A Temporal View of The Topology of Dynamic Bittorrent Swarms

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Abstract—This paper describes an experimental study of the overlay topologies of real-world Bittorrent networks, focusing on the activity of the nodes of its P2P topology and especially their dynamic relationships. Peer Exchange Protocol (PEX) messages are analyzed to infer topologies and their properties, capturing the variations of their behavior. Our measurements, verified using the Kolmogorov-Smirnov goodness of fit test and the likelihood ratio test and confirmed via simulation, show that a power-law with exponential cutoff is a more plausible model than a pure power-law distribution. We also found that the average clustering coefficient is very low, supporting this observation. Bittorrent swarms are far more dynamic than has been recognized previously, potentially impacting attempts to optimize the performance of the system as well as the accuracy of simulations and analyses.

I. INTRODUCTION

Among P2P applications, Bittorrent is the most popular. In 2008, P2P transfer dominated Internet traffic and Bittorrent is the most popular P2P protocol. P2P traffic is still growing, though recent studies suggest that its growth is slower than that of Internet traffic as a whole [1] [2].

Many properties of Bittorrent, such as upload/download performance and peer arrival and departure processes, have been studied [3], but only a few projects have assessed the topological properties of Bittorrent. The Bittorrent system is different from other P2P systems. The Bittorrent protocol does not offer peer traversal and the Bittorrent tracker also does not know about topologies since peers never send information to the tracker concerning their connectivity with other peers. While a crawler can be used in other P2P networks, such as Gnutella, in Bittorrent we cannot easily use a crawler to discover topology, making direct measurement of the topology difficult.

In this paper we describe our study of Bittorrent networks, where real-world Bittorrent swarms were measured using a rigorous and simple method in order to understand the Bittorrent network topology. To our knowledge, our approach is the first to perform such a study on real-world Bittorrent network topologies. We used the Bittorrent Peer Exchange (PEX) messages to infer the topology of Bittorrent swarms listed on a Bittorrent tracker claiming to be the largest Bittorrent network on the Internet [4] [5], instead of building small Bittorrent networks on testbeds such as PlanetLab and OneLab as other researchers have done. We also performed simulations using the same approach to show the validity of the inferred topology resulted from the PEX messages by comparing it with the topology of the simulated network.

In addition to demonstrating the validity of our measurement methods, we show that a power-law with exponential cut-off distribution is a better model than a pure power-law distribution. In terms of the clustering property, we show Bittorrent networks is more of a random network than a scale-free network. While these results may contradict earlier findings, our simulations also demonstrated the same phenomenon.

The rest of this paper is organized as follows. We first briefly explain the Bittorrent PEX, followed by the experiment methodology to infer Bittorrent network topologies using PEX. In the analysis, this paper looks into the PEX messages by comparing it with the topology of the simulated network.

II. BITTORRENT PEER EXCHANGE

Bittorrent is a P2P application designed to distribute large files with a focus on scalability and efficiency. When joining a swarm, a Bittorrent application contacts a tracker, which responds with an initial peer set of randomly selected peers, possibly including seed and leecher IP addresses and port numbers. PEX is a mechanism introduced in Bittorrent to discover other peers in the swarm, in which two connected
peers exchange messages containing a set of connected peers. With PEX, peers only need to use the tracker as an initial source of peers.

It appears that most clients began to introduce PEX in 2007 [6]. However, there is no PEX specification, only a kind of informal understanding among Bittorrent client developers. Therefore, there are differences, e.g., for some Bittorrent clients derived from rasterbar libtorrent [7], the PEX message can only contain a maximum of a hundred IP address and port pairs. In other Bittorrent clients, the number of IP address and port pairs is decided based on the size of the PEX message. This implementation difference may affect the ultimate behavior of the network.

