# Fall Semester, 2005 <br> B.Y. Choueiry <br> CSCE 421/821: Foundations of Constraint Processing 

## Homework 2

Assigned: Tuesday, September 12, 2005
Due: Thursday, September 22, 2005
Total value: 80 points
Notes: This homework must be done individually. If you receive help from anyone, you must clearly acknowledge it. Always acknowledge sources of information (URL, book, class notes, etc.). Please inform instructor quickly about typos or other errors.

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## Implementation of a generic CSP

(Total 80 points)
The goal of this exercise is to write code for generating the data structures and accessor functions that will allow you to implement (most) CSPs, and to test your implementation by reading examples from files. This implementation may need to be refined as we progress in the course, but at least the basic building-blocks for initializing, storing, and manipulating CSPs should be available. It is very important that you take this task seriously and do the implementation as clearly and neatly
as possible: future homework will build upon this code. In you notice any errors in the design or the description: please quickly mention them to the instructor as you encounter them.

This exercise has two parts: one for creating the basic data structures ( 60 points), and the other one for generating the encoding of a CSP instance by reading the date from a file ( 20 points). General indications:

- Please make sure that you keep your code and protect your files. Your name, date, and course number must appear in each file of code that you submit.
- All programs must be compiled, run and tested on cse.unl.edu. Programs that do not run correctly in this environment will not be accepted.
- A README file must be submitted. Otherwise, the entire homework is declared invalid.

We strongly advise you to do these homework in Common Lisp: it is particularly well adapted for the type of algorithms and functionalities you will have to implement, which will greatly facilitate your task and yield short and easily debbugable code.

## 1 Basic data structures

Below we specify (as best we can) the data structures that need to be defined for storing the encoding of a CSP. When generating an encoding, we will generate instances of these general data structures. We will restrict ourselves to binary CSPs. Those looking for a real challenge may want to consider generalizing their code, now or later, to non-binary CSPs.

### 1.1 Main data structures

1. all-problems. Create a global variable (e.g., a linked list) for storing all CSP instances generated. Every time a CSP instance is generated, it should be pushed (preferably automatically) into this list. This is the data structure that we will go to in order to access any of the problems stored in memory.
2. Problem instance. Create a record-like data-structure for storing a CSP instance. (For lispers, use defstruct.) This data structure should have the following attributes:

- variables: to be filled with a list of the data structures corresponding to the variables. Alert: this is not a list of the names of the variables.
- constraints: to be filled with a list of the data structures corresponding to the constraints. This list can be implemented as a hash-table where a key is the list of variables in the scope of a given constraint and the value is a pointer to the definition of the constraint. No matter how you choose to implement this, you may consider to list the names of the variables in the constraint in alphabetical order in order to improve access.
- (optional) values: a list of all the values in the problem. Such a list is usually useful in scheduling and resource allocation applications to store all resources such as machines.

3. Variable. Create a record-like data-structure for storing a CSP variable. This data structure should have the following attributes:

- problem: a pointer to the problem data-structure to which the variable belongs.
- name: the variable name or identifier (e.g., a string, an integer).
- initial-domain: to be filled with the list of values in the domain of the variable.
- constraints: to be filled with a list of the data structures corresponding to the constraints that apply to the variable.
- neighbors: to be filled with a list of the data structures of the CSP variables that share a constraint with the variable.

4. Constraint. Use a class to declare and store a CSP constraint. This data structure should have the following attributes:

- problem: a pointer to the problem data-structure where the constraint appears.
- variables: a list of pointers to the variables in the scope of the constraint.
- definition: to store the definition of a constraint: either as a set of tuples (for a constraint defined in extension) or as a function (for a constraint defined in intention).

5. Extensional constraint. Use a class to declare and store a CSP constraint declared in extension. This class should be a subclass of the constraint class, and thus inherit its attributes.
The definition slot of the constraint should store the (linked) list of values that are allowed by the constraint in the lexicographical order of the variables. For instance:

$$
\begin{equation*}
C_{V_{1}, V_{2}}=\{(1,2),(3,5),(2,3), \ldots\} \tag{1}
\end{equation*}
$$

Alternatively, you could store the allowed tuples in an array of two dimensional array of size $d^{2} \times 2$, where $d$ is the max domain-size (more generally, the size is $d^{k} \times 2$, where $k$ is the max arity). Each row in this array is a tuple allowed by the constraint. (This is similar to a table in a relation database.)
6. Intentional constraint. Use a class to declare and store a CSP constraint declared in intention. This class should be a subclass of the constraint class, and thus inherit its attributes.

The definition slot of the constraint should store a function that determines whether a list of variable-value pairs given in lexicographical order of the variables satisfies the constraint. For the time being, restrict yourself to variable-value pairs corresponding to the variables in the scope of the constraint. This is the function that consistent-p (see below) will need to access.

### 1.2 Main functions/methods

Further, create the following methods that apply to this constraint data-structure:

- arity: should return the number of variables in the scope of the constraint.
- unary-p: should return true if the constraint applies exactly to one variable and false otherwise.
- binary-p: should return true if the constraint applies to exactly two variables and false otherwise.


