

Computer Science & Engineering 155E Problem Solving Using Computers

Lecture 07 - Simple Data Types

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Chapter 7

- 7.1 Representation and conversion of numeric types
- 7.2 Representation and conversion of type `char`
- 7.3 Enumerated Types
- 7.5 Common Programming Errors

We have used three standard data types: `int`, `double`, and `char`.

- ▶ Type `int` values are used in C to represent both the numeric concept of an integer and the logical concepts `true` and `false`.
- ▶ Standard types and user-defined enumerated types are **simple**, or *scalar*, **data types** because only a single value can be stored in a variable of each type.

Representation and Conversion of Numeric Types

- ▶ Differences Between Numeric Types
- ▶ Numerical Inaccuracies
- ▶ Automatic Conversion of Data Types
- ▶ Explicit Conversion of Data Types

Differences Between Numeric Types

Uses of different data types:

- ▶ Data type `double` can be used for (many) "real" numbers.
- ▶ But:
 - ▶ Operations involving integers are faster than those involving `double`
 - ▶ Less storage space is needed to store type `int` values (32-bits versus 64-bits)
 - ▶ Operations with integers are always precise, whereas some loss of accuracy can occur when dealing with type `double` numbers.
- ▶ These differences result from the way numbers are represented in the computer's memory.

Round-off Error I

Example

```
1 b = 2.0;
2 printf("b = %.20f\n", b);
3 b = sqrt(2.0);
4 b = pow(b, 2.0);
5 printf("b = %.20f\n", b);
```

Output:

```
1 b = 2.00000000000000000000
2 b = 2.000000000000000044409
```

Round-off Error II

Example

- ▶ Certain numbers, such as $\sqrt{2}$ are *approximated*
- ▶ Internally, some interpolation method(s) are used
- ▶ Thus, $\text{sqrt}(2.0) = 1.41421356\dots$ is not accurate in the lower order digits

Base 10

- ▶ Humans have 10 fingers, so we naturally developed counting in *base-10*
- ▶ Single numbers are represented using arabic numerals 0 thru 9
- ▶ Single numbers are multiplied by various *powers of 10* and added together to form any possible number in base-10

$$532.41 = 5 \times 10^2 + 3 \times 10^1 + 2 \times 10^0 + 4 \times 10^{-1} + 1 \times 10^{-2}$$

Base 2

- ▶ Computers do not have fingers; they only have *states*: on/off, high-voltage/low-voltage, etc.
- ▶ Thus, computers work in base-2: *binary*
- ▶ All data are represented in memory as *binary strings*, strings of 0s and 1s.
- ▶ Single numbers are limited to 0, 1
- ▶ Single numbers are multiplied by various *powers of 2* and added together to form any possible number in base-2

$$\dots + b_2 \times 2^2 + b_1 \times 2^1 + b_0 \times 2^0 + b_{-1} \times 2^{-1} + b_{-2} \times 2^{-2} + \dots$$

Base Conversion

- ▶ Algorithms for conversion are straightforward, but beyond this course
- ▶ Necessary to simply understand what's going on behind the scenes

$$\begin{aligned} 110.011 &= 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-3} \\ &= 1 \times 4 + 1 \times 2 + 0 \times 1 + 0 \times \frac{1}{2} + 1 \times \frac{1}{4} + 1 \times \frac{1}{8} \\ &= 4 + 2 + 0 + 0 + \frac{1}{4} + \frac{1}{8} \\ &= 6.375 \end{aligned}$$

Data Representation I

- ▶ The binary string stored for type in value 13 is not the same as the binary string stored for 13.0
- ▶ Integers are whole numbers and so have a definite end (nothing to the right of the decimal)
- ▶ Floating point numbers could have any number of bits to the left and to the right of the decimal
- ▶ In order to represent a larger range of values, computers store floating point numbers in a manner analogous to *scientific notation*

Scientific Notation I

- ▶ Scientific Notation (base-10): any number is "normalized" by shifting the decimal place so that it is between 0 and 10:

$$14326.123 \rightarrow 1.4326123E4$$

$$0.00529 \rightarrow 5.29E-3$$

- ▶ Similarly, floating point numbers (**double**, **float**) are divided into two sections: the *mantissa* and the *exponent*.

Scientific Notation II

- ▶ The mantissa is a binary fraction between $\frac{1}{2} = 2^{-1}$ and $1 = 2^0$ for positive numbers and between -0.5 and -1.0 for negative numbers.
- ▶ The exponent is an integer.
- ▶ The mantissa and exponent are chosen so that:

$$real\ number = mantissa \times 2^{exponent}$$

- ▶ Because of the finite size of memory cell, not all real numbers in the range allowed can be represented precisely as type double values (irrationals, even rationals such as 1/3).

