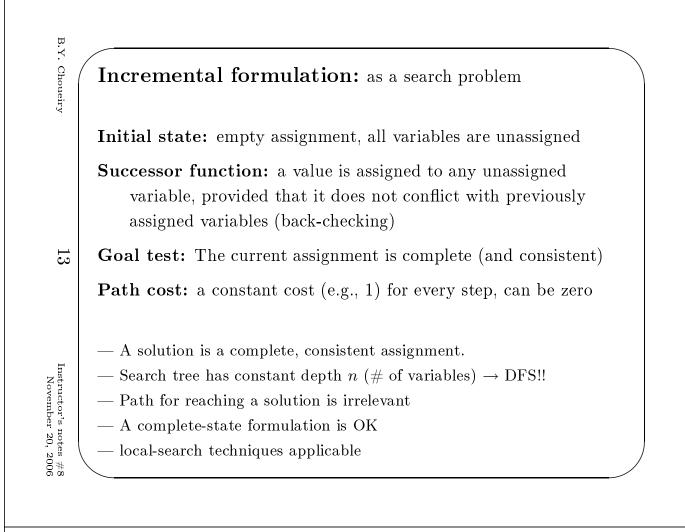


In general, **NP-complete** 

Instructor's notes #8 November 20, 2006







Domain types

$$\mathbf{Given} \ \mathcal{P} = (\mathcal{V}, \mathcal{D}, \mathcal{C}) \begin{cases} \mathcal{V} = \{V_1, V_2, \dots, V_n\} \\ \mathcal{D} = \{D_{V_1}, D_{V_2}, \dots, D_{V_n}\} \\ \mathcal{C} \ \text{set of constraints} \end{cases}$$

