

Elementary Data Structures

Chapter 11

CSCE310: Data Structures and Algorithms

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Sets are fundamental in CS

Sets are dynamic structures:

they grow, shrink, change over time

Typical operations:

- insert element
- delete element
- test membership

Objects:

1. key → dynamic set as a set of key values
2. satellite data (unused information)

Two types of operations:

1. Queries: $\text{Search}(S, k)$, $\text{Minimum}(S)$, $\text{Maximum}(S)$,
 $\text{Successor}(S, k)$, $\text{Predecessor}(S, k)$
2. Modifications: $\text{Insert}(S, k)$, $\text{Delete}(S, k)$

Time to execute a set operation generally measured in terms of the
size of the set given as one of its parameters

Dynamic sets as simple data structures using pointers

- Stacks
- Queues
- Linked lists
- Rooted trees
- *etc.*

Assume: you are familiar with arrays

Stack and queues

`Delete(S, k) \equiv Delete(S), deleted element is pre-specified`

In stacks: most recent element entered, LIFO

In queues: oldest element entered, FIFO

Implementation: *e.g.*, array

Stack

Insert operation: Push (S, x)

Delete operation: Pop (S)

Image: spring-loaded stacks of plates in cafeteria

Order popped is reverse of order pushed (LIFO)

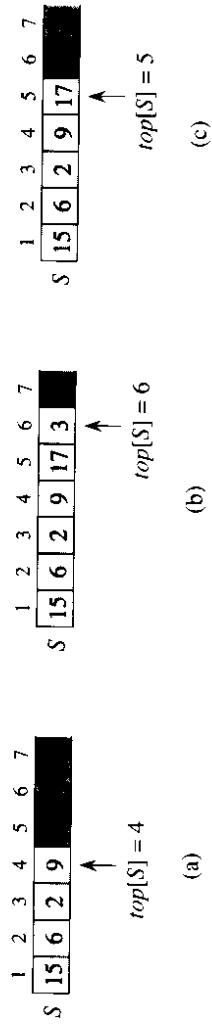


Figure 11.1 An array implementation of a stack S . Stack elements appear only in the lightly shaded positions. (a) Stack S has 4 elements. The top element is 9. (b) Stack S after the calls $PUSH(S, 17)$ and $PUSH(S, 3)$. (c) Stack S after the call $POP(S)$ has returned the element 3, which is the one most recently pushed. Although element 3 still appears in the array, it is no longer in the stack; the top is element 17.

For a stack of n elements (at most): $S[1..n]$

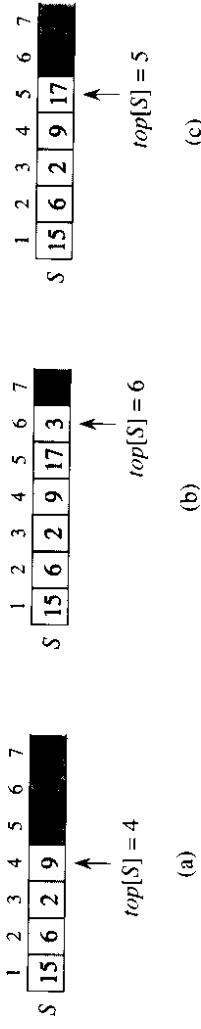


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For a stack of n elements (at most): $S[1..n]$

Attributes of S : top

(remember `length`?)

`top[S]`: index of most recently inserted element

Stacks elements: $S[1.. \text{top}[S]]$

Bottom of stack: $S[1]$

Top of stack: $S[\text{top}[S]]$

Empty stack: $\text{top}[S] = 0$

Test for emptiness: `Stack-empty(S)`

```
STACK-EMPTY( $S$ )
1 if  $top[S] = 0$ 
2 then return TRUE
3 else return FALSE
```

Popping on empty stack: underflow

```
PUSH( $S, x$ )
```

```
1  $top[S] \leftarrow top[S] + 1$ 
2  $S[top[S]] \leftarrow x$ 
```

Pushing on full stack: overflow ($top[S] > n$)

```
POP( $S$ )
1 if STACK-EMPTY( $S$ )
2 then error "underflow"
3 else  $top[S] \leftarrow top[S] - 1$ 
4 return  $S[top[S] + 1]$ 
```