III. Methodology and Experiment Design

We used PEX to collect peer neighbors information (see Figure 1) and then we describe the network formed in terms of properties such as node degree and average clustering. Besides collecting data from real Bittorrent networks, we ran simulations similar to these of Al-Hamra et al. [8]. In these simulations, we assumed that peer arrivals and departures (churn) follow an exponential distribution as explained by Guo et al. [3]. For simplification, we assumed that nodes are not behind a NAT. Since we are only interested in the construction of the overlay topology, we argue that our simulations are thorough enough to explain the overlay properties.

Temporal graphs have recently been proposed to study real dynamic graphs, with the intuition that the behavior of dynamic networks may be more accurately captured by a sequence of snapshots of the network topology as it changes over time. An instantaneous snapshot is taken at an exact time point, thus capturing only a few nodes and links. In this paper, we study the network dynamics by continuously taking network snapshots with the duration \( \tau \) as time evolves, and show them as a time series. A snapshot captures all participating peers and their connections within a particular time interval, from which a graph can be generated. The snapshot duration may have minor effects on analyzing slowly changing networks. However, in a P2P network, the characteristics of the network topology vary greatly with respect to the time scale of the snapshot duration [9]. We consider \( \tau = 3 \) minutes to be a reasonable estimate of minimum session length in Bittorrent [10].

A. Graph Sampling

Suppose that a Bittorrent overlay network is a graph \( G(V, E) \) with the peers as nodes or vertices and connections between the peers as edges. If we observe the graph in a time series, i.e., we take samples of the graph, the time-indexed graph is \( G_t = G(V_t, E_t) \). We define a measurement window \([t_0, t_0 + \tau]\) and select peers at random from the set:

\[
 V_{t_0, t_0+\Delta} = \bigcup_{t=t_0}^{t_0+\tau} V_t. \tag{1}
\]

Stutzbach et al. [11] showed that Equation (1) is only appropriate for exponentially distributed peer session lengths but we know from existing measurements that Bittorrent networks peer session lengths have very high variation [3]. Equation (1) focuses on sampling peers instead of peer properties. To cope with this problem, we must be able to sample from the same peer more than once at different points in time [11]. We may rewrite our desired sample as

\[
 v_{i,t} \in V_t, t \in [t_0, t_0 + \tau]. \tag{2}
\]

The number of peers in a swarm that is observed by our client is our population. The sampled peers set is the number of peers that exchange PEX messages with our client. Our sampled peers set through PEX messages exchange can observe about 70% of the peers in a population. This observation is consistent with [12].

B. Experimental Methodology

We joined the top 35 TV series torrents from the piratebay, which claims to be the biggest torrent tracker on the Internet. Almost all of these torrents were in steady-state phase, which is more dominant than bootstrapping and decay phase of Bittorrent’s lifetime. We used a modified rasterbar libtorrent [7] client that is connection greedy, where the client tries to connect to all peers it knows without a limit on the number of connections, and the client logs PEX messages received from other clients. PEX messages from old versions of Vuze Bittorrent clients contain all of peers they connected to in the past, hence these clients should be removed from the data. Removal of some peers in data processing is valid in terms of sampling with dynamics, see equation (2). In terms of connectivity, two popular Bittorrent clients: uTorrent and Vuze, by default try to connect to peer candidates randomly without any preference, thus we have random data sets. This implies that our data set is independent of measurement location and the number of measurement locations.

C. Data Analysis Background

Many realistic networks exhibit the scale-free property [13], though we note that “scale-free” is not a complete description of a network topology [14] [15]. It has been suggested that
Bittorrent networks also might have scale-free characteristics [16]. In this paper, we test this hypothesis.

In a scale-free network, the degree distribution follows a power-law distribution. A power-law distribution is quite a natural model and can be generated from simple generative processes [17], and power-law models appear in many areas of science [13] [17].