## 2 Loading and initializing a CSP instance

You are requested to write a parser that reads the description of a CSP as shown below and generates an encoding of it according to the data structures you have defined above. Below, we tentatively specify the format of the files you will have to read to load the definition of a CSP instance and generate the corresponding data structures, which you will then have to use to solve the problem with search. The content of this section is adapted from Catherine Anderson.

We strongly advise you to use lex and yacc, which will tremendously facilitate this task. It is worth the investment to learn how to use them.

The ability of your code to successfully read and correctly encode each CSP will be graded 5 points.

### 2.1 Constraints defined in extension

The constraint definition is given as a set of tuples after the names of the variables over which is it defined.

### 2.2 Constraints defined in intension

Below we provide some 'standard' names for constraints defined in intension. In the problem definition, the name will be preceded by the sign \#'. Assuming P1 and P2 are the variable names that appear as the first two parameters of each constraint, consider implementing, as you need them, the following constraints:

- \#'> : greater than (P1 > P2)
- \#' +1 : incremented by 1 than $(\mathrm{P} 2=\mathrm{P} 1+1)$
- \#'geq : greater than or equal to $(\mathrm{P} 1 \geq \mathrm{P} 2)$
- $\#^{\prime}<$ : less than (P1<P2)
- \#'leq : less than or equal to ( $\mathrm{P} 1 \leq \mathrm{P} 2$ )
- \#'mutex : not equal to ( $\mathrm{P} 1 \neq \mathrm{P} 2$ )
- \#'nextTo : $\mathrm{P} 1=(\mathrm{P} 2+1)$ or $\mathrm{P} 1=(\mathrm{P} 2-1)$
- \#'diagonal : $|\mathrm{Pi}-\mathrm{Pj}| \neq|\mathrm{i}-\mathrm{j}|$ (n-queen constraint)


### 2.3 File format

The text below gives the definition of the problem to be solved, and will be sent as a file to the class by email. This file is a command line argument for the CSP Parser. The structure of the data file is as follows:

First bracket: Problem identifier (alphabet only, not digits or other characters). Example line:

```
{ name of problem}
```

Second bracket: Variables, where \# is the number of variables The formal of the like is as follows:

```
{ # { variableName1, variableName2, ..., variableNameN}}
```

Third bracket: specifies the domains of the variables as the list of lists of the variable name and the corresponding domain. The character * can be used as the name of last item in the list to denote all remaining variables (to avoid repetition when some variable have the same domain). Example line:

```
{ {variableName3{1,2,3,7}}
    {variableName2{hello,hi,ola}}
    {* {a,b,c,d}}}
```

Fourth bracket: Unary constraints. Lists only those variables that have them. Gives a variable name and a listing of the values allowed. If there are no unary constraints, include the empty braces: \{ \}. Example line:

```
{ {variableName2{4,7}}
    {variableName5{1,10}} }
```

Fifth bracket: Binary constraint. List each constraint only once, that is in one direction. The parser should take the intersection of the allowed tuples of multiple constraints between the same two variables. Example line:

```
{ {variableName1, variableName4, #'=}
    {variableName5, variableName13, #'+3} }
```

Sixth bracket: Special case: Large mutex groups. To be used when the mutex is between more than two variables. The first number is the number of mutex groups. This is followed by the listing of all the variables in each group, enclosed in braces. Example line:

```
{2 {VariableName1,variableName2,variableName3,variableName4,variableName5}
    {VariableName6,variableName7,variableName8,variableName9,variableName10}

Seventh bracket: Indicates which solver engine will be used (BT, BJ, CBJ, BM, BMJ, BMCBJ, FC, FCBJ, FCCBJ), whether or not AC3 will be run (true) or not (false) as a pre-processing step and whether a single solution (S) or all solutions (A) are requested. The sample given below indicates that BT search (chronological backtracking) will be run, without AC3 are a pre-processing step, stopping after one solution:
```

{BT, false, S}

```

\subsection*{2.4 Example file: 4-queen problem}

The full data file for the 4-queen problem is given below, starting and stopping before and after the line of \#\#\#\#\#\#\#\#.
```

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
{ Four Queen Problem Configuration}
{4 {Q1,Q2,Q3,Q4}}
{{*{1,2,3,4}}}
{ }
{ {Q1,Q2,{(1,3),(1,4),(2,4),(3,1),(4,1),(4,2)}}
{Q1,Q3,{(1,2),(1,4),(2,1),(2,3),(3,2),(3,4), (4,1), (4,3)}}
{Q1,Q4,{(1,2), (1,3),(2,1),(2,3),(2,4),(3,1), (3,2), (3,4), (4, 2), (4, 3)}}
{Q2,Q3,{(1,3), (1,4), (2,4), (3,1), (4,1), (4,2)}}
{Q2,Q4,{(1, 2), (1,4), (2,1), (2,3), (3,2), (3,4), (4,1), (4,3)}}
{Q3,Q4,{(1, 3), (1, 4), (2,4), (3,1), (4, 1), (4, 2)}}}
{}
{BT,false,S}
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

```

\subsection*{2.5 Example file: 6-queen problem}

The full data file for the 6 -queen problem is given below, starting and stopping before and after the line of \#\#\#\#\#\#\#\#.
```