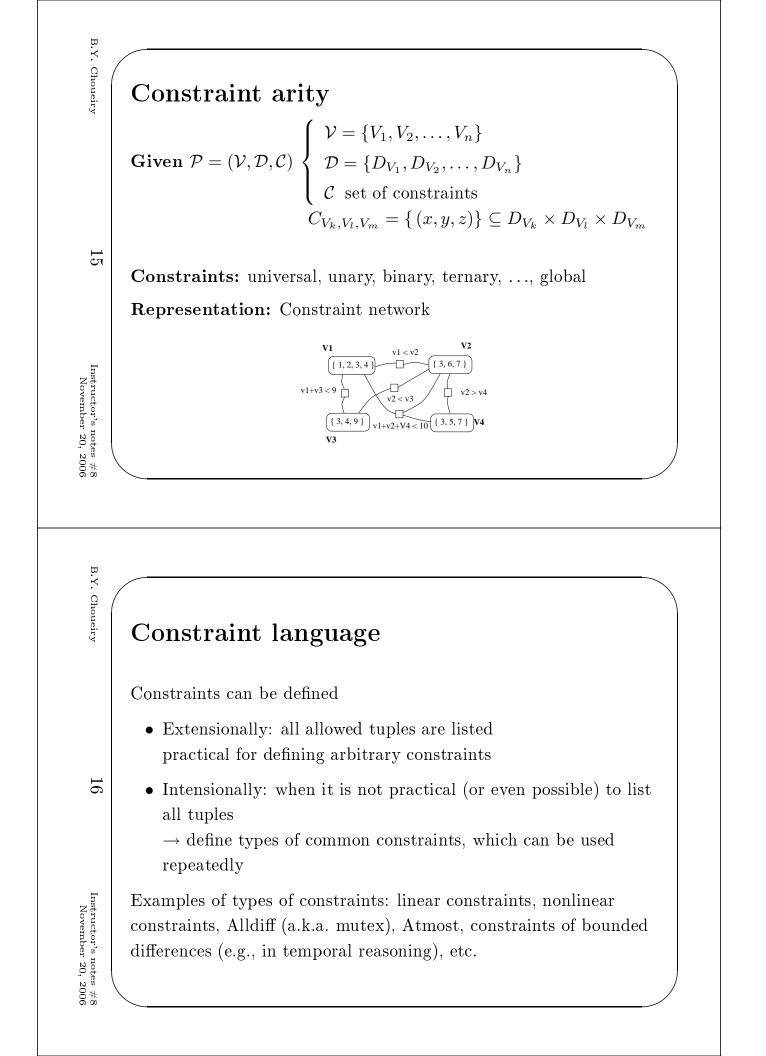
14

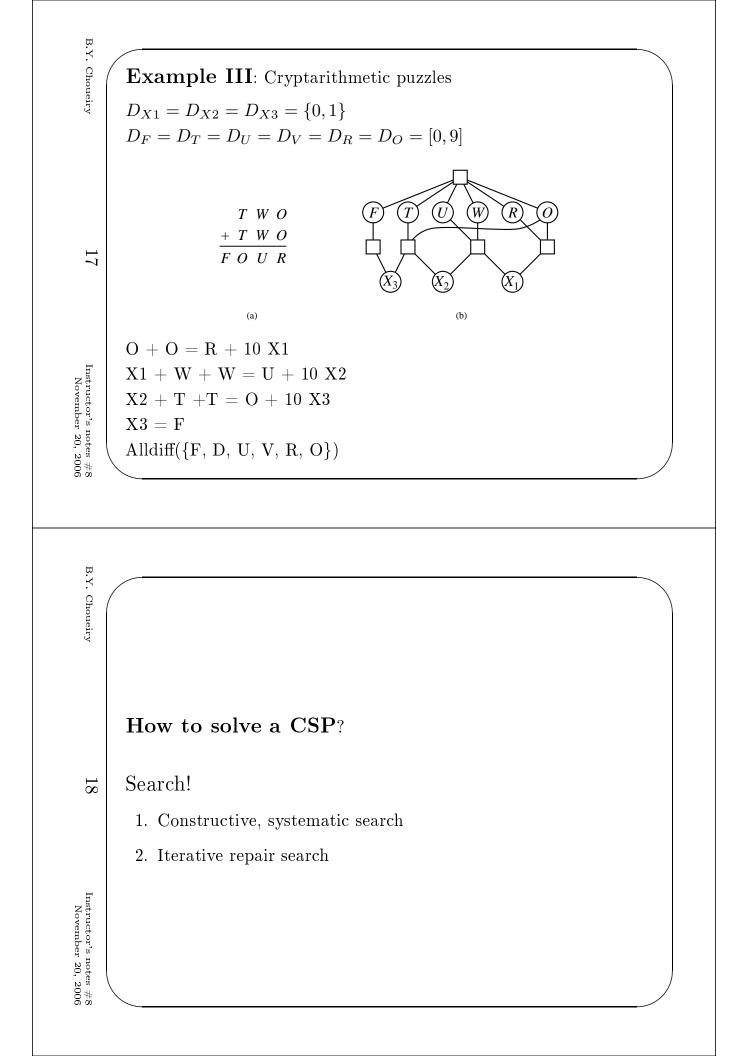
B.Y. Choueiry

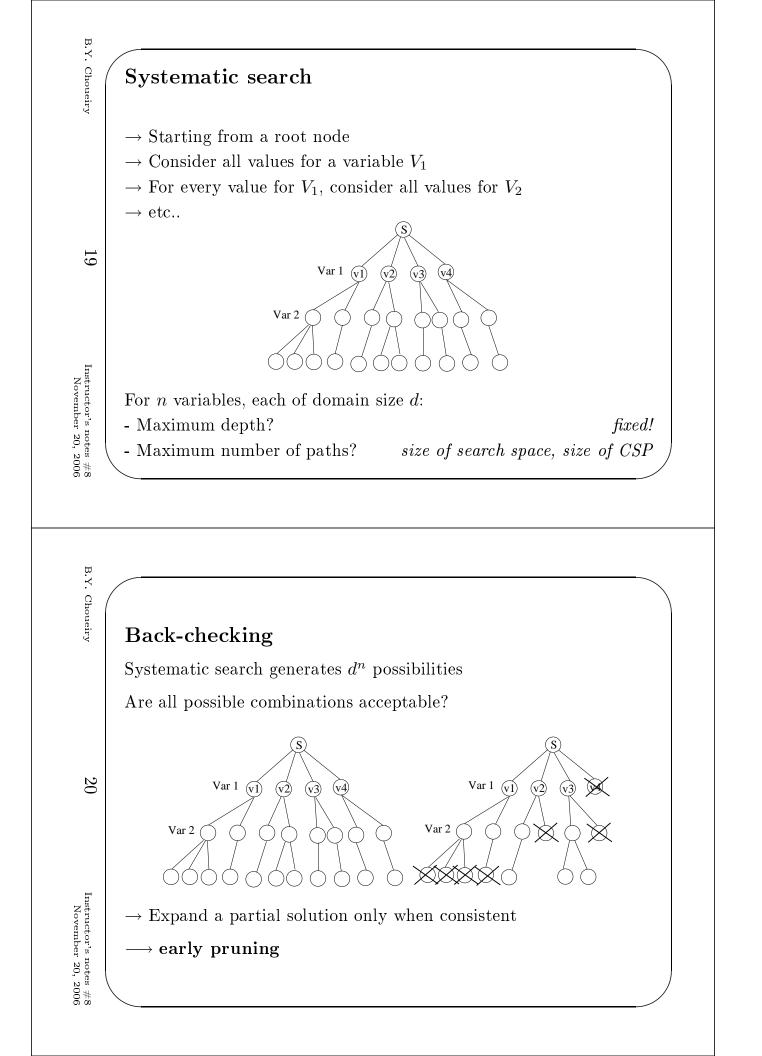
 $C_{V_i,V_j} = \{ (x,y) \} \subseteq D_{V_i} \times D_{V_j}$ 