A power-law distribution can be described as

\[ Pr[X \geq x] \propto x^{-\alpha}. \]  

where \( x \) is the quantity of distribution and \( \alpha \) is commonly called the scaling parameter. The scaling parameter usually lies in the range \( 1.8 < \alpha < 3.5 \). In discrete form, the above formula can be expressed as:

\[ p(x) = Pr(X = x) = Cx^{-\alpha}. \]  

This distribution diverges on zero, therefore there must be a lower bound of \( x \), called \( x_{min} > 0 \), that holds for the sample to be fitted by a power-law. If we want to estimate a good power-law scaling parameter then we must also have a good \( x_{min} \) estimation.

We use maximum likelihood to estimate the scaling parameter \( \alpha \) of power-law [13]. This approach is accurate to estimate the scaling parameter in the limit of large sample size. For the detailed calculations of both \( x_{min} \) and \( \alpha \), see Appendix B in [13].

IV. EXPERIMENT RESULTS

The CDF of the number of peers for every swarm during measurement is shown in figure 2. It is clear that the number of peers has high variability due to churns in Bittorrent networks.

A. Power-law Distribution of Node Degree

We want to know the power-law distribution of the measured Bittorrent networks, and we do not know \textit{a priori} if our data are power-law distributed. Simply calculating the estimated scaling parameter gives no indication of whether the power-law is a good model. To test the applicability of a power-law distribution, we use the goodness-of-fit test as described by Clauset et al. [13]. First, we fit data to the power-law model and calculate the Kolmogorov-Smirnov (KS) statistic for this fit. Second, we generate power-law synthetic data sets based on the scaling parameter \( \alpha \) estimation and the lower bound of \( x_{min} \). We fit the synthetic data to a power-law model and calculate the KS statistics, then count what fraction of the resulting statistics is larger than the value for the measured data set. This fraction is called the \( p \) value. If \( p \geq 0.1 \) then a power-law model is a good model for the data set, and if \( p < 0.1 \) then power-law is not a good model.

As mentioned before, a good estimation for \( x_{min} \) is important to get a overall good fit. Too small an \( x_{min} \) will cause a fit only to the body of the distribution. Too high an \( x_{min} \) will cause a fit only to the tail of the distribution. Figure 3 illustrates the fit for snapshots of \textit{torrent1} and \textit{torrent3}. For \textit{torrent1}, setting \( x_{min} = 2 \) leads to \( \alpha = 2.11 \), while \( x_{min} = 1 \) gives \( \alpha = 2.9 \). For \textit{torrent1}, \( x_{min} = 1 \) visually does not give a good fit, while for \textit{torrent3}, setting \( x_{min} = 1 \) leads to a visually good fit.

Figure 4 shows the CDF for \( p \) values for all data sets. This figure shows that from the K-S statistics point of view, around 45% of the time, Bittorrent networks do not follow a power-law model.

However these data sets must be interpreted with care. The usage of the maximum likelihood estimators for parameter estimation in power-law is guaranteed to be unbiased only in the asymptotic limit of large sample size, and some of our data sets fall below the rule of thumb for sample size, \( n = 50 \) [13]. In the goodness-of-fit test, a large \( p \) value does not mean the power-law is the correct distribution for data sets, because there may be other distributions that match the data sets and there is always a possibility that small value of \( p \) the distribution will follow a power-law even though the power-law is not the right model [13]. We address these concerns next.

B. Alternative Distributions

Even if we have estimated the power-law parameter properly and the fit is decent, it does not mean the power-law model...
is good. It is always possible that non-power-law models are better than the power-law model. We use the likelihood ratio test [18] to see whether other distributions can give better parameter estimation. We only consider a power-law model and a power-law with exponential cut-off model as examples to show model selection. Model selection for power-law model and power-law with exponential cut-off is a kind of nested model selection problem. In a nested model selection, there is always the possibility that a bigger family (power-law) can provide as good a fit as the smaller family (power-law with exponential cut-off). In likelihood ratio test, we must provide the significance value ($\rho$ value). For concrete explanation and real-world examples, we refer the readers to [13].