Pseudo-code for Push(Pop) increment (decrement) counter

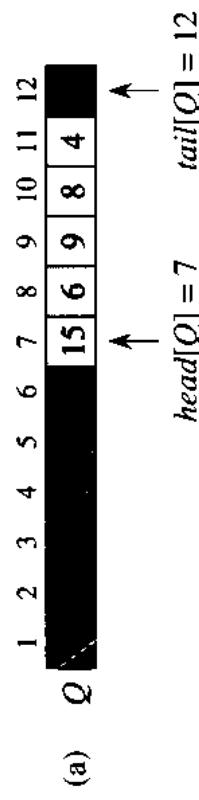
Queues

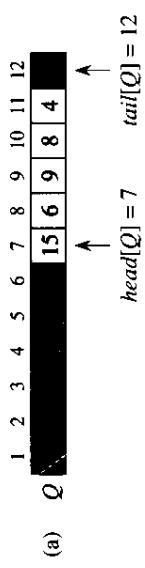
Insert operation: Enqueue (S, x)

Delete operation: Dequeue (S)

Image: line of people at the post office

Order popped is reverse of order pushed (LIFO)



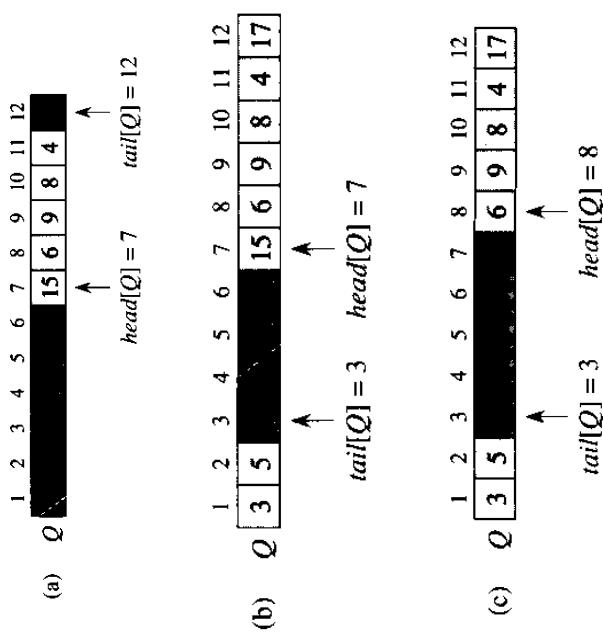


Attributes of S : `head` and `tail`

Enqueued: added at the tail, dequeued: always from head

Elements in queue are in positions:

`head[Q]`, `head[Q] + 1`, ..., `tail[Q] - 1`



Wrap around (circular): position 1 directly follows position n

Empty queue: $\text{head}[Q] = \text{tail}[Q]$

Full queue: $\text{head}[Q] = \text{tail}[Q] + 1$

Initially: $\text{head}[Q] = \text{tail}[Q] = 1$

Dequeue empty list: underflow

```
DEQUEUE( $Q$ )
1  $x \leftarrow Q[\text{head}[Q]]$ 
2 if  $\text{head}[Q] = \text{length}[Q]$ 
3   then  $\text{head}[Q] \leftarrow 1$ 
4 else  $\text{head}[Q] \leftarrow \text{head}[Q] + 1$ 
5 return  $x$ 
```

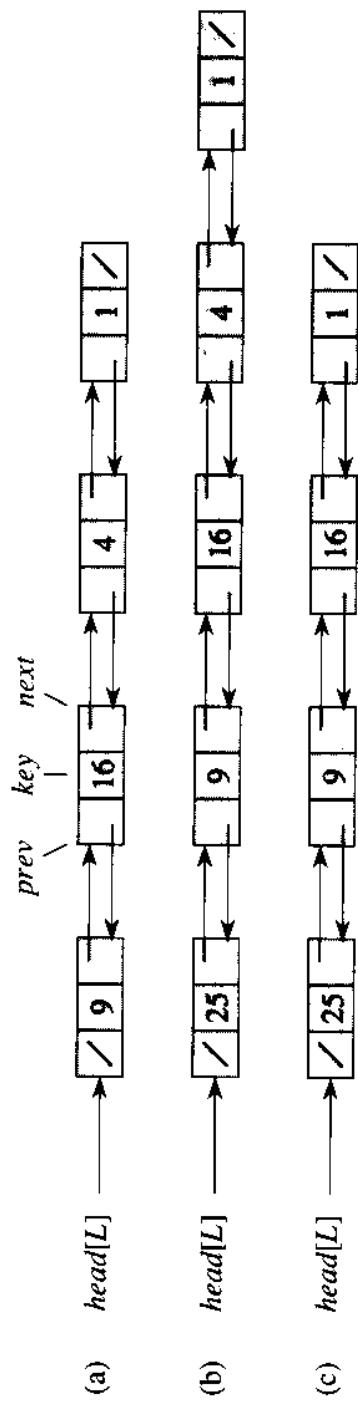
Enqueue full queue: overflow

```
ENQUEUE( $Q, x$ )
1  $Q[\text{tail}[Q]] \leftarrow x$ 
2 if  $\text{tail}[Q] = \text{length}[Q]$ 
3   then  $\text{tail}[Q] \leftarrow 1$ 
4 else  $\text{tail}[Q] \leftarrow \text{tail}[Q] + 1$ 
```