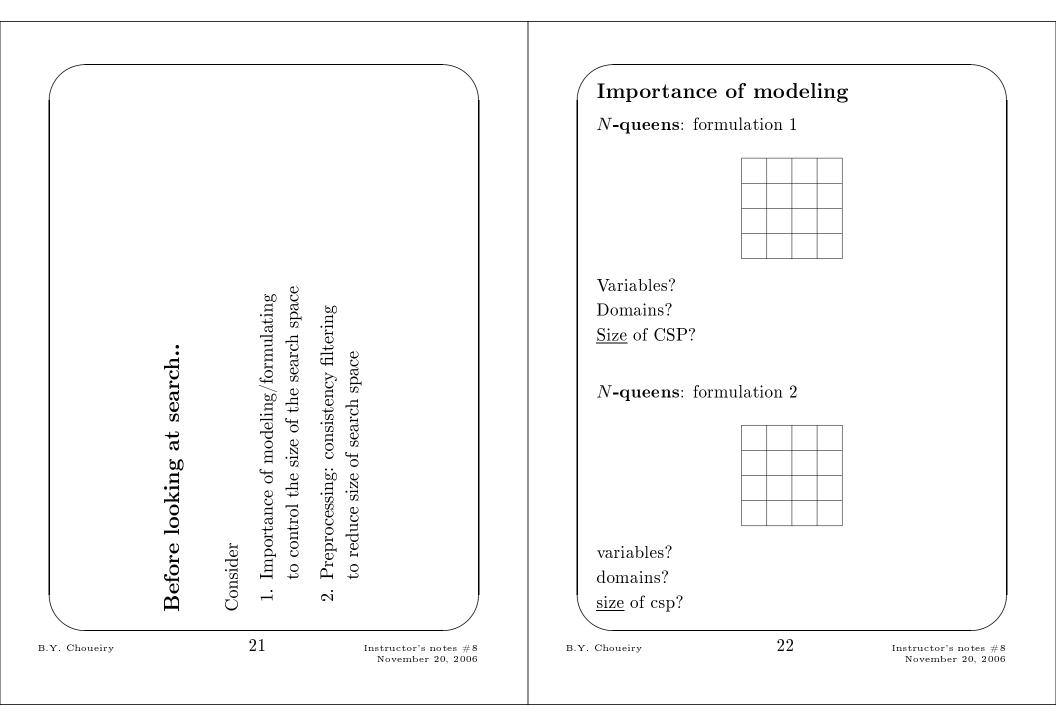
#### **Domains:**

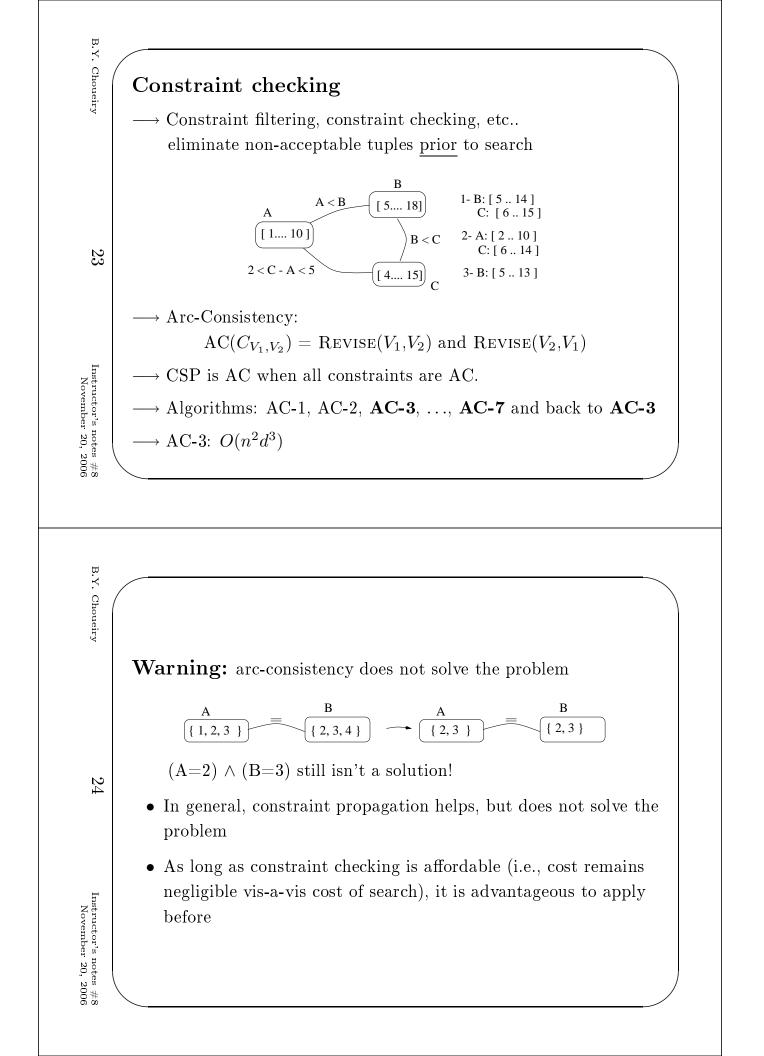
 $\begin{array}{c} \longrightarrow \text{ restricted to } \{0, 1\}: \text{ Boolean CSPs} \\ \longrightarrow \text{ Finite (discrete): enumeration techniques works} \\ \longrightarrow \text{ Continuous: sophisticated algebraic techniques are needed} \\ & \text{ consistency techniques on domain bounds} \end{array}$ 