Under the likelihood ratio test, we compare the pure power-law model to power-law with exponential cut-off, and the $\rho$ value here helps us establish which of three possibilities occurs: (i) $\rho > 0.1$ means there is no significant difference between the likelihood of the data under the two hypotheses being compared and thus neither is favored over the other; if we already rejected the pure power-law model, then this does not necessarily tell us that we also can reject the alternative model; (ii) $\rho < 0.1$ and the sign of $LR = -$ negative means that there is a significant difference in the likelihoods and that the alternative model is better; if we have already rejected the pure power-law model, then this case simply tells us that the alternative model is better than the bad model we rejected; (iii) if $\rho < 0.1$ and the sign of $LR = +$ positive means that there is a significant difference and that the pure power-law model is better than the alternative; if we have already rejected the pure power-law model, then this case tells us the alternative is even worse than the bad model we already rejected.

Figure 5 shows a $p$ value vs $\rho$ value scatter plot, divided into three areas. Area 1: $p$ value $< 0.1$ and $\rho$ value $> 0$. Area 2: $p$ value $> 0.1$ and $\rho$ value $< 0.1$ Area 3: $\rho$ value $> 0.1$ and $p$ value $> 0.1$. This figure shows that 52% of the samples lie in area 1, thus an alternative model may be plausible for these samples.

Now we plot $p$ value vs LR as shown in figure 6 for $\rho < 0.1$. We divide the figure into four areas: area 1, area 2, area 3, and area 4 with green lines as borders to see how sparse the points in each area. Area 1: LR=positive sign and $p$ value $< 0.1$. Area 2: LR=positive sign and $p$ value $> 0.1$. Area 3: LR=negative sign and $p$ value $< 0.1$. Area 4: LR=negative sign and $p$ value $> 0.1$. In this figure, 58% of the samples lie in area 3 and 42% lie in area 4, while there are no samples in areas 1 and 2, which means that the alternative model is better. Although in the case $p$ value $< 0.1$ we reject power-law as the plausible model, the alternative model is still better than the power-law model. We believe that these results are caused by peers that are not willing to maintain large numbers of concurrent connections (high node degree). These observations clearly demonstrate that comparing the model to other models is a very complex task in highly dynamic networks.

C. Clustering Coefficient

Clustering describes the topology robustness. It has practical implications; for example, if node A is connected to node B and node B to node C, then there is a probability that node A will also be connected to node C, improving the robustness of the network against the failure of a connection. Clustering is quantified by a node clustering coefficient as follows:

$$c_v = \frac{2T(v)}{\text{deg}(v)(\text{deg}(v) - 1)}$$  \hspace{1cm} (5)

and for the whole graph the clustering coefficient is

$$C = \frac{1}{n} \sum_{v \in G} c_v.$$  \hspace{1cm} (6)

A larger clustering coefficient represents more clustering at nodes in the graph, therefore the clustering coefficient expresses the local robustness of the network. The distinction between a random and a non-random graph can be measured by clustering-coefficient metrics [19]. A network that has a high clustering coefficient and a small average path length is called a small-world model [19]. Newman [20] mentions that virus outbreaks spread faster in highly clustered networks.
In Bittorrent systems, a previous study [21] mentioned the possibility that Bittorrent’s efficiency partly comes from the clustering of peers. Figure 7 shows the CDF clustering coefficient value of our data sets. Only one torrent exhibits clustering coefficient less than 0.1 for about 40% of the snapshots, while for the other torrents, more than 70% are less than 0.1. This low clustering coefficient observation is the same as that observed by Dale et al. [16]. Considering only the low clustering coefficient, the Bittorrent topologies seem to be close to random graphs.