Pseudo-code for Enqueue(Dequeue) increment (decrement) tail
(head)

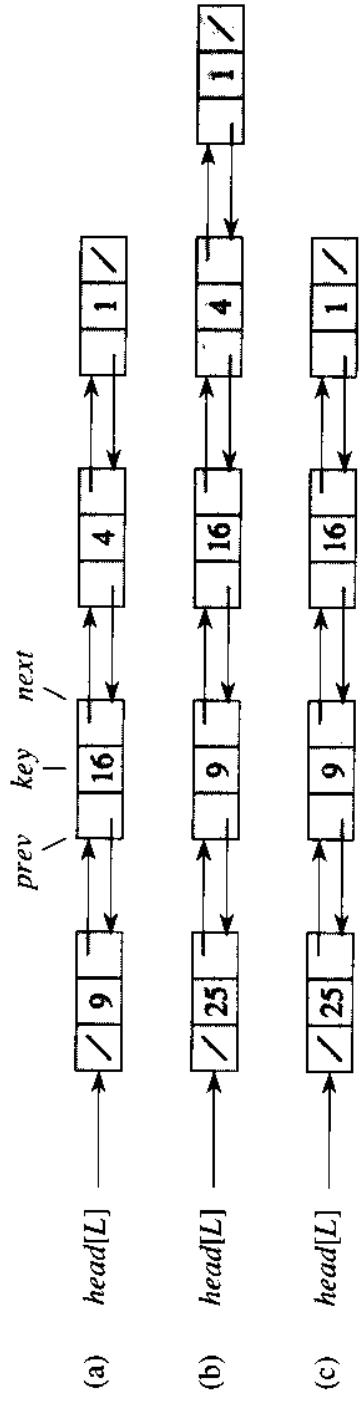
Linked list

Objects arranged in a linear order according to a pointer in each object



Each element x :

- 1 key field
 - 2 pointers fields (`next[x]`, `prev[x]`)

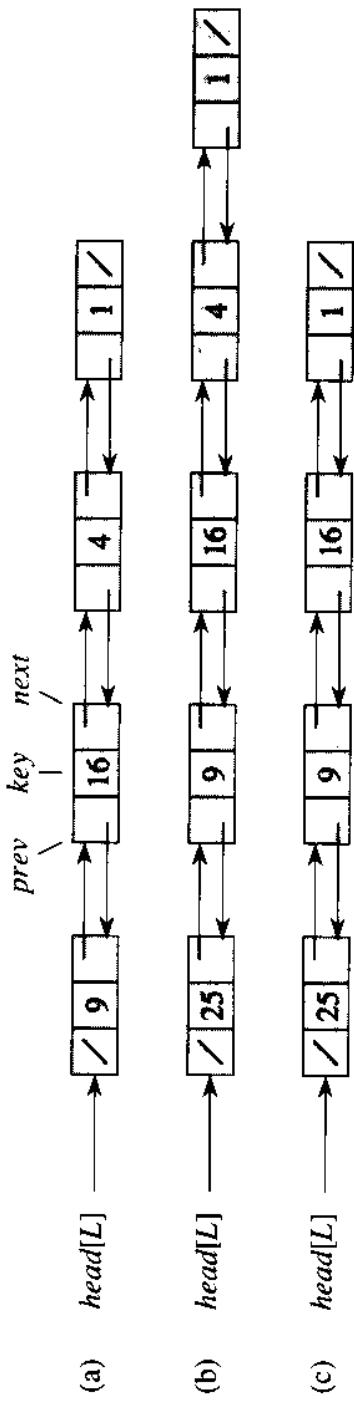


First element, head: $prev[x] = \text{nil}$

Last element, tail: $next[x] = \text{nil}$

Attribute $\text{Head}[L]$ points to first element in list

Empty list: $\text{Head}[L] = \text{nil}$



Simply linked list (no *prev*) vs. doubly linked list

Circular vs. non-circular list

Sorted list (vs. unsorted)

- linear order of items \equiv linear order of keys
- minimum item is head, maximum item is tail

Circular list (ring of elements):
prev of head is tail, and next of tail is head