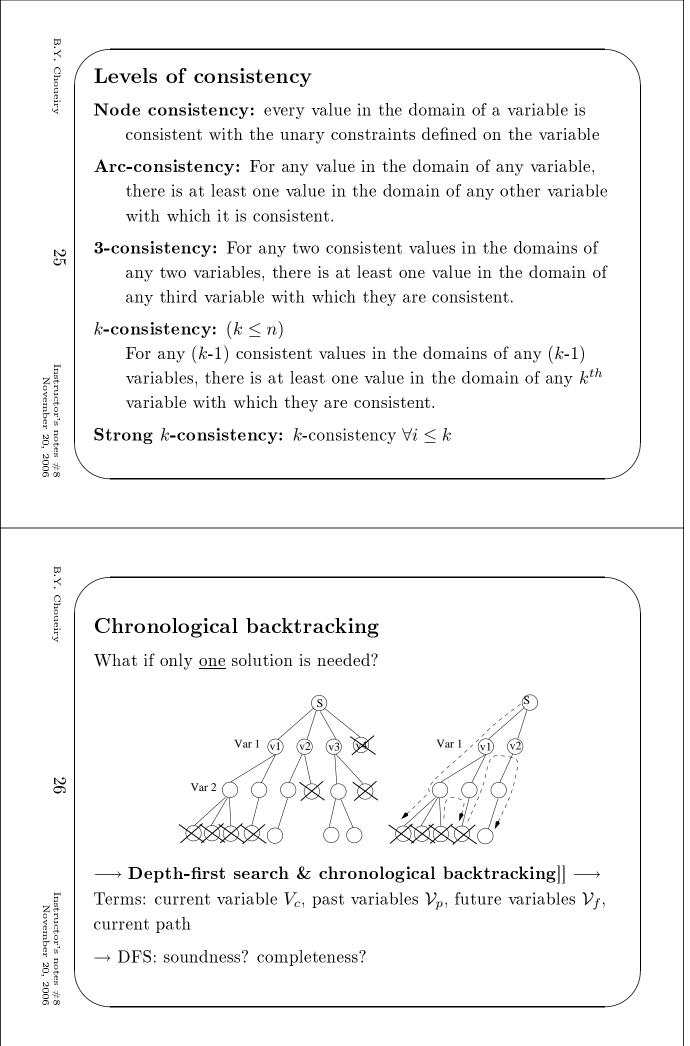


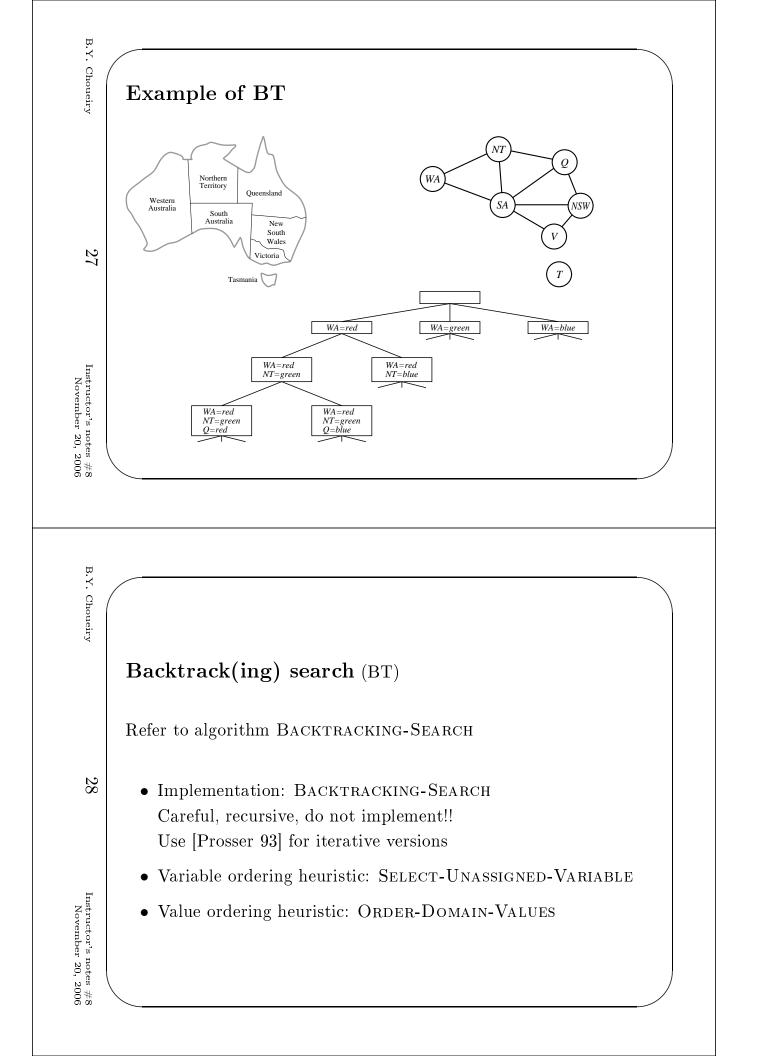


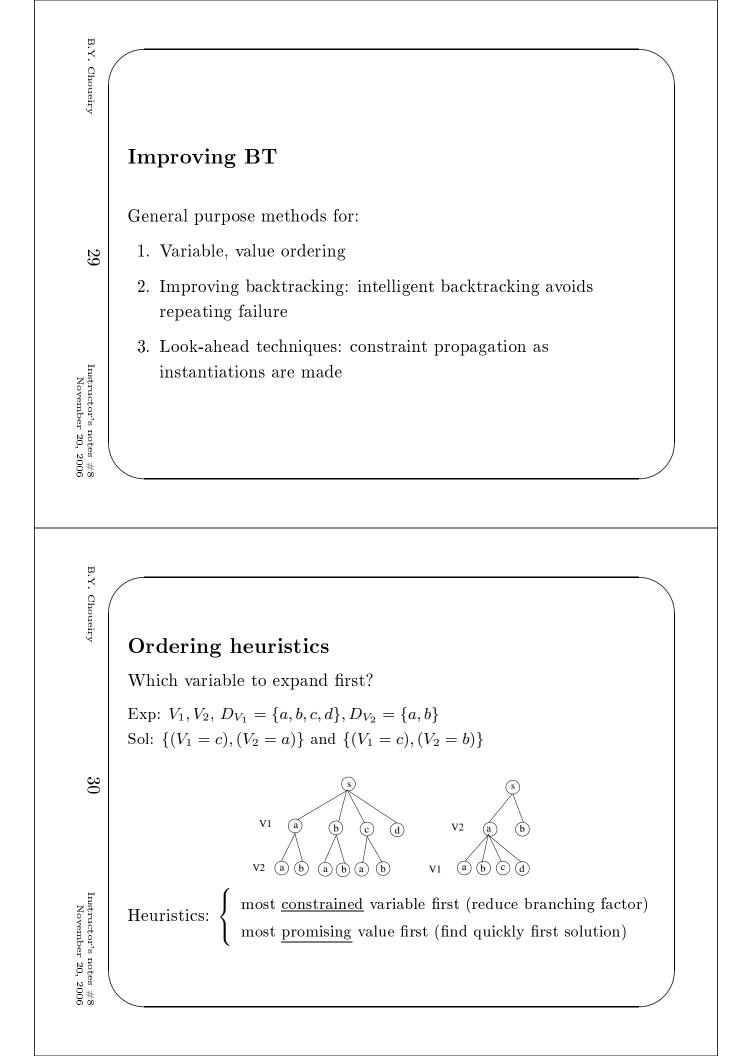


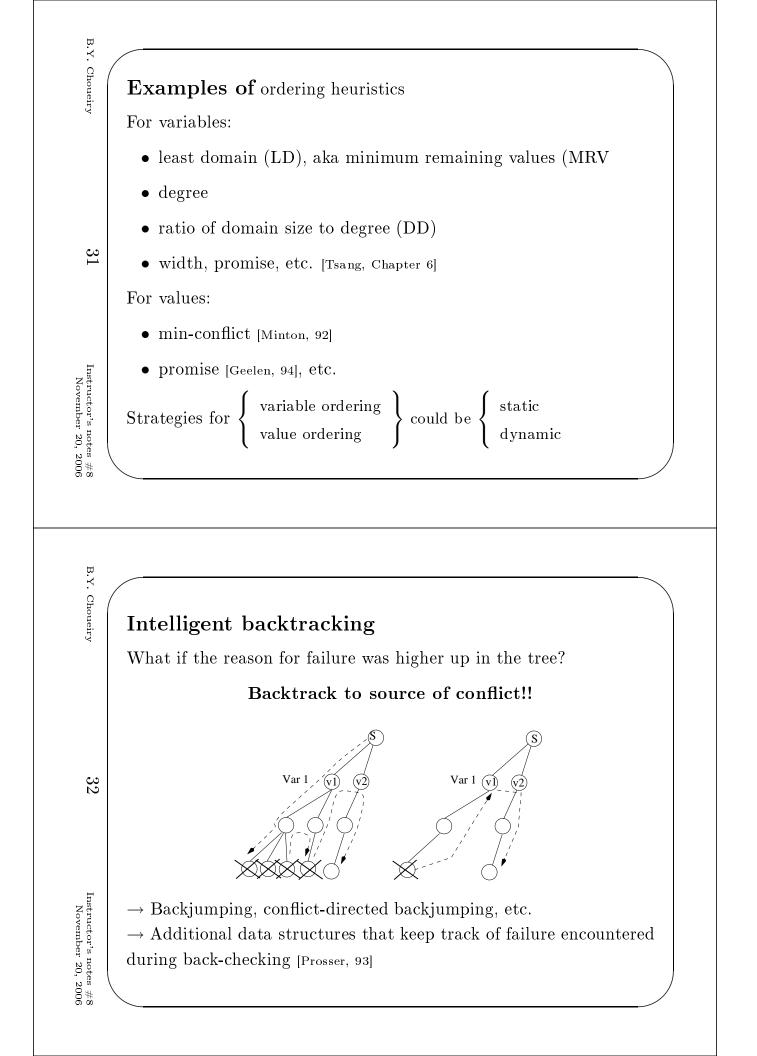


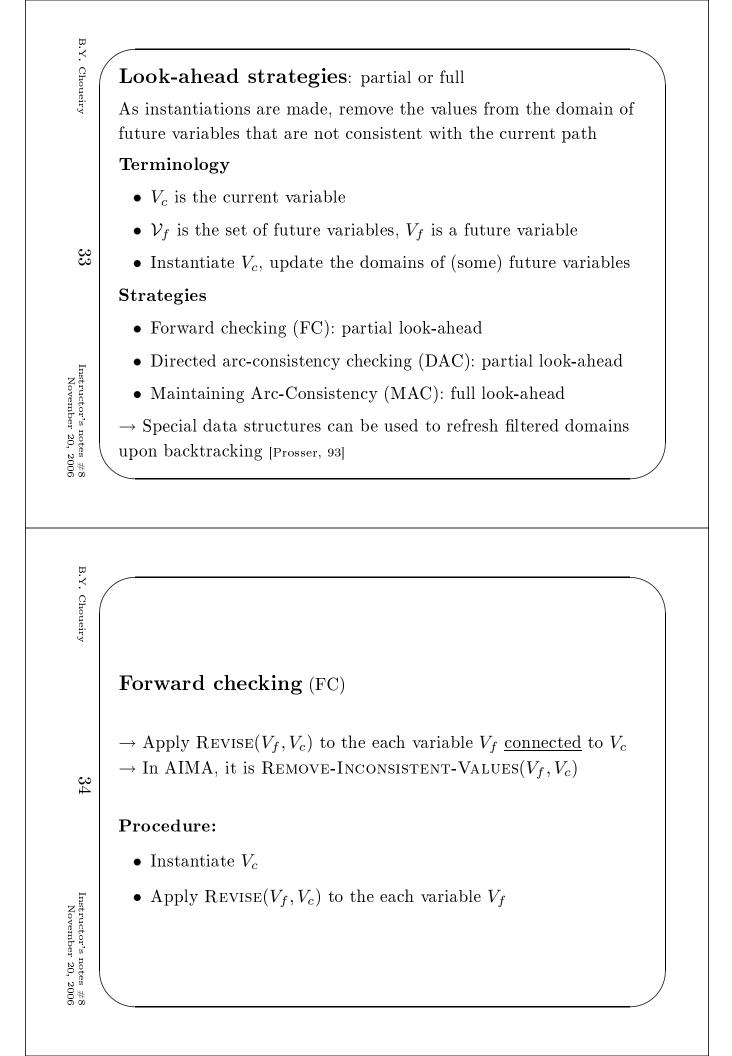


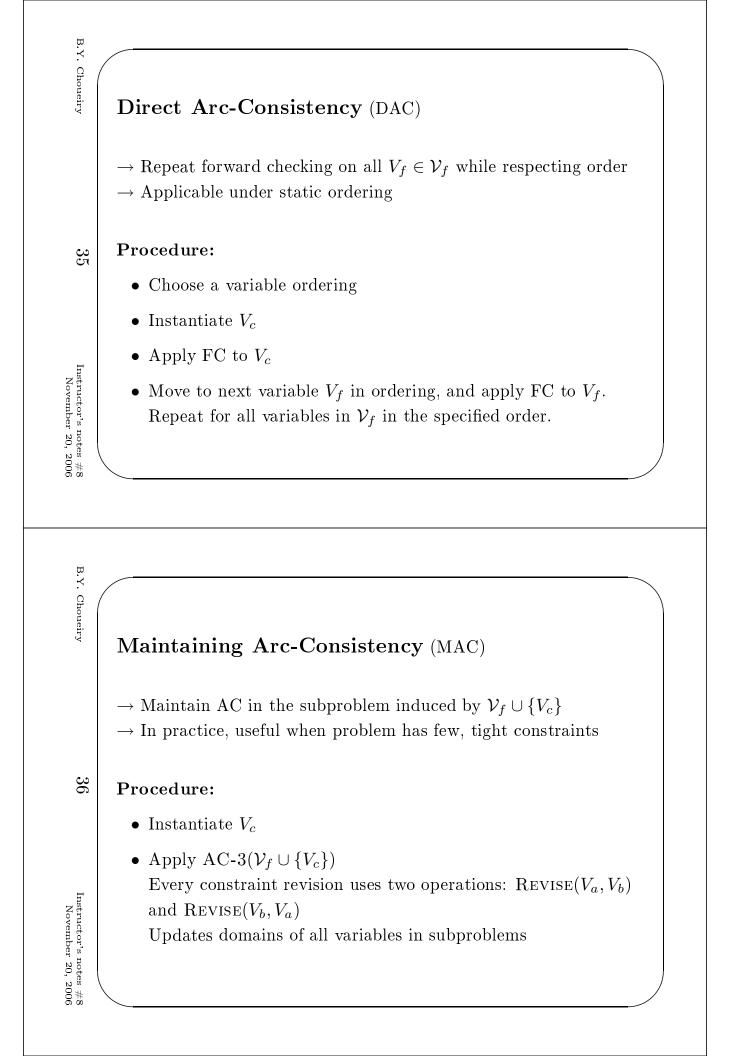


