

~~Logical Equivalence Law~~

→ What we have learned in last week?

- ① logical equivalence law.
- ② Propositional functions; arguments; arity: universe of discourse.
- ③ Quantifiers.
- ④ logic programming. Transcribing English to logic

→ Exercises:

1.2. equivalence law:

* Show $(P \vee Q) \rightarrow R \equiv (P \rightarrow R) \wedge (Q \rightarrow R)$

solution:

$$\begin{aligned}
 & (P \vee Q) \rightarrow R && \text{(Given)} \\
 \Rightarrow & \underbrace{(P \vee Q)} \vee R && \text{(implication)} \\
 = & (\neg P \wedge \neg Q) \vee R && \text{(De Morgan)} \\
 = & \underline{R \vee (\neg P \wedge \neg Q)} && \text{(commutative)} \\
 = & (R \vee \neg P) \wedge (R \vee \neg Q) && \text{(Distribution)} \\
 = & (\underbrace{\neg P \vee R}) \wedge (\underbrace{\neg Q \vee R}) && \text{(commutative)} \\
 = & (P \rightarrow R) \wedge (Q \rightarrow R) && \text{(implication)}
 \end{aligned}$$

1.3:10:

Universal Quantifiers

P4)

Let $C(x)$ be the statement "x has a ~~dog~~ ^{cat}"

$D(x)$ be the statement "x has a dog".

define the
range
for x

Express each of these statements in terms of $C(x)$ and $D(x)$.

-a) ^{there is} A student in our class has a cat and a dog:

- we assume that this means that one student has ~~all~~ ~~these~~ both animals:

$$\exists x (C(x) \wedge D(x))$$

-b) all student in our class have a dog or a cat.

- $\forall x (C(x) \vee D(x))$

-d) No student in our class has a cat and a dog.

- This is the negation of part (a):

$$\neg \exists x (C(x) \wedge D(x))$$

- $\exists x (C(x) \wedge \neg D(x))$ → what does this expression mean

- some student in our class has a cat but not a dog.