V. CONFIRMATION VIA SIMULATION

Here we use simulations to compare the overlay topology properties based on our real-world experiments. We set the maximum peer set size to 80, the minimum number of neighbors to 20, and the maximum number of outgoing connections to 80. In our simulation, the result is quite easy to get since we are on a controlled system; we can directly read the global topology properties from our results. We also have the simulated PEX messages. We compare the global overlay topology properties as the final result from the simulator with the overlay topology that we get from PEX on the same simulator. Figure 8 shows the $\alpha$ estimate and $p$ value both for the global result and the PEX result from our simulator. It clearly shows that global result and the PEX result from the simulator produce very low $p$ values. We calculate the Spearman correlation for both $\alpha$ values from the global result and the PEX result. The Spearman rank correlation coefficient is a non-parametric correlation measure that assesses the relationship between two variables without making any assumptions of a monotonic function. The Spearman rank correlation test gives $0.38 \leq \rho \leq 0.5$, which we consider to be moderately well correlated.

VI. RELATED WORK

Bittorrent protocol performance has been explored extensively [3] [22] [23] [24]. The rarest first algorithm was discussed in [22], average download speed was discussed in [23], peer arrival and departure process was discussed in [3] and the effect of distributon of the peers on the download job progress was discussed in Y.Tian et al. [24]. The huge numbers of peers sending P2P download requests to random targets on the Internet and anti-P2P companies injecting bogus peers through PEX were discussed in Z.Li et al. [25]. Higher upload-to-download ratios in Bittorrent darknet were discussed in C.Zhang et al. [26]. Although we know that the topology can have a large impact on performance, to date only a few papers have addressed the issue. Urvoy et al. [27] used a discrete event simulator to show that the time to distribute a file in a Bittorrent swarm has a strong relation to the overlay topology. Al-Hamra et al. [28], also using a discrete event simulator, showed that Bittorrent creates a robust overlay topology and the overlay topology formed is not random. They also show that peer exchange (PEX) generates a chain-like overlay with a large diameter. Dale et al. [16], in an experimental study on PlanetLab, show that in the initial stage of Bittorrent a peer will get a random peer list from the tracker. They found that a network of peers that unchoked each other is scale-free and the node degree follows a power-law distribution with exponent approximately 2. Dale et al. [16] also showed that the path length formed in Bittorrent swarms averages four hops and Bittorrent swarms have low average clustering coefficient. However, little work has been done on determining that topology in the real world. Our results agree with previous research [16] in some areas and disagree in others, perhaps for two reasons. First, power-law claims must be handled carefully. Many steps are required to confirm the power-law behavior, including alternative model checking, and we must be prepared for disappointment since other models may give a better fit. Second, our methodology relies on real work measurement combine with simulation for validation. We are using real swarms from a real and operational Bittorrent tracker. This real-world measurement will reflect different types of clients connected to our swarm, and each client has a different behavior. We also face difficult-to-characterize network realities such as NAT and firewalls. Our ability to reproduce key aspects of the topology dynamics suggests that these factors have only limited impact on the topology, somewhat to our surprise.
VII. CONCLUSION AND FUTURE WORK

We have investigated the properties of Bittorrent overlay topologies from the point of view of the peer exchange protocol using real swarms from a real and operational Bittorrent tracker on the Internet. We obtain instantaneous snapshots of the active topology of the Bittorrent network over a month. We cope with the dynamics of the overlay by sampling peer properties. Our results agree in some particulars and disagree in others with prior published work on isolated testbed experiments on Bittorrent, suggesting that more work is required to fully model the behavior of real-world Bittorrent networks. Unlike [16], we find that the node degree of the graph formed in a Bittorrent swarm can be described by a power law with exponential cut-off, and the observation of a low clustering coefficient implies Bittorrent networks are close to random networks. Some areas of improvement that we have identified for future work are: more correlation analysis of the number of peers with $\alpha$ and $p$ value, continued characterization with NAcED peers, wider likelihood ratio test with other models and comparing the results with simulation for global graph properties such as distance distribution and spectrum. We hope to incorporate these properties into a complete $dK$ series for the evolution of a real-world Bittorrent overlay as it evolves over time [15]. We conclude that further work throughout the community is necessary to continue to improve the agreement of simulation and controlled experiment with the real world, and that such work will impact our understanding of Bittorrent performance and its effects on the Internet.

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