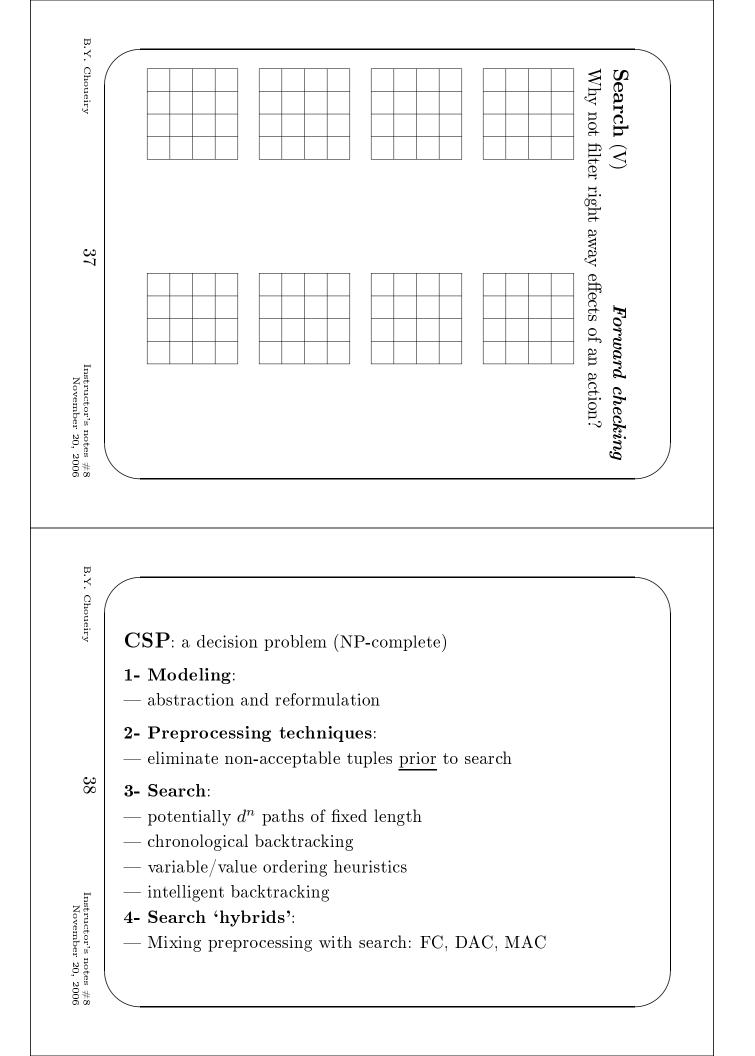


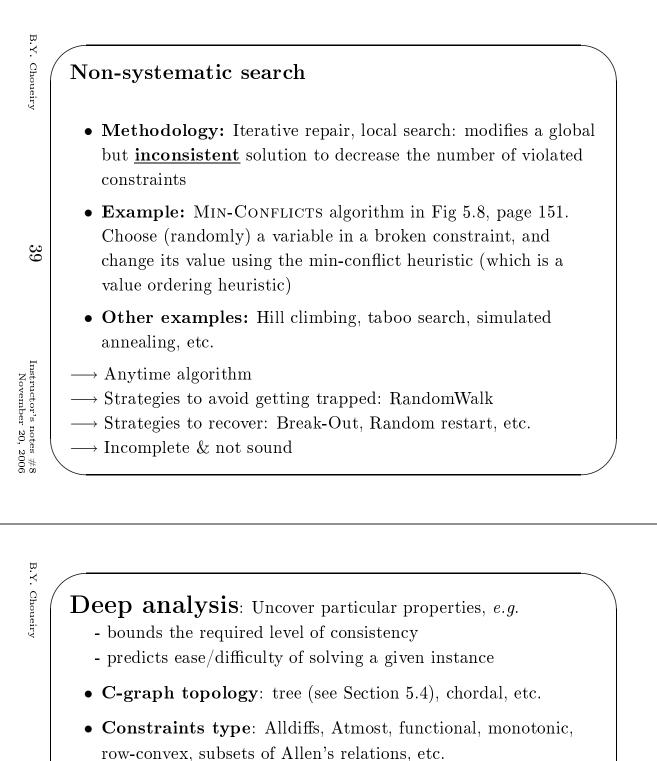








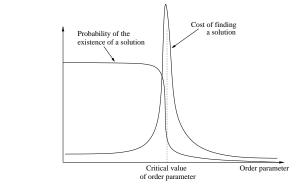


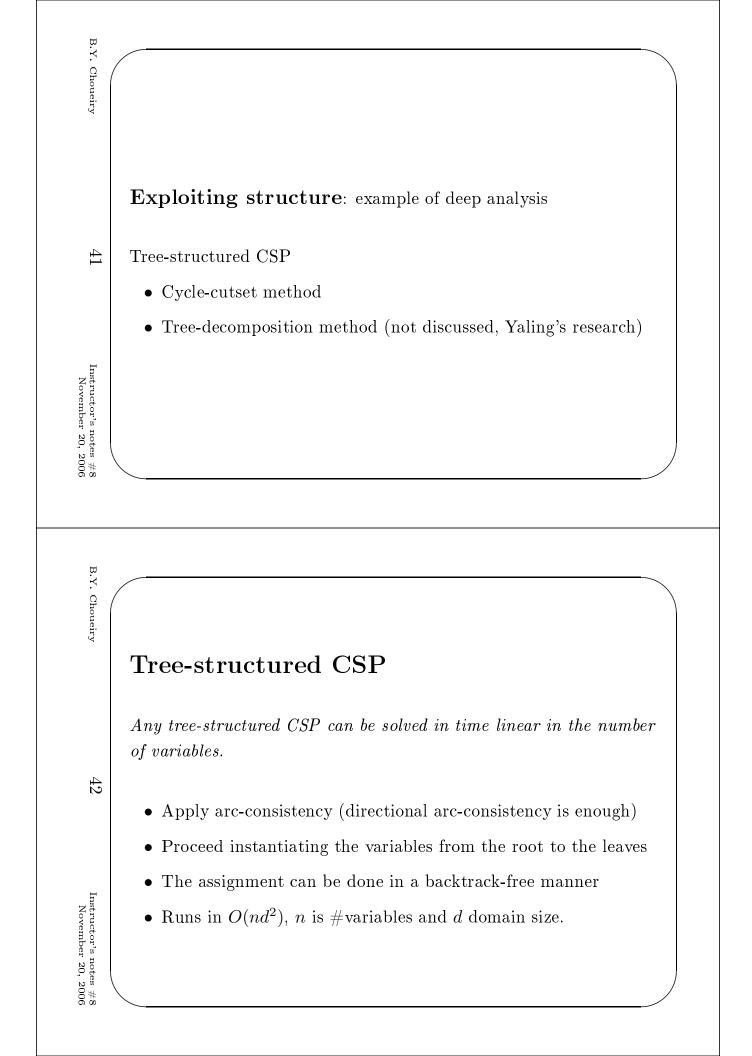


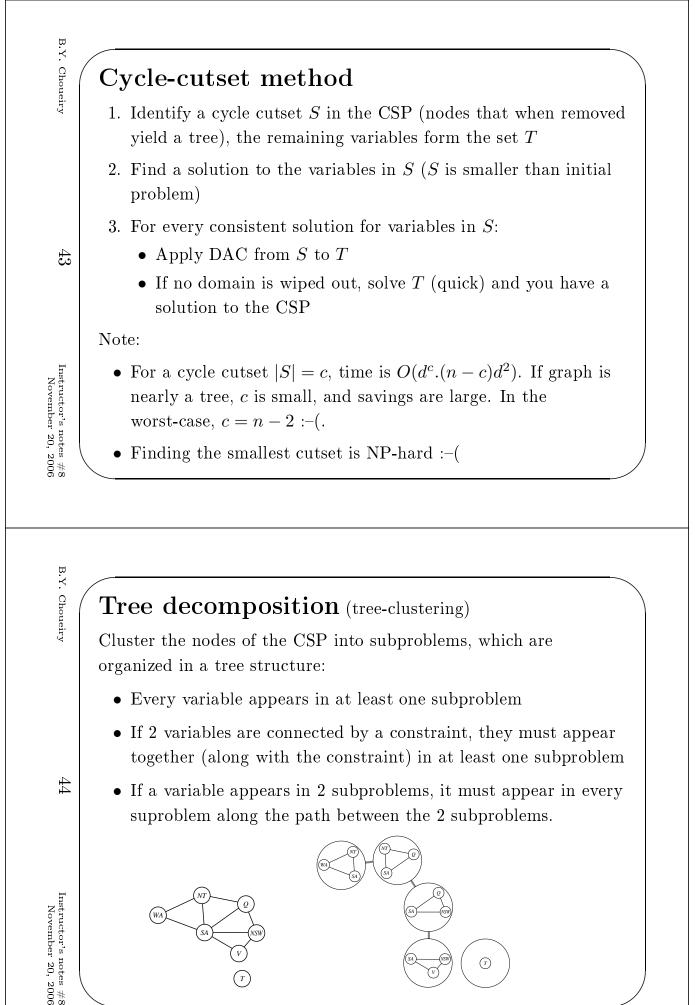
- row-convex, subsets of Allen's relations, o