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
{ Six Queen Problem Configuration}
{6 {Q1,Q2,Q3,Q4,Q5,Q6}}
{{*{1,2,3,4,5,6}}}
{ }
{ {Q1,Q2,\#'diagonal}
{Q1,Q3,\#'diagonal}
{Q1,Q4,\#'diagonal}
{Q1,Q5,\#'diagonal}
{Q1,Q6,\#'diagonal}
{Q2,Q3,\#'diagonal}
{Q2,Q4,\#'diagonal}
{Q2,Q5,\#'diagonal}
{Q2,Q6,\#'diagonal}
{Q3,Q4,\#'diagonal}
{Q3,Q5,\#'diagonal}
{Q3,Q6,\#'diagonal}

```
\{Q4,Q5,\#'diagonal\}
\{Q4,Q6,\#'diagonal\}
\{Q5,Q6,\#'diagonal\}\}
\{1 \{Q1,Q2,Q3,Q4,Q5,Q6\}\}
\{BT,false,S\}
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

\subsection*{2.6 Example file: Zebra}

The full data file for the zebra problem is given below, starting and stopping before and after the line of \#\#\#\#\#\#\#\#.
```

\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
{Zebra Problem configuration}
{25{Norway,England, Japan,Spain,Ukrane,blue,red,green, yellow,ivory, coffee,
tea,oj,milk,water,horse,snail,zebra,fox,dog,Chesterfield,Parliment,
LuckyStripe,Kool,OldGold}
}
{{*{1,2,3,4,5}}}
{ {Norway{1}}
{milk{3}}
}
{ {England,red,\#'=}
{Spain,dog,\#'=}
{coffee,green,\#'=}
{Ukrane,tea,\#'=}
{snail,OldGold,\#'=}
{Kool,yellow,\#'=}
{LuckyStripe,oj,\#'=}
{Japan,Parliment,\#'=}
{green,ivory,\#'+1}
{Chesterfield,fox,\#'nextTo}
{Kool,horse,\#'nextTo}
{Norway,blue,\#'nextTo}
}
{5 {Norway,England, Japan,Spain,Ukrane}
{blue,red,green,yellow,ivory}
{coffee,tea,oj,milk,water}
{horse,snail,zebra,fox,dog}
{Chesterfield,Parliment,LuckyStripe,Kool,OldGold}
}
{BJ,false,S}
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

```

\subsection*{2.7 Example file: Graduation-picture puzzle}

An additional problem is given below: Graduation Pictures. The following puzzle is a typical logic problem found in logic puzzle books. There is a graduation the local high school and a photographer takes a picture of Fay and 5 other young women (including Ms. Owens) in their graduation robes (each of a different color, including lavender) each standing on a step one higher then the person in front of them. From the following bits of information, find out the full names of the women, what color robes they each wore and which step they were standing on.
- Amy was on the step just below the Ms. Mertz and just above the women in green.
- Although Beth was not on the top step, she was above both the women in red and the Ms. Pinot.
- Coral stood below the Ms. Nash and above the women in green.
- Dana stood just below the women in blue and just above Ms. Lyons.
- Ms. Kelly stood just below Erin and just above the women in yellow.
- Ms. Mertz wasn't on step 4 and the Ms. Pinot wasn't on step 5.
- Coral did not wear yellow or pink.
```

Data file:
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
{Graduation Picture Problem Configuration}
{18 {Amy,Beth,Carol,Dana,Erin,Fay,blue,green,lavender, pink,red,
yellow,Kelly,Lyons,Mertz,Nash,Owens,Pinot}}
{{*{1,2,3,4,5,6}}}
{ {Mertz{1,2,3,5,6}}
{Pinot{1,2,3,4,6}}
{Beth{2,3,4,5,6}}
{Owens{2,3,4,5,6}}
}
{ {blue,Dana,\#'+1}
{Dana,Lyons,\#'+1}
{Erin,Kelly,\#'+1}
{Kelly,yellow,\#'+1}
{Mertz,Amy,\#'+1}
{Amy,green,\#'+1}
{red,Pinot,\#'mutex}
{Carol,yellow,\#'mutex}
{Carol,pink,\#'mutex}

```
```

{red,Beth,\#'>}
{Pinot,Beth,\#'>}
{Carol,Nash,\#'>}
{green,Carol,\#'>}
}
{3 {Amy,Fay,Beth,Carol,Dana,Erin}
{lavender,green,red,blue,yellow,pink}
{Owens,Mertz,Pinot,Nash,Lyons,Kelly}
}
{BJ,false,S}
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#

```
```

