Week 5 Recitation

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- (3 min max) Go over quiz from last week
- (3 min max) Go over homework from last week.
- Questions about lecture / homework so far?
- 1.6:23) Show that at least 10 of any 64 days chosen must fall on the same day of the week.
 - We proceed with a proof by contradiction.
 - We assume that it is not the case that "at least 10 days of any 64 days chosen fall on the same day of the week."
 - This means that "less than 10 days of any 64 days chosen fall on the same day of the week." Assume, it is 9 days. Then we have "9 days of any 64 days chosen fall on the same day of the week."
 - There are 7 days in a week. If we choose 9 days out of every day of the week, then we have chosen 9×7 days = 63 days, exactly.
 - However, we need to choose 64 days. Therefore, there is one extra day that needs to be chosen. Whichever day we choose, this choice will bump up the 'count' of chosen days to 10, which contradicts the statement "9 days of any 64 days chosen fall on the same day of the week."
 - Therefore, at least 10 of any 64 days chosen must fall on the same day of the week.
- 1.5:15a) All students in this class understand logic. Xavier is a student in this class. Therefore, Xavier understands logic.
 - Define your predicates: Q(x): x is in the class P(x): x understands logic
 - Universe of Discourse: All students
 - Theory: $\forall x P(x) \rightarrow Q(x), P(Xavier)$

- Conclusion: Q(Xavier)
- Proof:
 - StepReason1. $\forall x P(x) \rightarrow Q(x)$ Premise2. $P(Xavier) \rightarrow Q(Xavier)$ Universal instantiation from (1)3. P(Xavier)Premise4. Q(Xavier)Modus ponens from (2) and (3)
- 1.6:27) Prove that for every n a positive integer, n is odd if and only if 5n + 6 is odd.

 \Rightarrow First, we prove: n is odd $\Rightarrow 5n + 6$ is odd)

- 1. $n \text{ is odd} \Rightarrow n = 2k + 1$ by definition
- 2. Plugging in the value of n into 5n + 6, 5n + 6 = 5(2k + 1) + 6 = 10k + 5 + 6 = 10k + 11 = 2(5k + 2) + 1 = 2k' + 1

3. Therefore, 5n + 6 is odd.

 \Leftarrow Next we prove: 5n + 6 odd $\Rightarrow n$ is odd. We use a proof by contrapositive and establish that "n is even $\Rightarrow 5n + 6$ even."

- 1. $n ext{ is even } \Rightarrow n = 2k$ by definition
- 2. Plugging in the value of n into 5n + 6 = 5(2k) + 6 = 10k + 6 = 2(5k + 3) = 2k'
- 3. Therefore, 5n + 6 is even.

Therefore, n is odd iff 5n + 6 is odd.

• (Last 15 minutes) Give quiz