- Order parameter (phase transition)

40

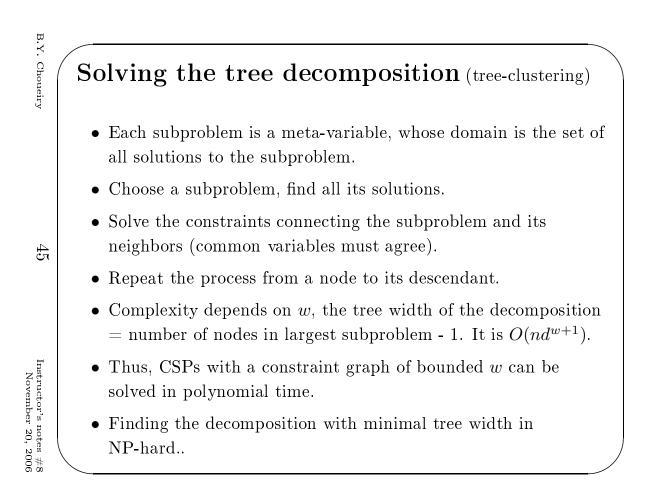
Instructor's notes #8 November 20, 2006







(T)



## **Research** directions

Preceding (*i.e.*, search, backtrack, iterative repair, V/V/ordering, consistency checking, decomposition, symmetries & interchangeability, deep analysis) + ...

#### **Evaluation of algorithms:**

worst-case analysis vs. empirical studies random problems?

#### **Cross-fertilization:**

SAT, DB, mathematical programming, interval mathematics, planning, etc.