Mantissa-Exponent Example I

- ▶ Let 110.011 be our number as before
- ▶ Shift right to get the Mantissa: .110011
- ▶ We had to shift 3 places, so the exponent is 3 (in binary, that is 11)

Mantissa-Exponent Error I

- ▶ When converting to the mantissa-exponent format, we may shift *lower order bits* out of range (we can only hold 64 bits)
- ▶ Bits shifted out of range are dropped, leading to round off error

Range of Types

Table: Range of values typical in most C implementations

Type	Range
short	-32,767 ... 32,767
unsigned short	0 ... 65,535
int	-32,767 ... 32,767
unsigned int	0 ... 65,535
long int	-2,147,483,647 ... 2,147,483,647
unsigned long int	0 ... 4,294,967,295

Range of Types

Table: Range of values according to the ANSI C specification

Type	Approximate Range	Significant Digits	Bits (CSE)
float	$10^{-37} \dots 10^{38}$	6	32
double	$10^{-307} \dots 10^{308}$	15	64
long double	$10^{-4931} \dots 10^{4932}$	19	128

Numerical Inaccuracies I

- ▶ **Representation error:** some fractions cannot be represented in the decimal number system (e.g., 1/3 is 0.3333...), some fractions cannot be represented exactly as binary numbers in the type `double` format.
 - ▶ Sometimes called *round-off error*
 - ▶ This depends on the number of binary digits used in the mantissa. More bits \rightarrow smaller error.
 - ▶ Because of this kind of error, an equality comparison of two type `double` values can lead to surprising results.
 - ▶ `for(i=0.0; i != 10.0; i+=0.1) ...`
 - ▶ Problems can occur when manipulating very large and very small real numbers.

Numerical Inaccuracies II

- ▶ **Cancellation error** Adding a small number to a large number, the larger number may “cancel out” the smaller number.
- ▶ If x is much larger than y , then $x + y$ may have the same value as x (example: $1000.0 + 0.0000001234$ is equal to 1000.0 on some computers).
- ▶ **Arithmetic underflow**: Multiplying small numbers may cause the result to be too small to be represented accurately, so it will be represented as zero.
- ▶ **Arithmetic overflow**: adding/multiplying large number (recall: 13!)

Round-Off Error Example

Recall the round cents function we wrote:

```
1 double roundCents(double m) {
2     double x;
3     x = m * 100;
4     x = floor(x);
5     x = x / 100;
6
7     printf("m-x = %.50f\n", m-x);
8     if(m - x >= 0.005)
9     {
10         x = x + .01;
11     }
12     return x;
13 }
```

Round-Off Error Example

First run:

```
1 enter a number: 100.075
2 m-x = 0.0050000000000000966338120633736252784729003906250000
3 The rounded value is: 100.080000
```

Second run:

```
1 enter a number: 171.065
2 m-x = 0.004999999999999545252649113535881042480468750000000
3 The rounded value is: 171.060000
```

Automatic Conversion of Data Types

```
1 int    k = 5,    m = 4,    n;
2 double x = 1.5, y = 2.1, z;
```

- ▶ $k + x$: k is converted before adding since x is of type `double`
- ▶ $z = k / m$: conversion is done after division, since both operands are of type `int`
- ▶ $n = x * y$: $x * y$ evaluates to get 3.15 , but then is converted to 3 to store it in a type `int`
- ▶ These conversions are *automatic* and *implicit*

Explicit Conversion of Data Types

- ▶ In addition to automatic conversions, C also provides an explicit type conversion operation called a **cast**:
`z = (double)k / (double)m;`
- ▶ The value to be converted causes the value to change to `double` data format *before* it is used in the computation
- ▶ Casting is a very high precedence operation, so it is performed before the division
- ▶ `(double)(k/m)` will do k/m first: The highest precedence operator is always the parentheses

Enumerated Types

- ▶ Certain programming problems require *new* data types
- ▶ Ex: it makes sense in a calendar program to be able to distinguish between months
- ▶ C allows you to associate a numeric code with each category by creating an **enumerated type** that has its own list of meaningful values.

```
1 typedef enum {
2     january, february, march, april, may,
3     june, july, august, september, october,
4     november, december}
5 month_t;
```

Enumerated Types

- ▶ Defining type `month` as shown causes the **enumeration constant** `january` to be represented as the integer 0, `february` to be represented as integer 1, etc.
- ▶ Variable `month` and the twelve enumeration constants can be manipulated just as one would handle any other integers.
- ▶ Like variables and functions, user defined types must be defined *before* you use them
- ▶ Enumerated types are *integers*, the keywords associated with them cannot be printed
- ▶ Be careful when doing arithmetic operations on enumerated types

Enumerated Types

```
1  month_t myMonth;  
2  myMonth = january;  
3  myMonth++;  
4  if (myMonth == february)  
5      printf("True");  
6  else  
7      printf("False");  
8  
9  printf("myMonth = %d",myMonth);  
10 myMonth = myMonth + 100000;
```

Common Programming Errors I

- ▶ Arithmetic underflow and overflow resulting from a poor choice of variable type are common causes of run-time errors
- ▶ Programs that approximate solutions need to be careful of rounding errors
- ▶ When defining enumerated types, only identifiers can appear in the list of values for the type.

Common Programming Errors II

- ▶ Do not reuse one of the identifiers in another type, as a variable name, etc. (compile error)
- ▶ Keep in mind that there is no built-in facility for input/output of the identifiers that are the valid values of an enumerated type. You must either display the underlying integer representation or write your own input/output functions.