### Modeling & Reformulation

#### Multi agents:

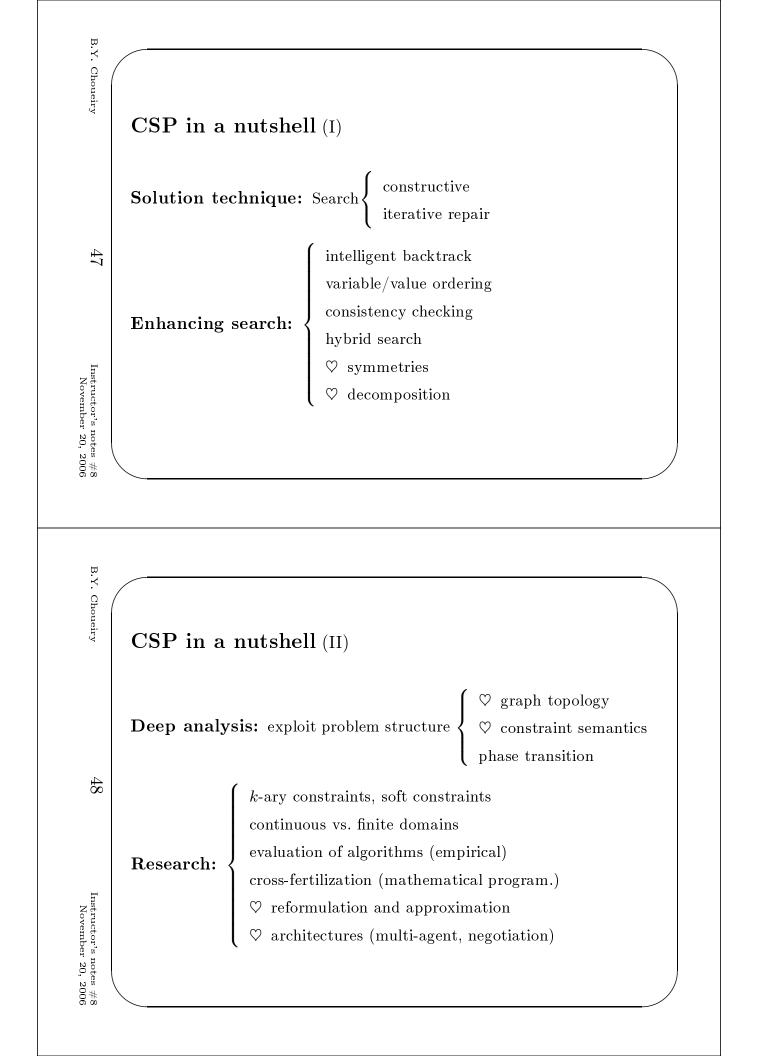
Distribution and negotiation

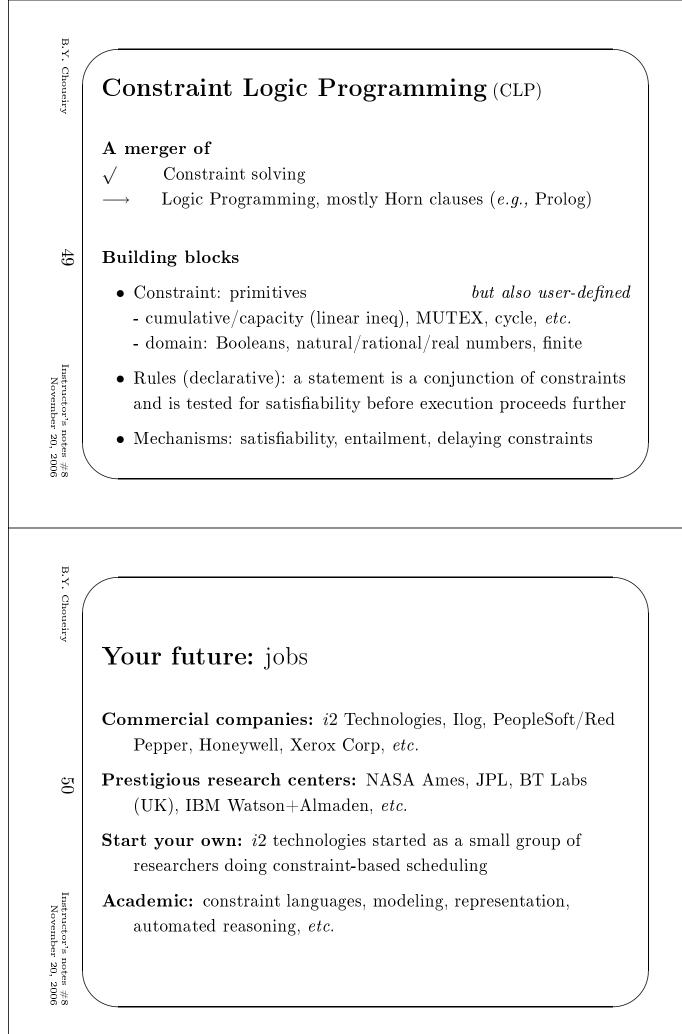
 $\rightarrow$  decomposition & alliance formation

Instructor's notes #8 November 20, 2006

46

B.Y. Choueiry





# Constraint Processing Techniques are the basis of new languages:

Were you to ask me which programming paradigm is likely to gain most in commercial significance over the next 5 years I'd have to pick Constraint Logic Programming (CLP), even though it's perhaps currently one of the least known and understood. That's because CLP has the power to tackle those difficult combinatorial problems encountered for instance in job scheduling, timetabling, and routing which stretch conventional programming techniques beyond their breaking point. Though CLP is still the subject of intensive research, it's already being used by large corporations such as manufacturers Michelin and Dassault, the French railway authority SNCF, airlines Swissair, SAS and Cathay Pacific, and Hong Kong International Terminals, the world's largest privately-owned container terminal.

 $Byte,\ Dick\ Pountain$ 

51

Instructor's notes #8 November 20, 2006

B.Y. Choueiry